

# TSC Modelling of Current Ramp Scenarios with ITB-Generated Bootstrap Currents in JT-60U Reversed Shear Discharges

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*JT-60U*

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# Outline

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- A Modelling of Internal & Edge Transport Barriers (ITB & ETB) relevant to bootstrap currents has been implemented on TSC.
- The TSC nicely reproduced a specified ramp-up of JT-60U RS discharge assisted with the ITB & ETB-generated bootstrap currents.
  - A self-adjustment of the ITB-foot radius ( $r_{\text{foot}}$ ) to the magnetic shear reversal ( $q_{\text{min}}$ ) results in a remarkable recover of the ramp-up detail (E36486).
  - A mis-alignment of  $r_{\text{foot}}$  with  $q_{\text{min}}$  leads to outward or inward drift of ITBs, which show quite different profile property.
- A fast and strong ITB build-up near plasma core may cause an over-drive bootstrap current which accompanies a negative electric field just inside of the ITB region.
  - ➔ The TSC has demonstrated a detailed process of Current Hole formation.

# ITB & ETB Modelling on TSC

JT-60U

TSC is a free boundary, axisymmetric, single fluid, time-evolution code with PF coil power supplies,  
 ➔ realistic ramp-up simulation available.

- ITB & ETB Model
  - Prescribed pressure profiles given by functions of hyperbolic tangent of radius ( ).
  - Radii of ITB-foot &  $q_{\min}$  monitored were adjusted during TSC simulations.

- Numerical Model

- Momentum eq. of single fluid  $\mathbf{m}$  :

$$\frac{d\mathbf{m}}{dt} + \mathbf{F}_v(\mathbf{m}) = \mathbf{j} \times \mathbf{B} - \nabla p$$

- Faraday's law for  $\mathbf{g}$  & time-evolution

$$\frac{d\mathbf{B}}{dt} = -\nabla \times \mathbf{E} \quad ; \quad \nabla \times \mathbf{B} = \mathbf{j} + \mathbf{g}$$

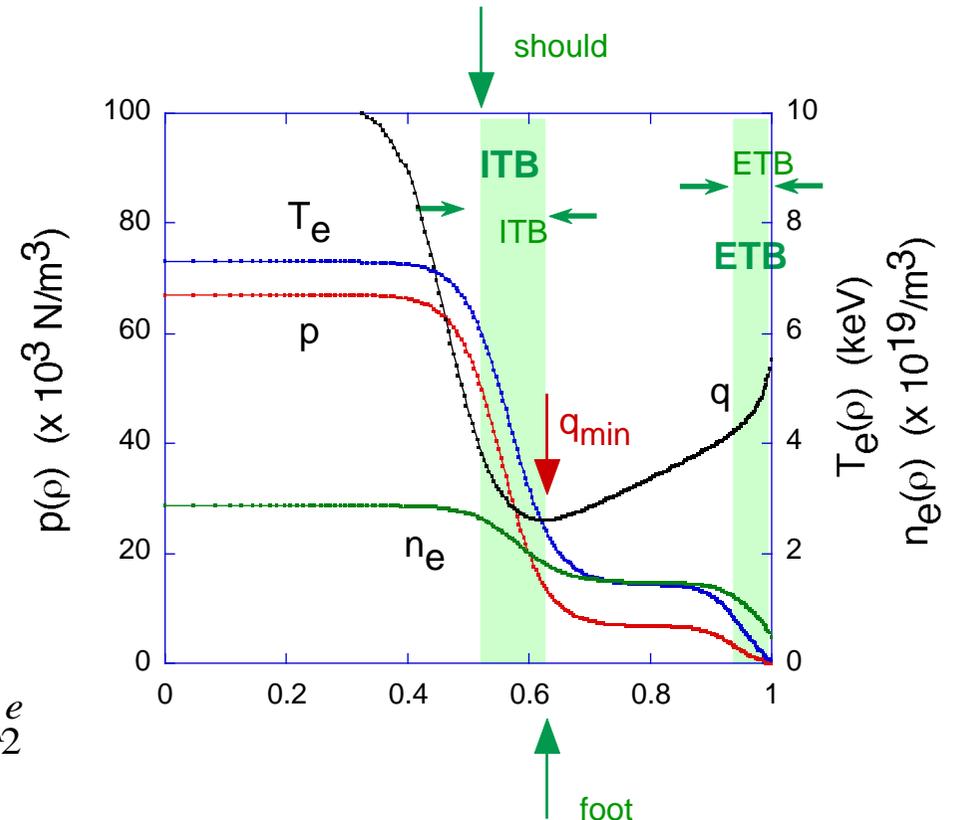
- Ohm's law :  $\mathbf{j}_{\text{oh}} = \mathbf{j}_{\text{total}} - \mathbf{j}_{\text{bs}}$

$$\mathbf{E} + \mathbf{v} \times \mathbf{B} = \mathbf{j}_{\text{oh}}$$

- ITB & ETB-generated BS Current

$$\langle \mathbf{j}_{\text{bs}} \cdot \mathbf{B} \rangle = L_{31} \left[ A_1^e + Z_i^{-1} T_i / T_e \left( A_1^i + \sum_i A_1^e \right) \right] + L_{32} A_2^e$$

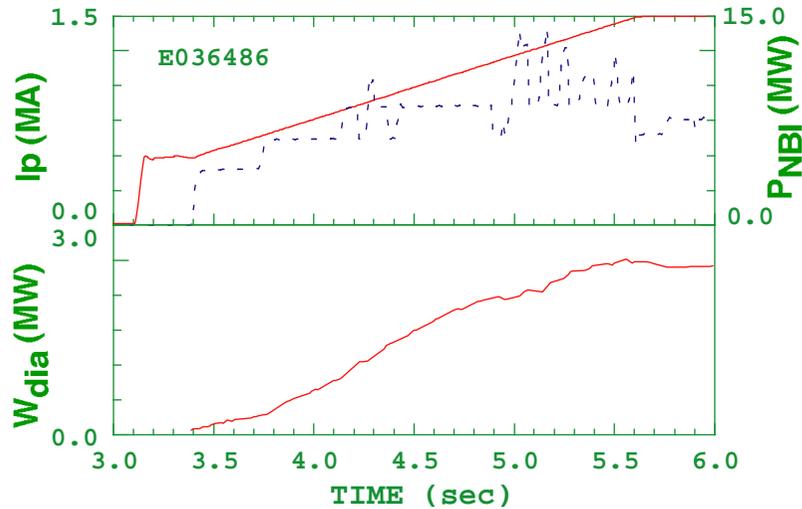
S. P. Hirshman, Phys. Fluids 31 (1988) 3150.



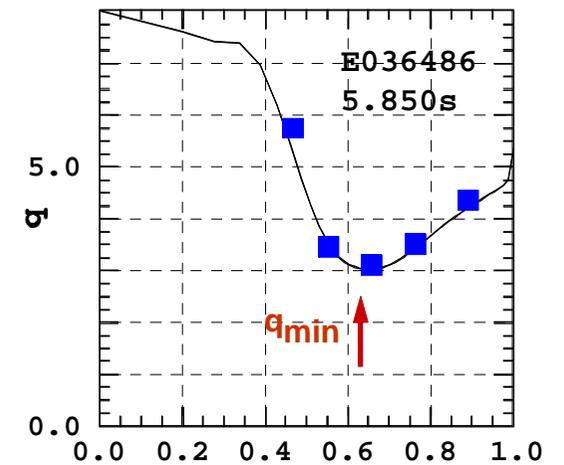
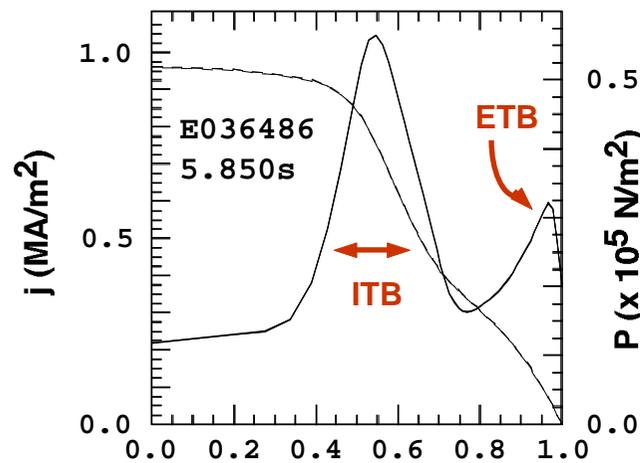
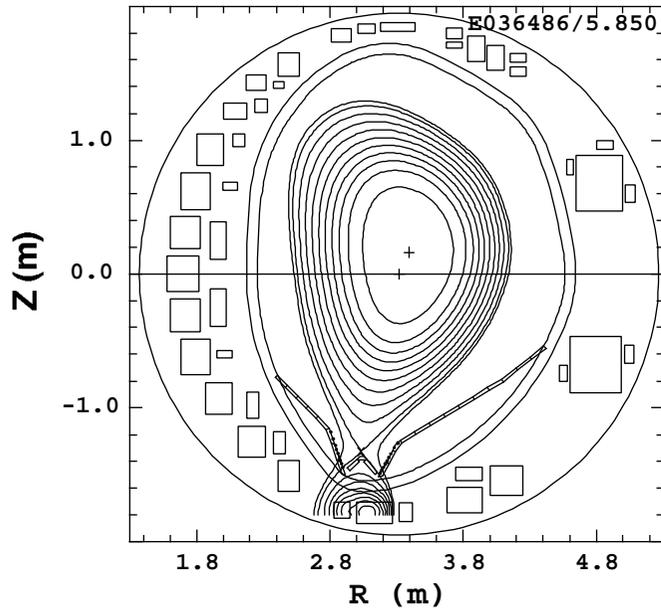
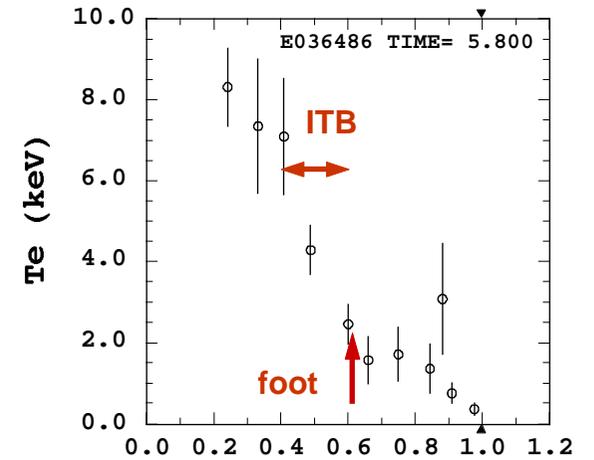
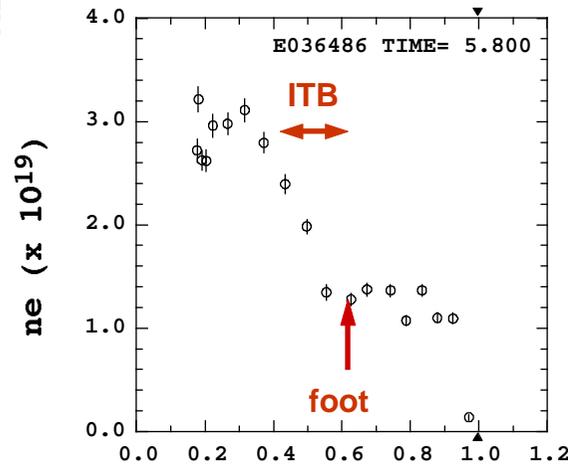
# Standard Ramp-up with ITB-Generated BS Current in JT-60U

JT-60U

- A well shaped RS discharge of 1.5 MA at 5.8 sec (E36486)



- foot  $\sim 0.6$  from  $T_e(\rho)$ ,  $n_e(\rho)$
- $(q_{min}) \sim 0.6$  from  $j(\rho)$  &  $q(\rho)$   $\rightarrow$  foot  $\sim (q_{min})$



# TSC Reproduction of $I_p$ Ramp-up with ITB Model : $foot = (q_{min})$

JT-60U

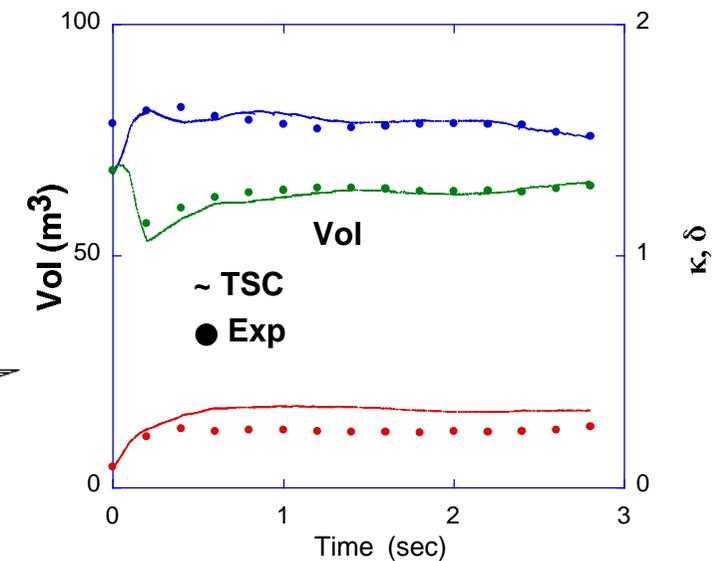
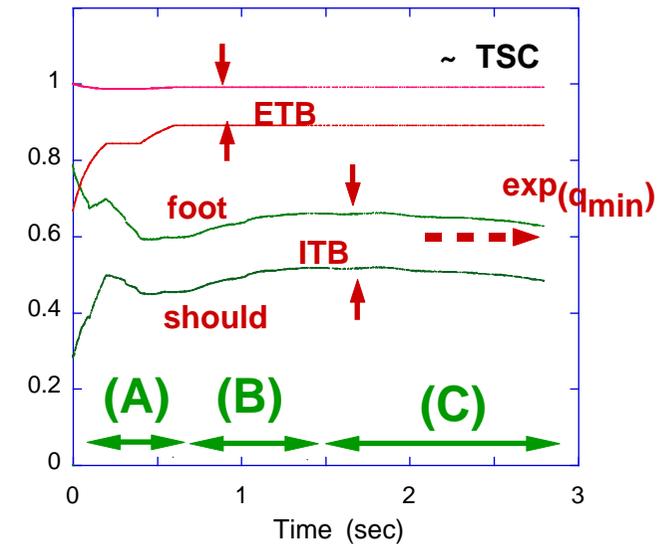
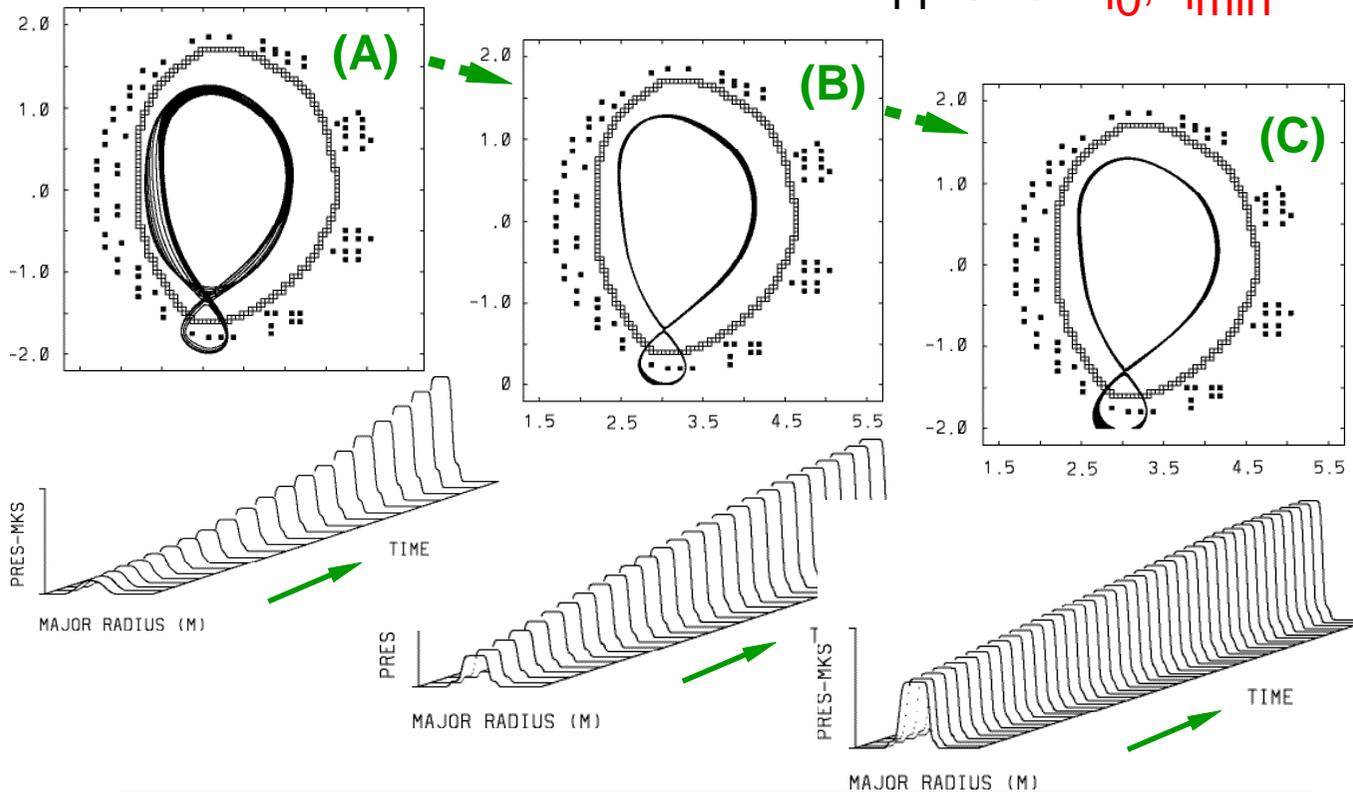
Simulation Inputs :

- Initial plasma equilibrium
- PF coil currents in time
- $p(\ )$ ,  $ne(\ )$ , ITB as bellow



Simulation Outputs :

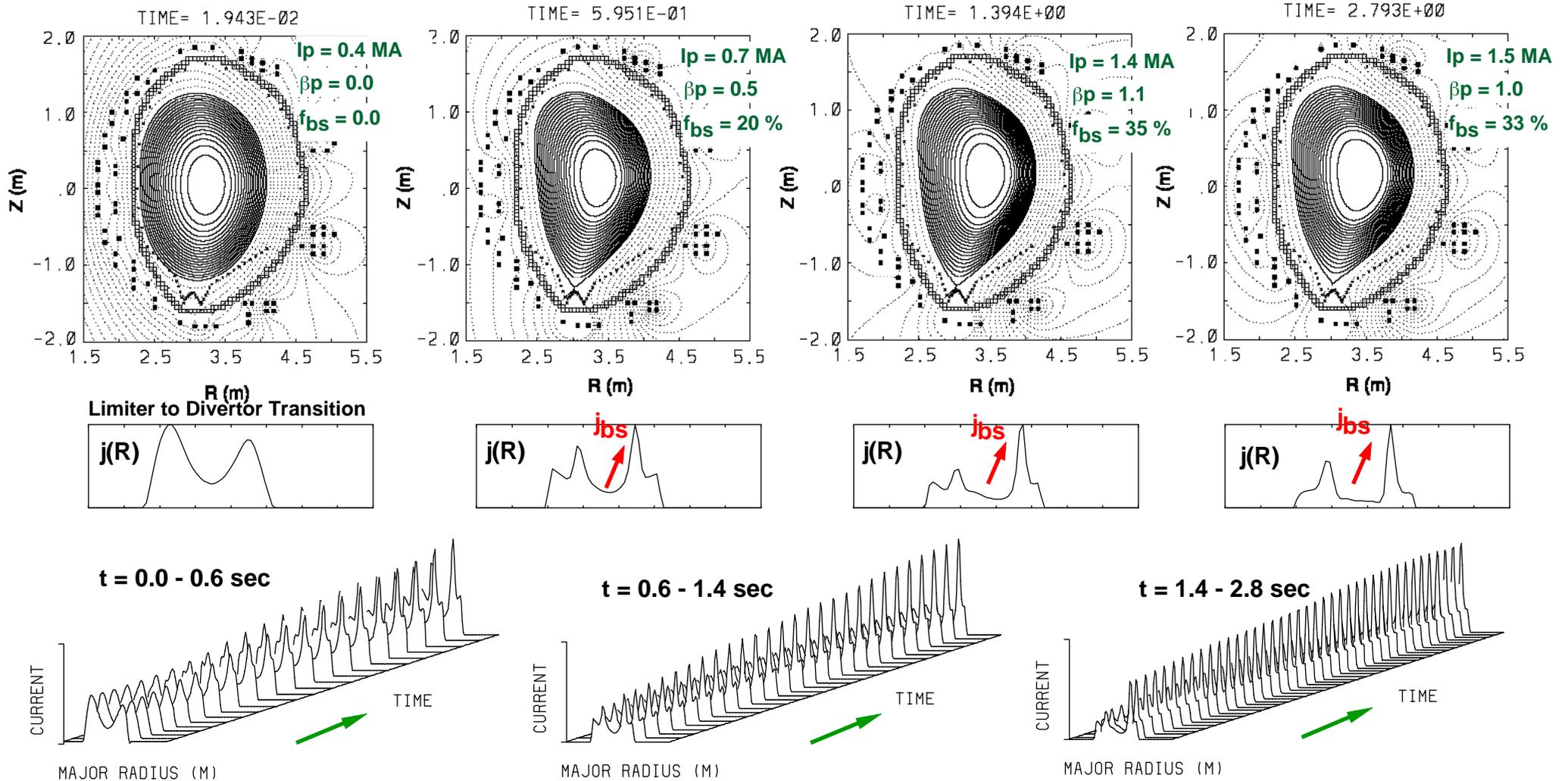
- Position :  $(R_p, Z_p)$
- Shape :  $\epsilon$ ,  $\delta$ , Vol.
- $I_p$ ,  $I_{bs}$ ,  $foot$ ,  $(q_{min})$
- $q$ -profile :  $q_0$ ,  $q_{min}$



The ITB modeling by self-adjusting  $foot$  to  $(q_{min})$  results in a remarkable recover of E36486 ramping-up.

# Time-Evolution of Equilibria & Current Profile (TSC)

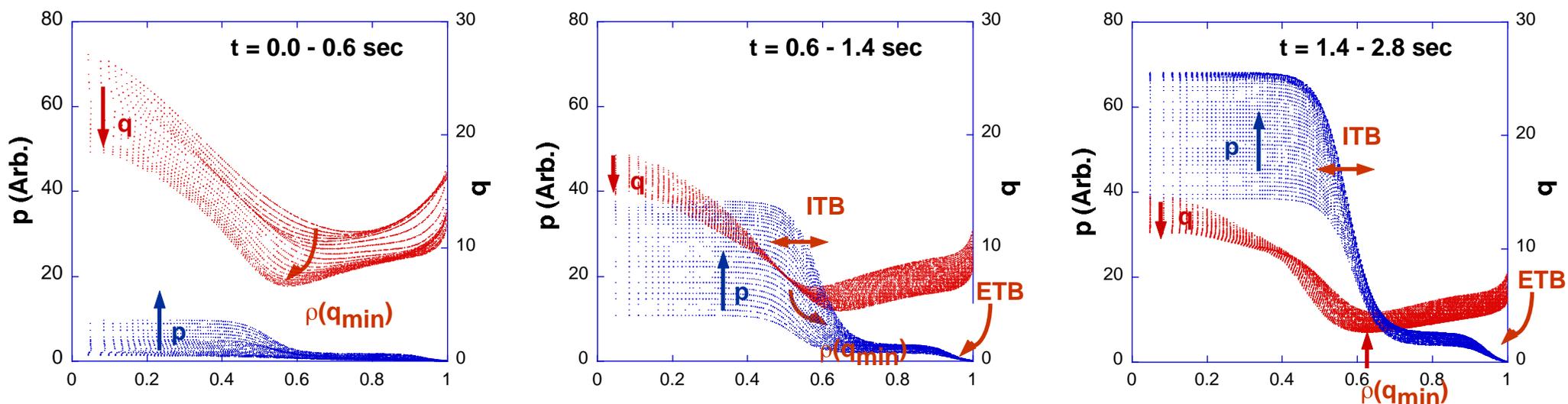
JT-60U



Almost exact plasma shape and very similar  $j$ -profile to E36486 was recovered by the ITB model of  $\rho_{\text{foot}} = \rho(q_{\text{min}})$ .

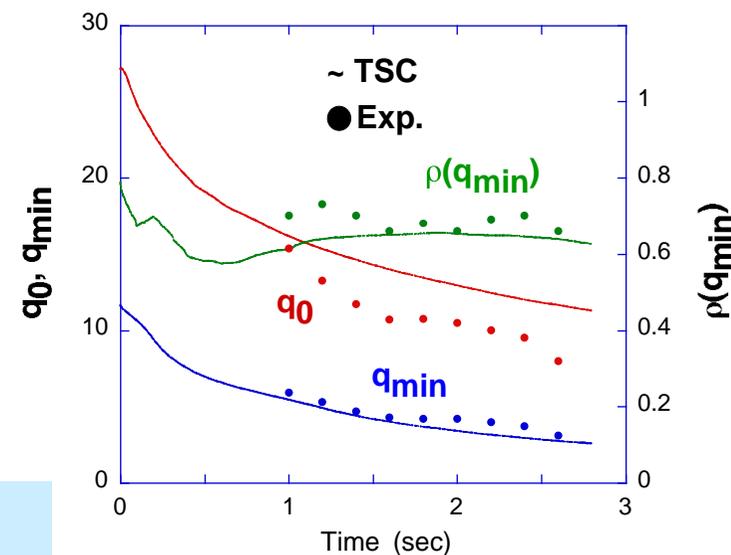
# Time-Evolution of q-Profile (TSC)

JT-60U



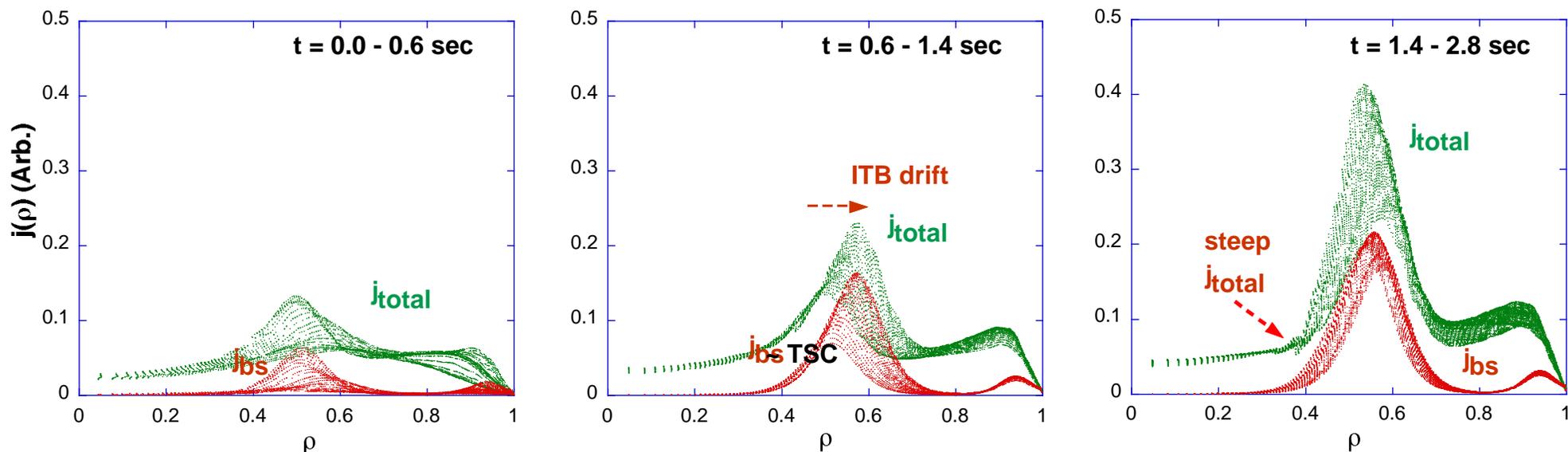
- The ITB location ( $\rho_{foot}$ ) drifts to  $\sim 0.6$  as well as the experiment of ( $q_{min}$ ).
- $q_{min}$  of TSC agrees with the experiment ( $\sim 3.0$ ).
- $q_0$  of TSC ( $\sim 11.0$ ) seems larger than the experiment ( $\sim 8.0$ ).

The ITB modeling of  $\rho_{foot} = \rho(q_{min})$  can provide similar evolution of  $q(\rho)$  to the experiment of E36486.



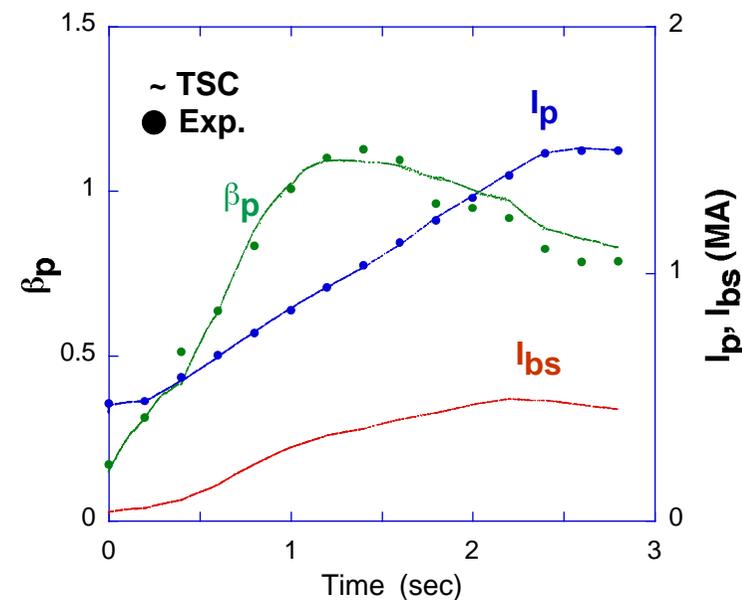
# Time-Evolution of Current Profile (TSC)

JT-60U



- $j_{total}(\rho)$  is localized at  $\rho \sim 0.6$  as experiment, because of the localization of under-drive BS current.
- BS current fraction ( $f_{bs}$ ) was 40 % at most.
- After a substantial BS current driven, a steep profile of  $j_{total}(\rho)$  just inside of ITB region is appearing.

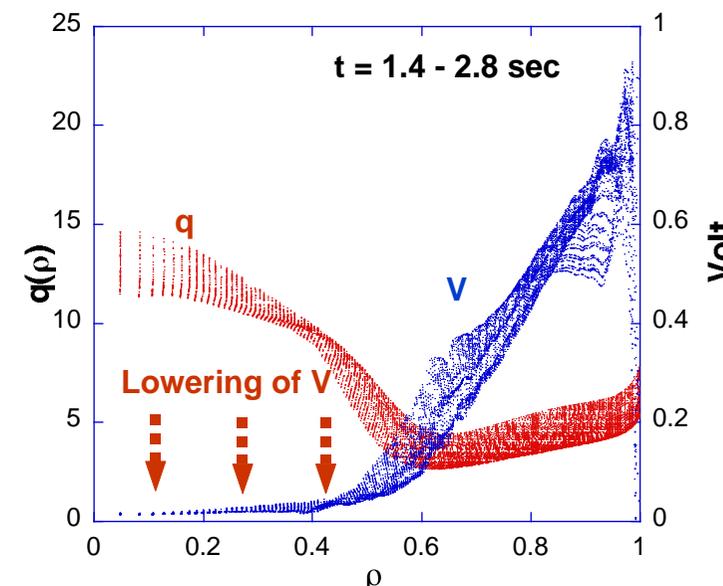
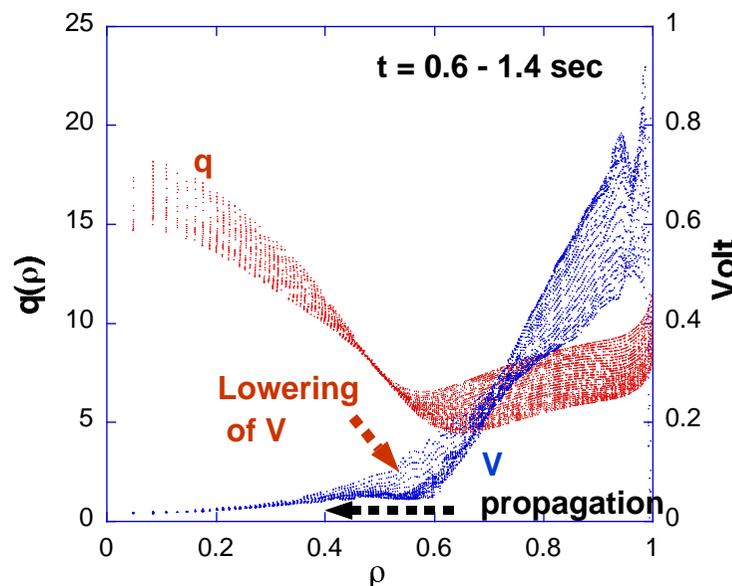
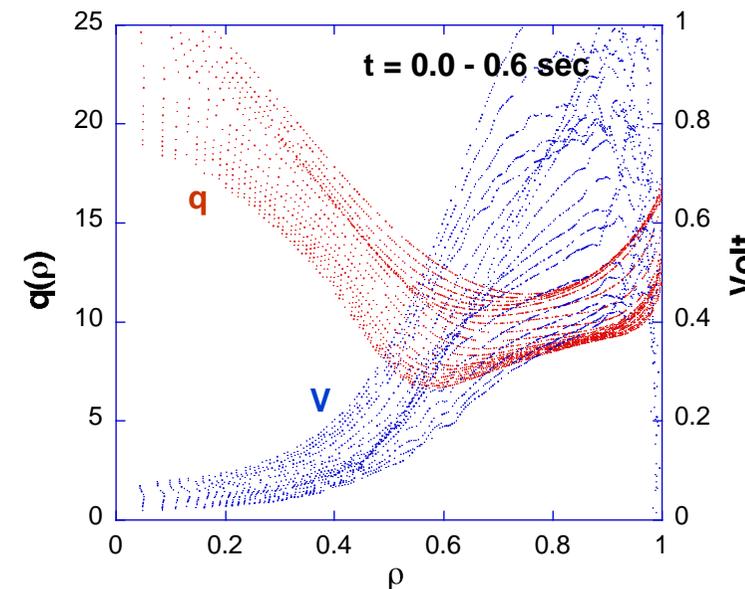
TSC building-up of plasma current was in good agreement with experiment (E36486).



# Time-Evolution of E-Profile (TSC)

JT-60U

- At initial phase of  $t = 0.0 - 0.6$  sec, electric field is decreasing as the plasma temperature arises.
- As BS current increases in accordance with ITB ( $t = 0.6 - 1.4$  sec), total current becomes to locally distribute around the ITB.
  - ➔ lowering of electric field around the ITB
- The low electric field is propagating to plasma core region, and makes a lowering of electric field there, but BS current is still an under-drive.

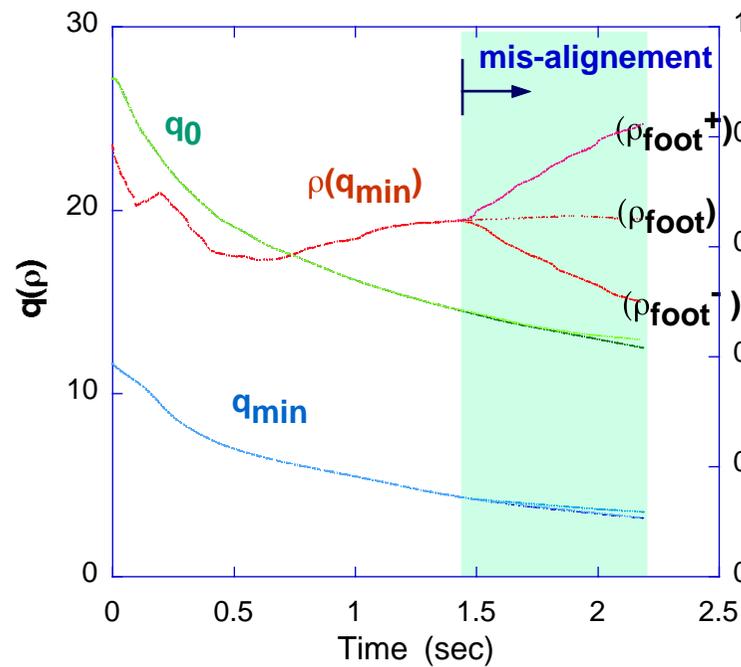
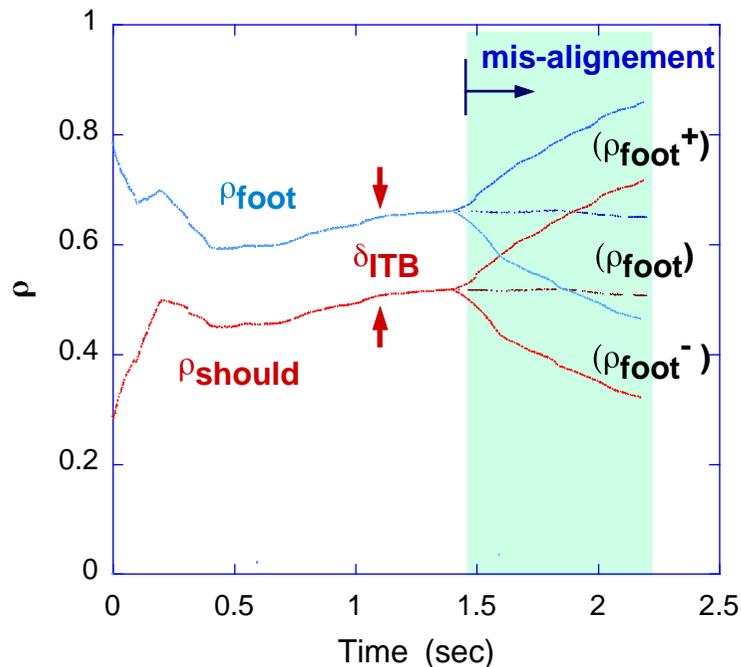


E-profile with a strong deformation evolves in accordance with the locality of BS current distribution.

# When $\rho_{\text{foot}}$ disagrees with $\rho(q_{\text{min}})$ , how the ITB is moving?

JT-60U

- Motivation induced by the interest of operational reactor scenarios & power estimation of non-inductive, external control of current profile, e.g. NNBI, LHCD, ECCD, FW etc.



mis-alignments starts at 1.4 sec.

$$\text{Outside Offset : } \rho_{\text{foot}}^+ = \rho(q_{\text{min}}) + \delta_{\text{ITB}}/4$$

$$\text{Inside Offset : } \rho_{\text{foot}}^- = \rho(q_{\text{min}}) - \delta_{\text{ITB}}/4$$

- Small mis-alignment of  $\rho_{\text{foot}}$  with  $\rho(q_{\text{min}})$  leads to outward or inward drift of ITBs.
- During the ITB drift, both  $q_0$  and  $q_{\text{min}}$  is almost unchanged.

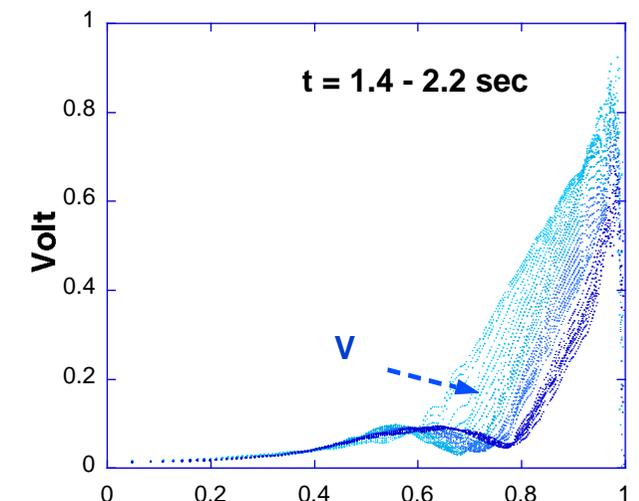
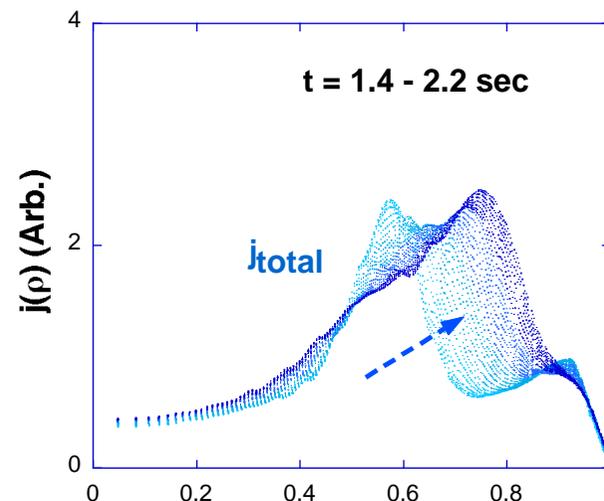
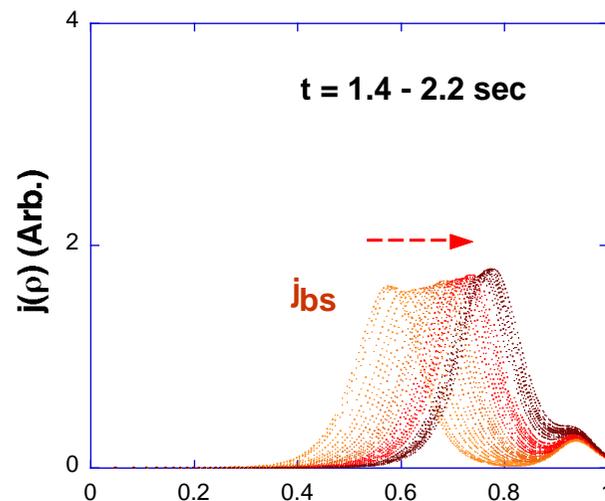
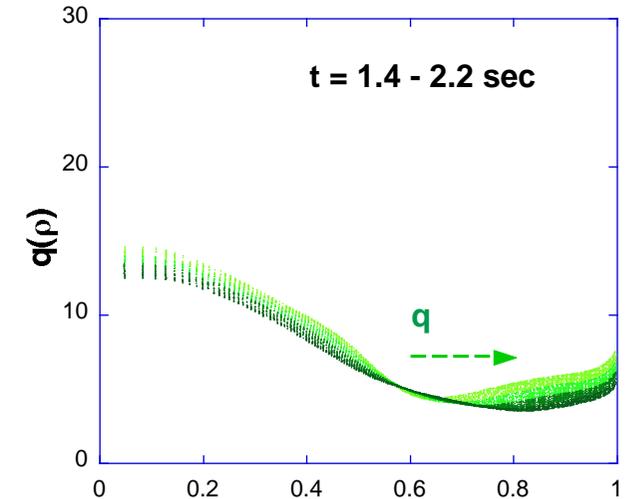
Although outward-going and inward-going property looks like symmetric, time-evolutions of current, electric field and  $q$ -profiles are quite different as Next.

# ITB-Expansion for an Outside Offset : $\text{foot} > (q_{\min})$

JT-60U

- Time-evolution of  $q$ -profile and  $j_{bs}$  is almost uniform, parallel, outward-going.
- $j_{\text{total}}$  looks outward-going as well, leaving its tracing field behind.
- The electric field profile ( $V$ ) has a weak deformation.
- Finally, expanding ITB becomes to merge with ETB.

ITB-expansion arising from mis-alignment of  $\text{foot} > (q_{\min})$  is nearly uniform, parallel, outward-going.



# ITB-Shrinkage for an Inside Offset : $foot < (q_{min})$

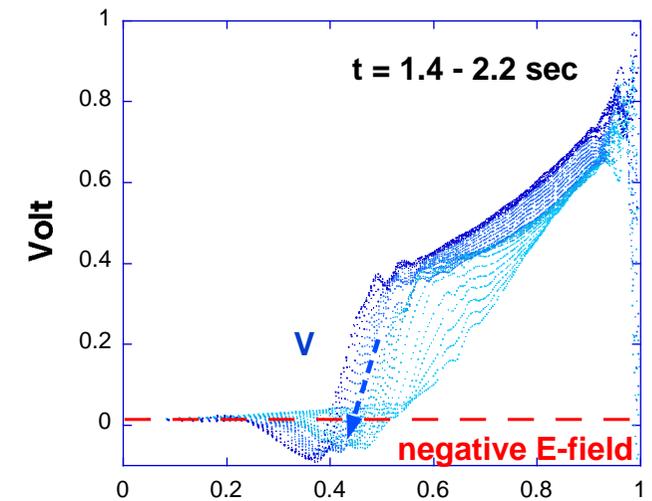
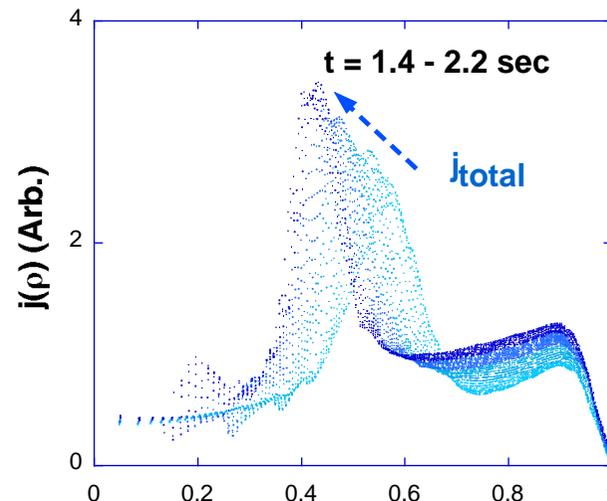
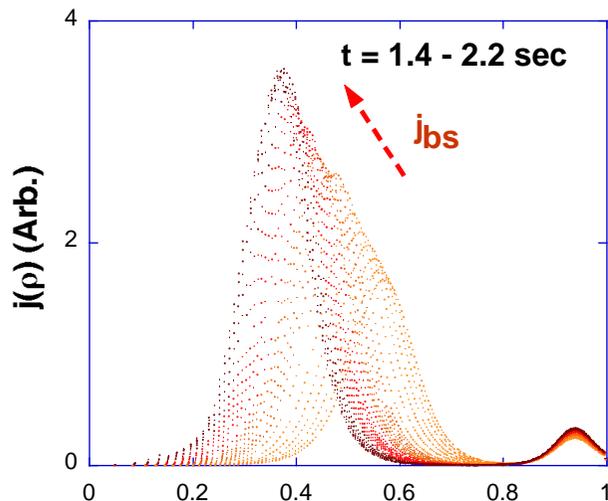
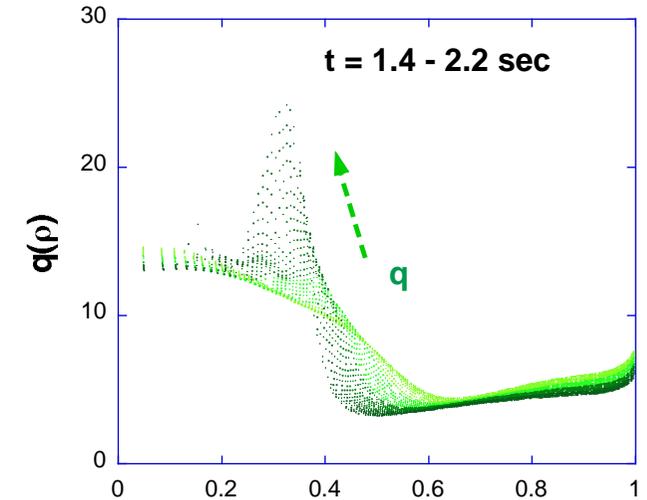
JT-60U

- A remarkable localization of  $q$ -profile and electric field appears in the inside front of shrinking ITB.
- BS current  $j_{bs}$  is not parallel moving, but substantially increases.
- In the inside front of shrinking ITB, increasing BS current  $j_{bs}$  becomes over-drive than  $j_{total}$ .

$$j_{bs} = -\frac{\sqrt{p}}{B_p} \frac{dp}{dr}$$

➔ Over-drive BS current leads to negative E-field there.

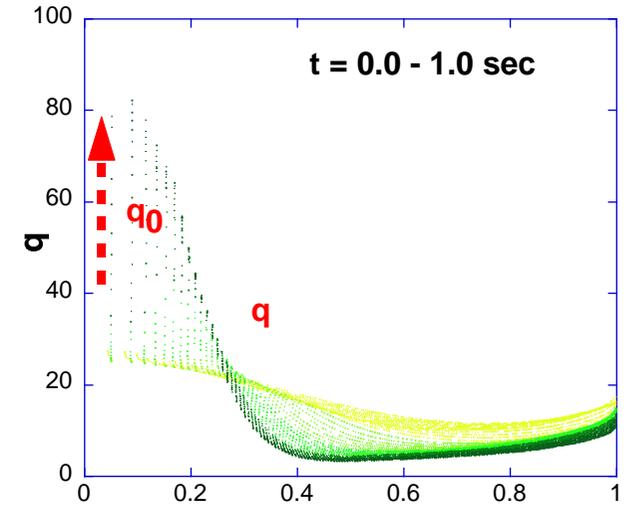
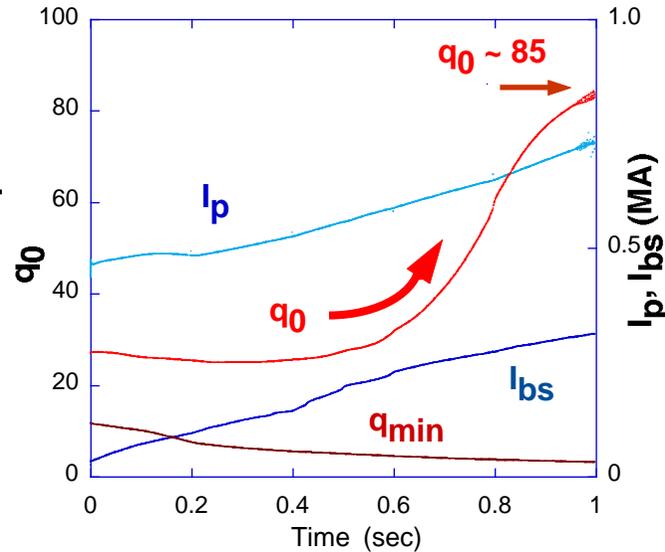
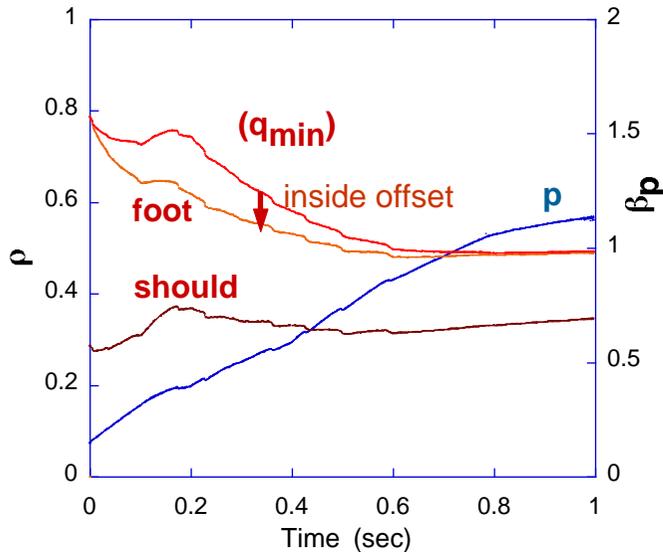
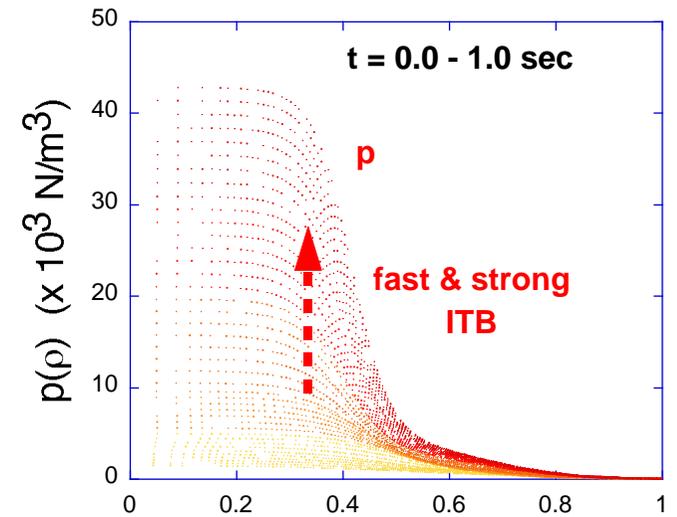
ITB build-up near plasma core region is more easy to dig out the ohmic current from the ITB region.



# TSC Simulation of Current Hole Formation

JT-60U

- By inputting an inside offset of fast & strong ITB in TSC, ITB moved to  $\rho_{\text{foot}} \sim 0.5$  at  $t = 0.6$  sec.
- $I_p$  and  $I_{bs}$  continue to ramp-up in simulation as well as E36486
- A remarkable increase of  $q_0$  appeared, then  $q_0$  went more than 80 at  $t = 1.0$  sec.



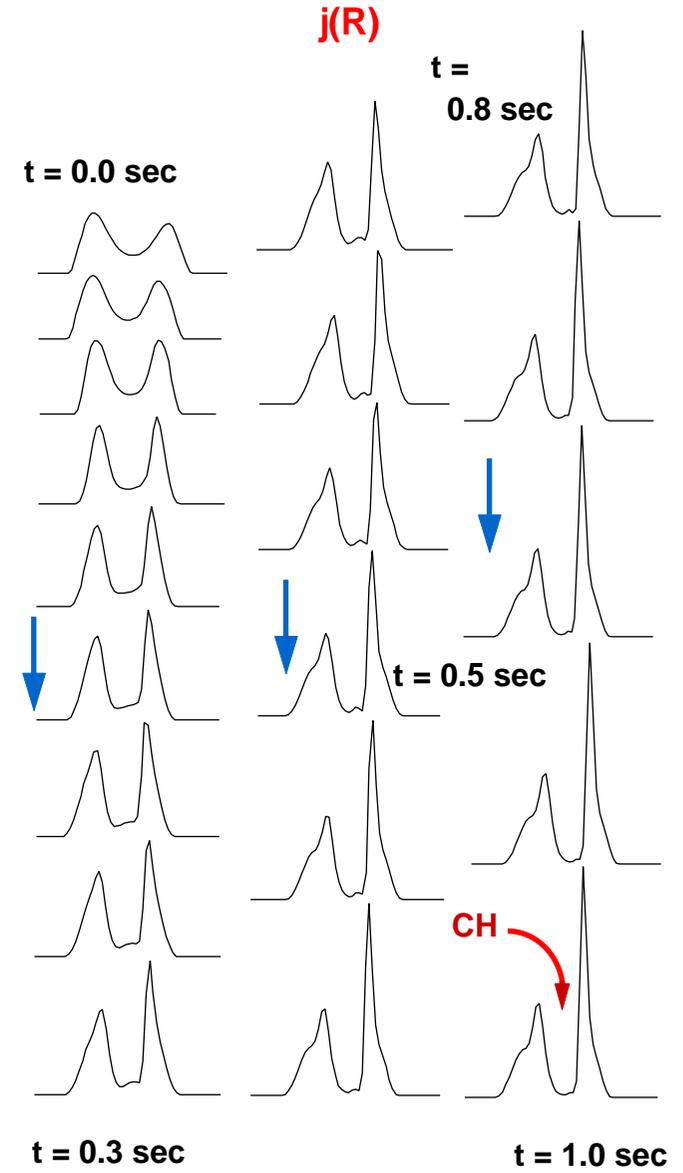
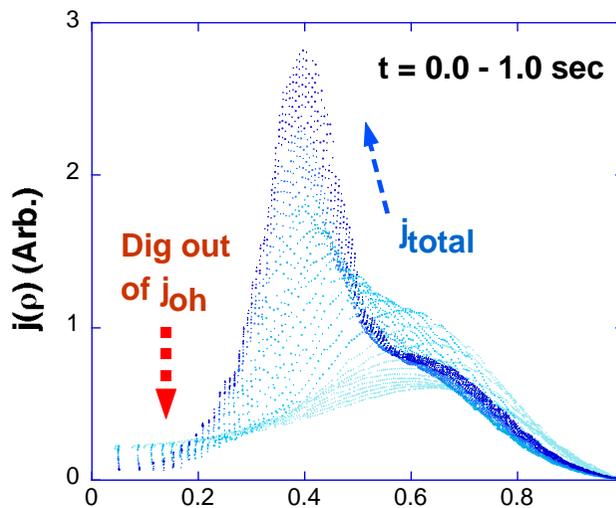
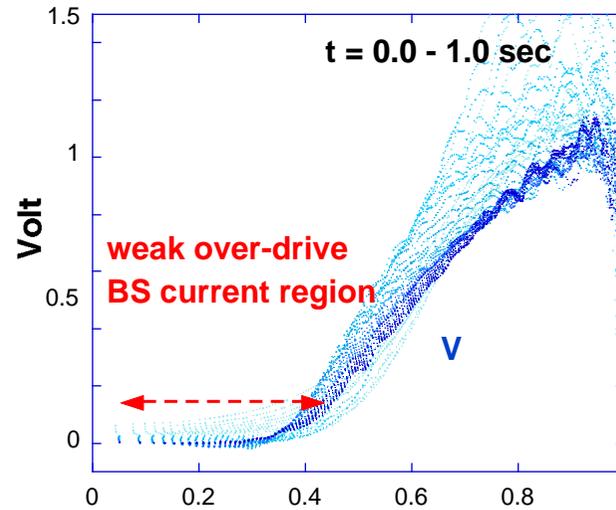
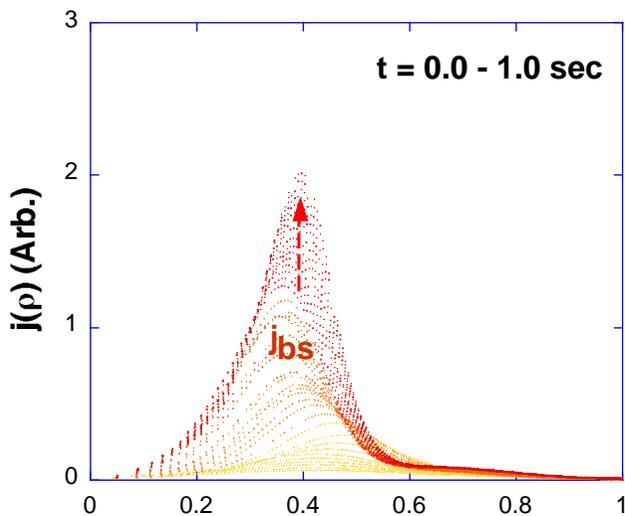
# Current Hole Formation due to Over-Drive BS Currents

JT-60U

- After  $t = 0.5$  sec, BS current becomes over-driving for wider region inside of ITB.
- In consequence, weak negative electric field digs out the ohmic current from ITB region.



Current Hole

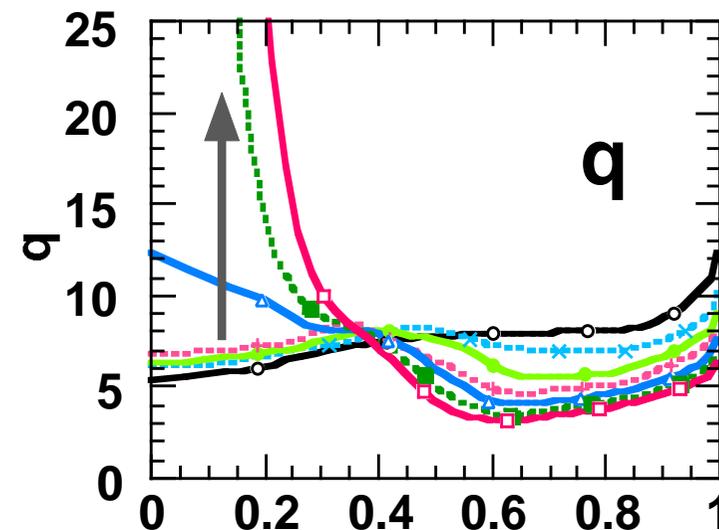
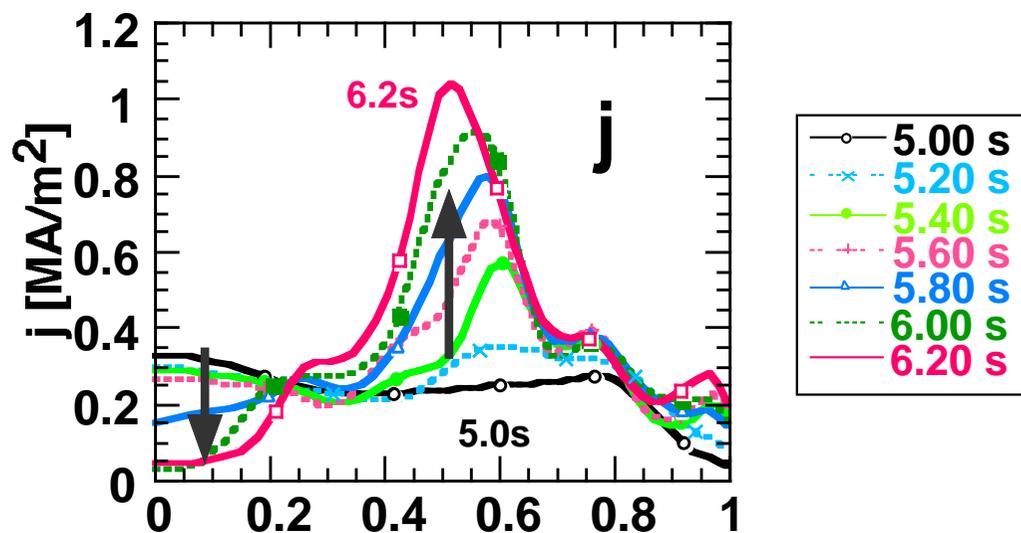
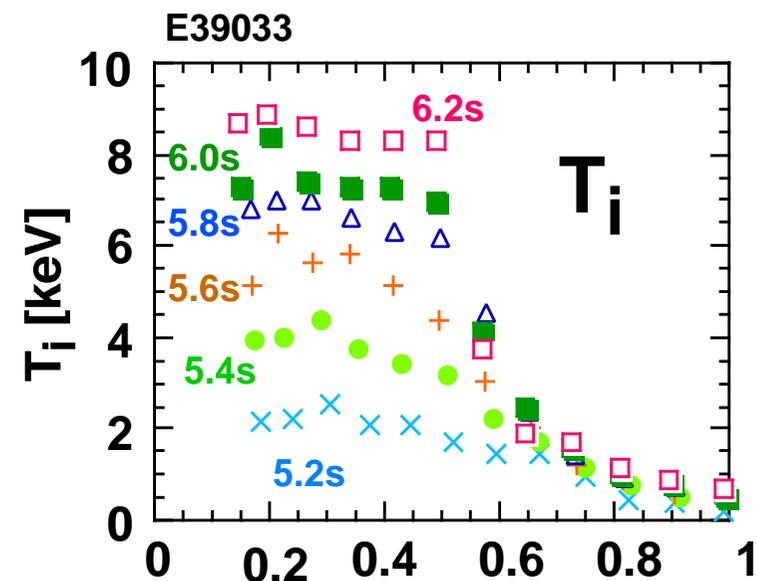


# Discovery of Current Hole in JT-60U

JT-60U

- In plasma core region, an area w/o any of Bp was discovered in JT-60U & JET (**Current Hole**).
- ITB build-up
  - ➔ Off-axis BS current increase
  - ➔  $j(0)$  decrease &  $q(0)$  rise
- Formation of Current Hole as single fluid TSC

Stable Current Hole remained alive for several sec.



# Summary

JT-60U

- A simple ITB & ETB model was installed in time-evolution MHD code (TSC).
  - Current ramp-up with associated BS current was studied for a tokamak operational purpose.
  - A specific ramp-up of JT-60U RS discharge was reproduced by the TSC, when the ITB-foot adjusts to the magnetic shear reversal.
  - A fast and strong ITB build-up near plasma core was pointed out to cause an over-drive bootstrap current inside the ITB region.
- ➔ The TSC has demonstrated an example process of Current Hole formation.

Following issues are listed for Future Study

- Ramp-up optimization without Center Solenoid for reactor
- ITB model improvement using transport model instead of prescribed pressure
- Possibility of slow ramp-up to reduce AC loss of SC coils in reactor
- External control to expand the ITB region & power estimation of the control