

# **Global Stability Issues for a Next Step Burning Plasma Experiment**

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**with input from**

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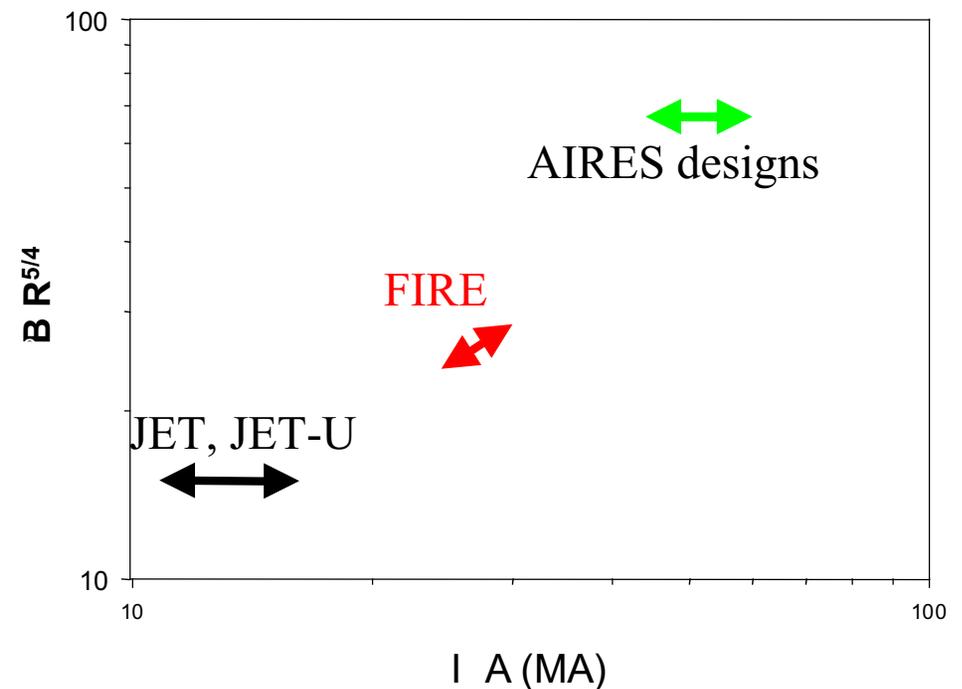
Quebec

## Abstract

We present analysis which supports the feasibility of a next-step burning plasma experiment. The FIRE design has  $R = 2$  m,  $a = .525$  m,  $\kappa_{95} = 1.77$ ,  $\delta_{95} = 0.4$ ,  $B = 10(12)$  T,  $I = 6.44(7.7)$  MA,  $H = 1.2$  (1.0) for the reference (high-field) discharge, with monotonic q-profile and sawtoothed ELMy H-mode operation. The primary issues for MHD are associated with (1) the  $q=1$  surface, (2) energetic particle modes (3) edge currents due to the H-mode pedestal, (4) neoclassical tearing modes, and (5) error fields and locked modes. We find (1) the  $m=1, n=1$  mode requires non-linear analysis including energetic-particle effects, (2)  $\alpha$ -particle driven Alfvén modes, RTAE and KTAE, are expected to be stable for  $\beta_\alpha < 0.5\%$ , (3) the predicted critical value for the onset of the NTM is very close to the operating point for the high-field option, and may be mediated by self or active control of seed island width or active island current drive, (4) the nominal self-consistent operating point is stable to external kink modes without a conducting wall and (5) error field requirements need to be revisited. Advanced operating modes with  $q > 2$  everywhere and high-bootstrap fraction also hold promise but need to be further developed.

# Fire is a logical next step between JET/JET-U and a fusion power plant

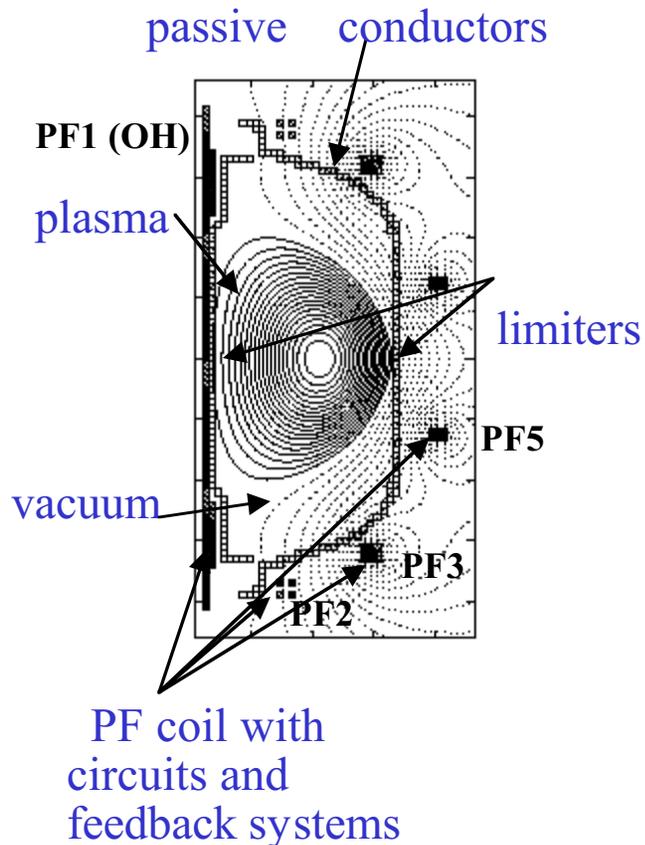
- A **major step** in the study of alpha-heating dominated plasmas
- Provides **critical data** for extrapolating to reactors
- Provides data point for critical **benchmarking** of advanced simulation codes and will
- **Stimulate development** of even more advanced numerical simulation
- Will provide **focus** to experimental and theory programs



## FIRE operating modes

	$I_p(\text{MA})$	$B_T$	$T(\text{s})$	$\beta_N$	$f_{BS}$
Standard operating mode (LF)	6.5	10	21	2.7	0.3
High-field (shorter pulse mode)	7.7	12	12	1.9	0.2
<hr/>					
Advanced Tokamak 1 <sup>st</sup> stability	5.6	9	30	2.9	0.5
Reversed Shear Wall stabilized	4.5	6.7	60	4.5	0.8

# Tokamak Simulation Code (TSC) is unique tool for modeling the evolution of a free-boundary axisymmetric plasma on the resistive time scales



- arbitrary transport model
- neoclassical-resistivity
- bootstrap-current,
- auxiliary-heating
- ballooning-mode transport
- circuit equations for all the poloidal field coils
- induced currents in passive conductors, halo
- feedback systems for  $I_p$ , position, and shape.
- current-drive,
- alpha-heating,
- radiation,
- pellet-injection,
- sawtooth model,

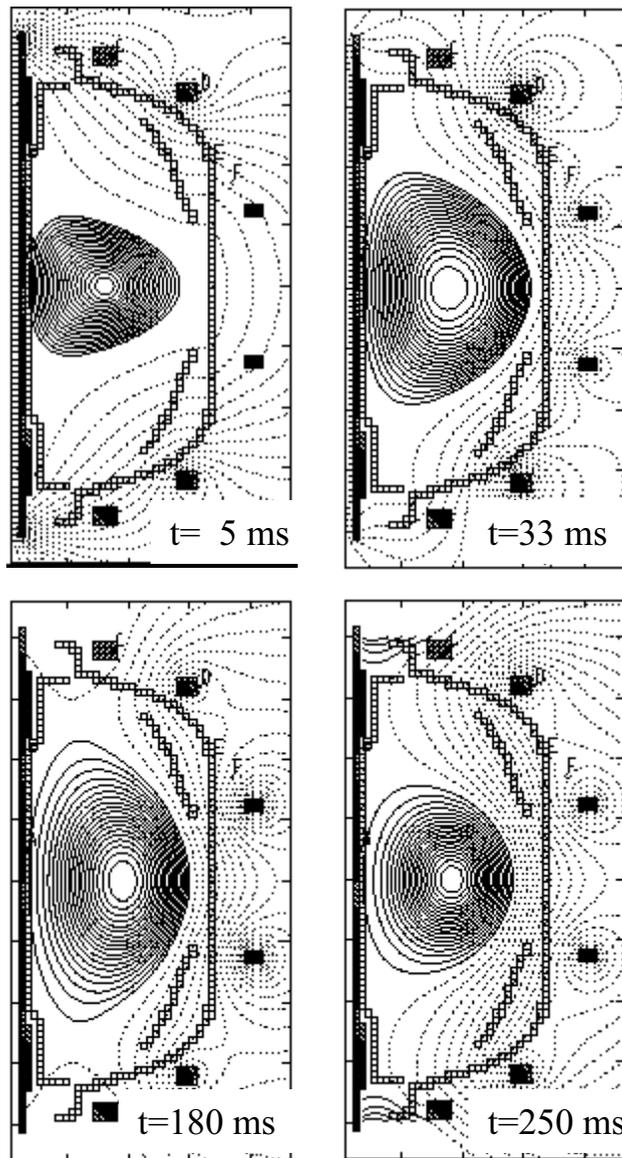
TSC was chosen by ITER as the standard model for:

- poloidal flux consumption and pulse length
- timescales for current rampup and rampdown
- shape control requirements

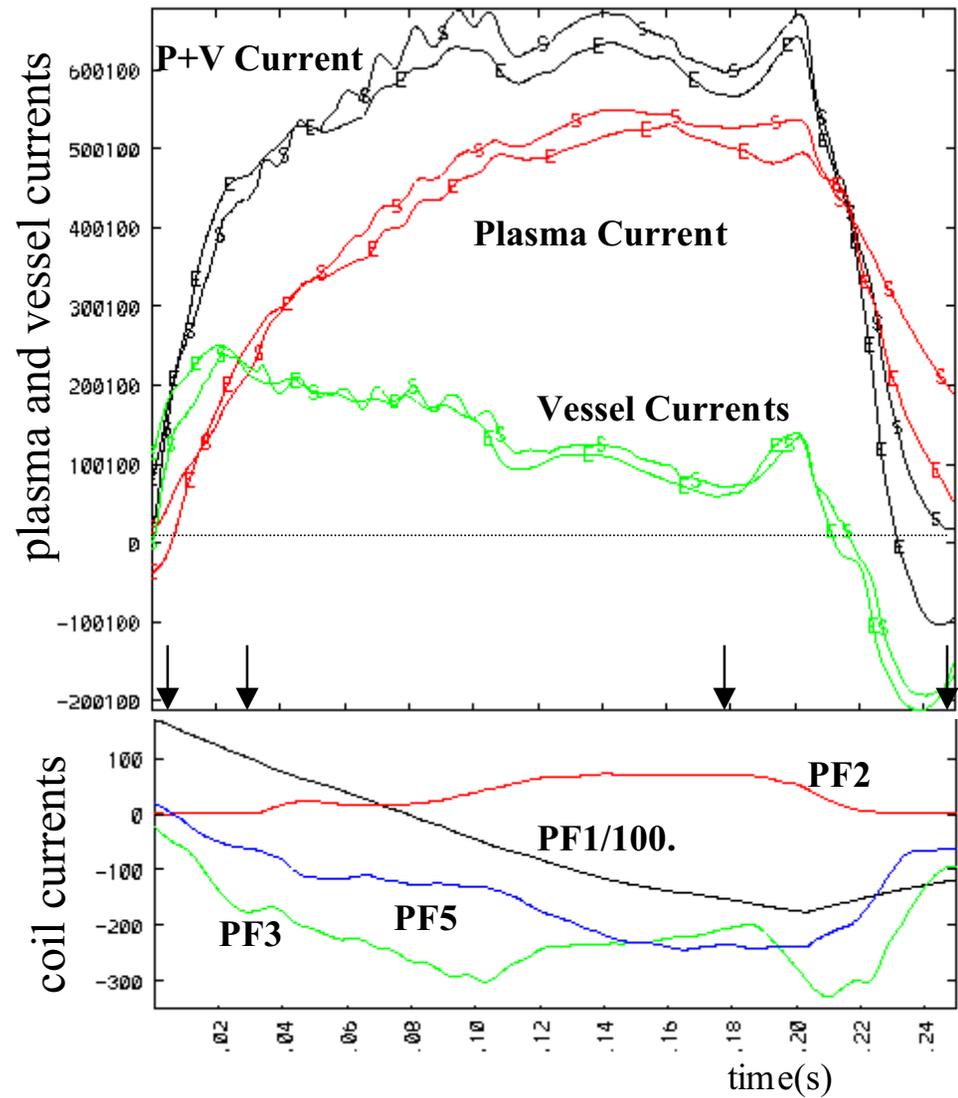
## New Directions:

- integrated modeling of core and edge
- improved models of non-linear saturation of high- $\beta$  m=1 mode, ELMs, balloon-unstable region

## TSC simulation of NSTX shot 100920

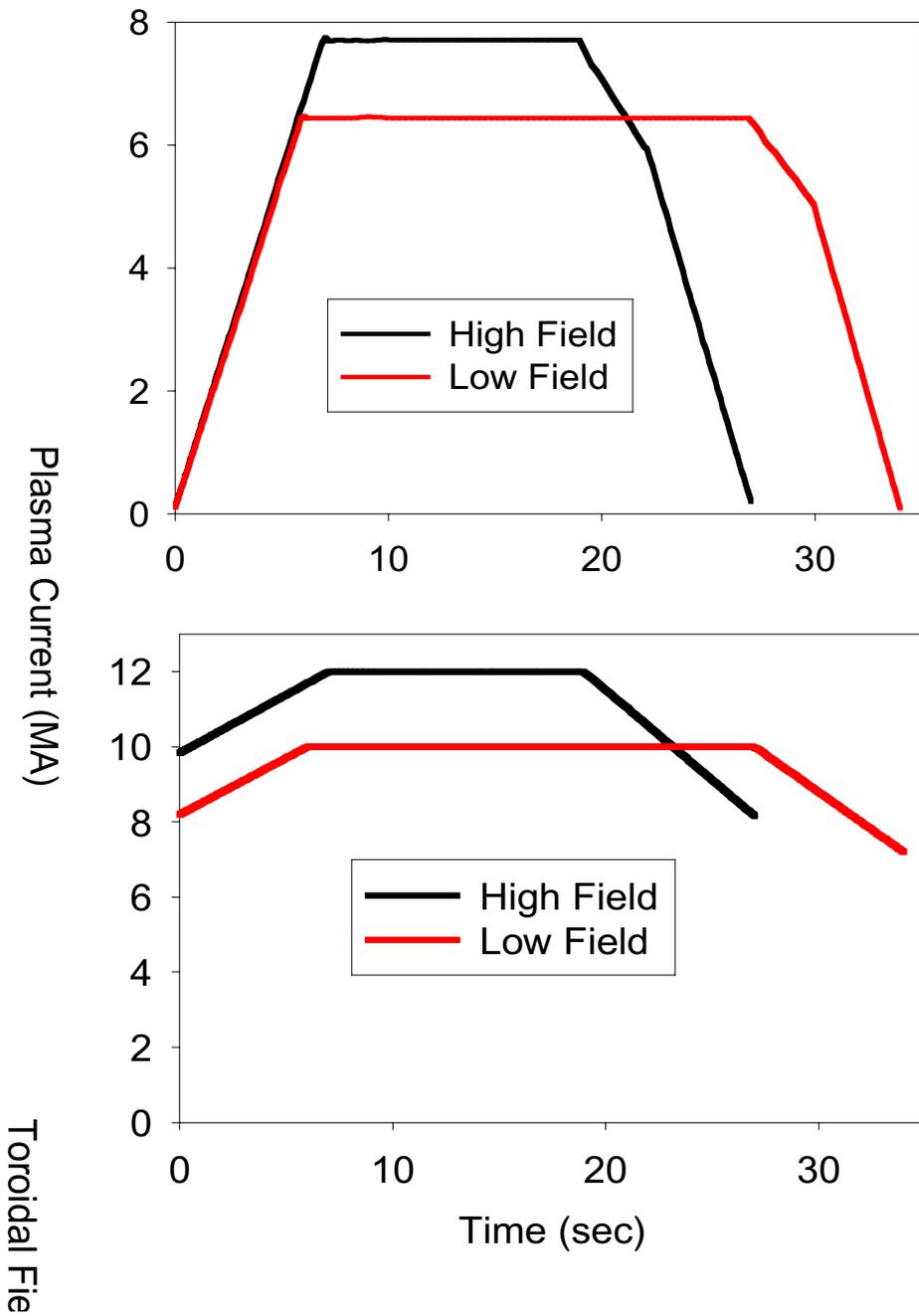


E .. experimental data S..computed by TSC



Simulation uses experimental coil currents:  
computes plasma and vessel currents

Plasma Current and Toroidal Field



# Guidelines for Predicting Plasma Performance

Confinement (Elmy H-mode) ITER98(y,2):

$$\tau_E = 0.144 I^{0.93} R^{1.39} a^{0.58} n_{20}^{0.41} B^{0.15} A_i^{0.19} \kappa^{0.78} P_{\text{heat}}^{-0.69} H(y,2)$$

Density Limit:

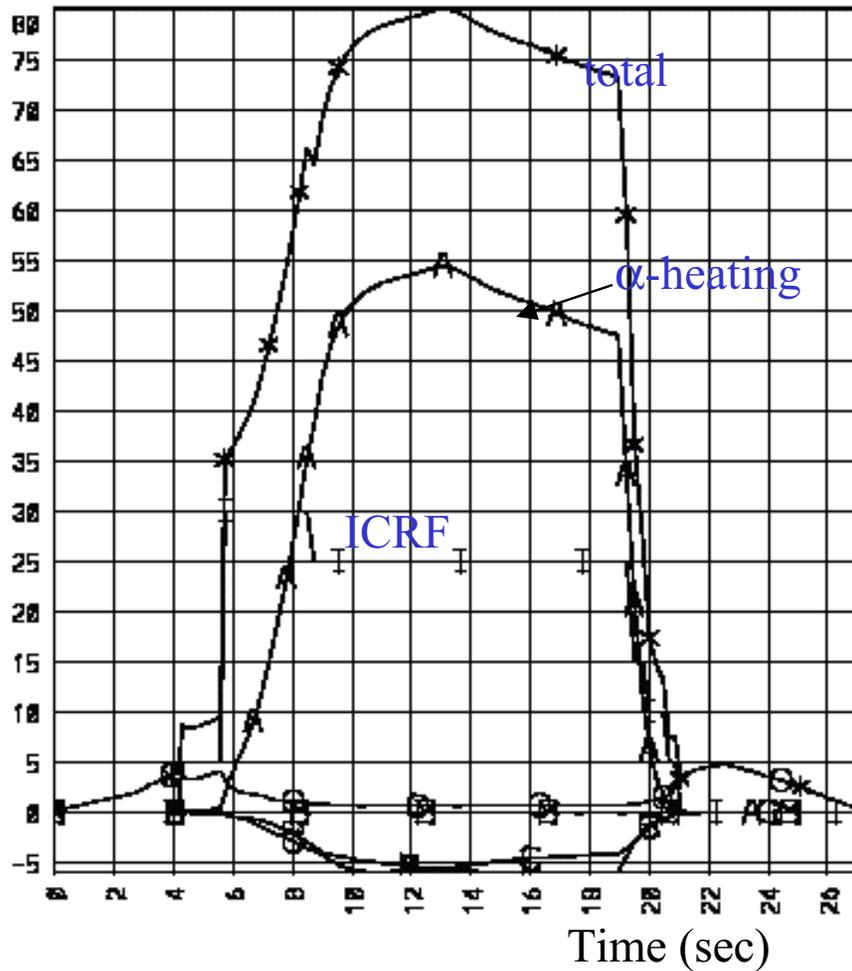
$$n_{20} < 0.75 n_{\text{GW}} = 0.75 I_p / \pi a^2$$

H-Mode Power Threshold:

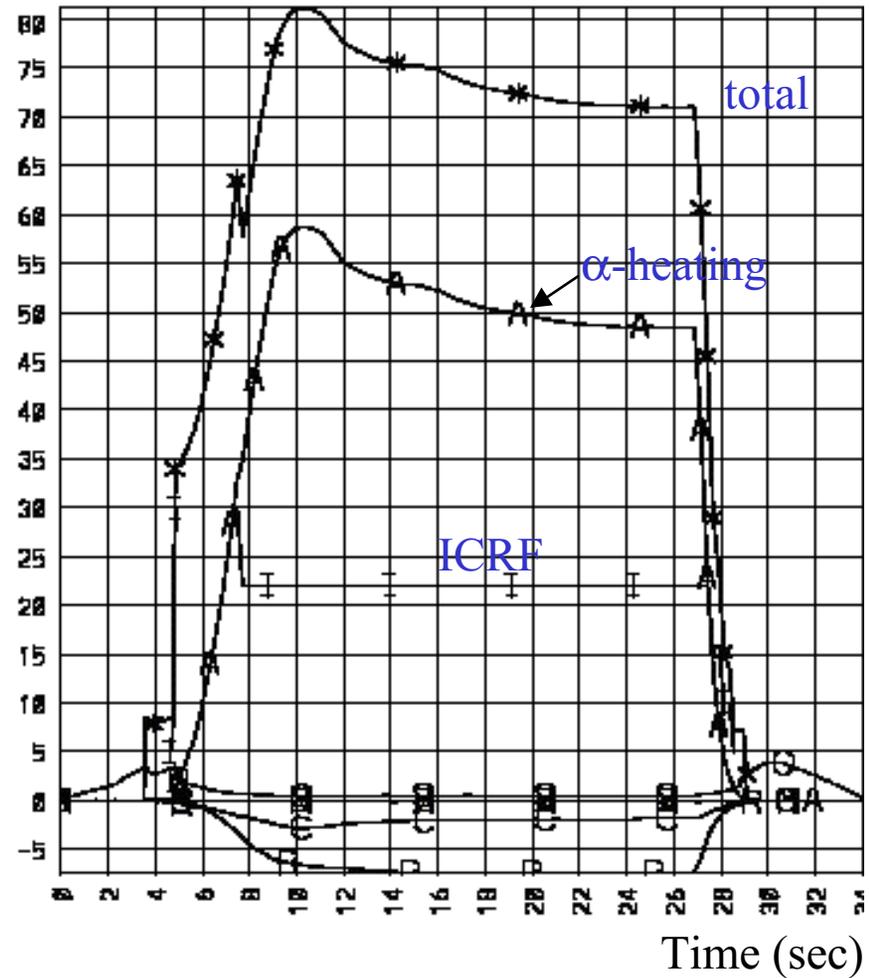
$$P_{\text{th}} > (2.84/A_i) n_{20}^{0.58} B^{0.82} R a^{0.81}$$

High Field:  $H = 1.0$  (12 T, 7.7 MA)

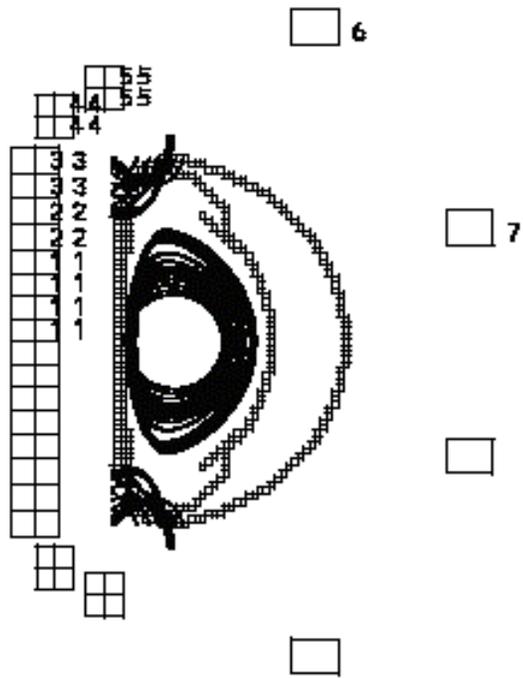
Low Field:  $H = 1.2$  (10 T, 6.5 MA)



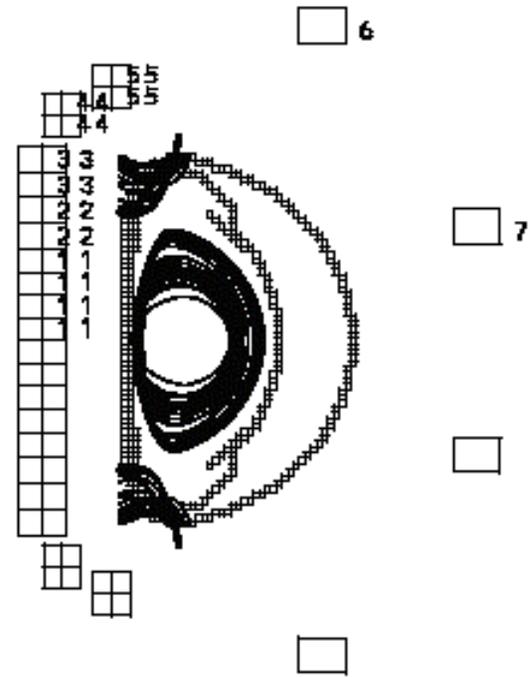
$Q > 10$  for 9 sec



$Q > 10$  for 18 sec

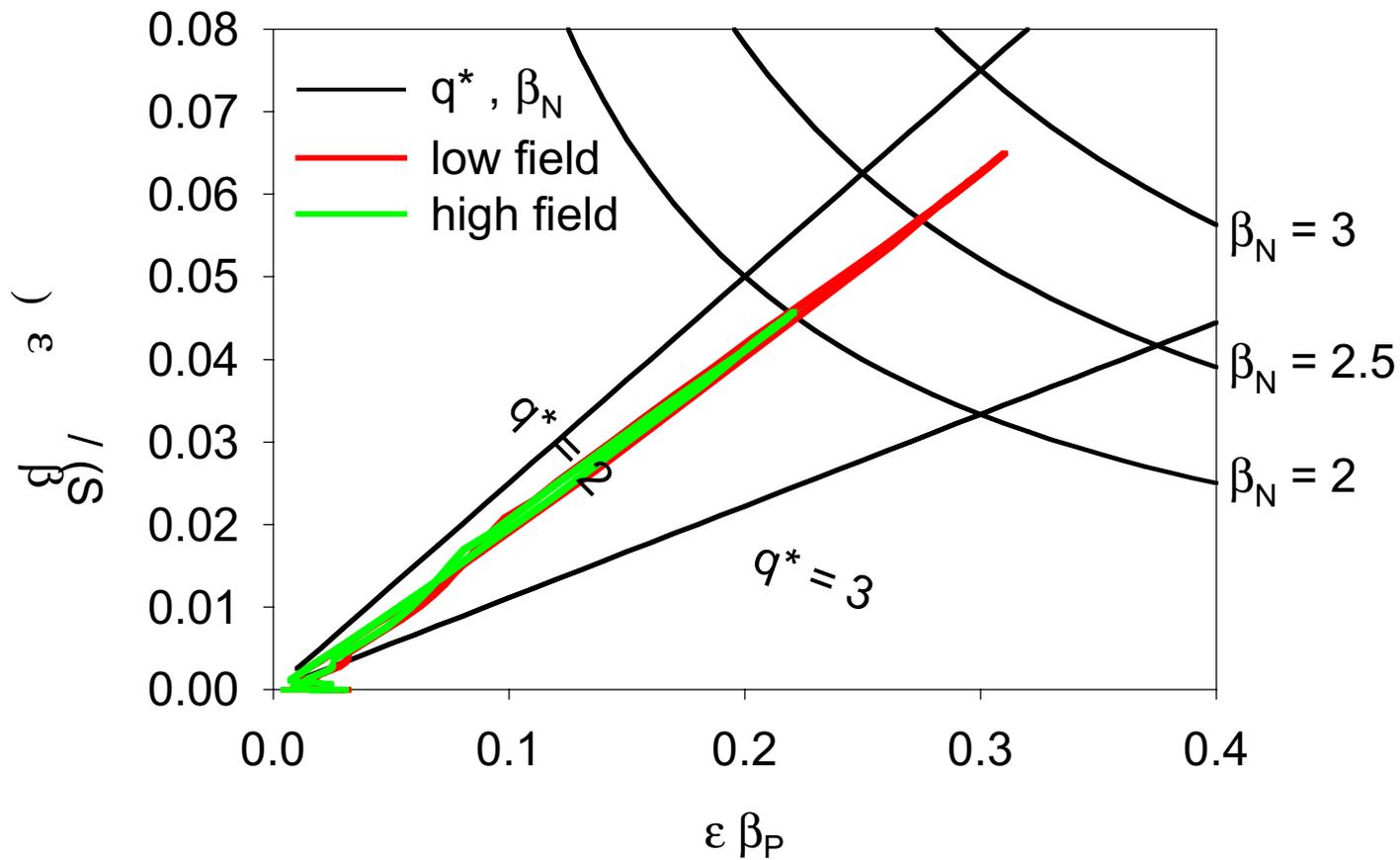


High Field



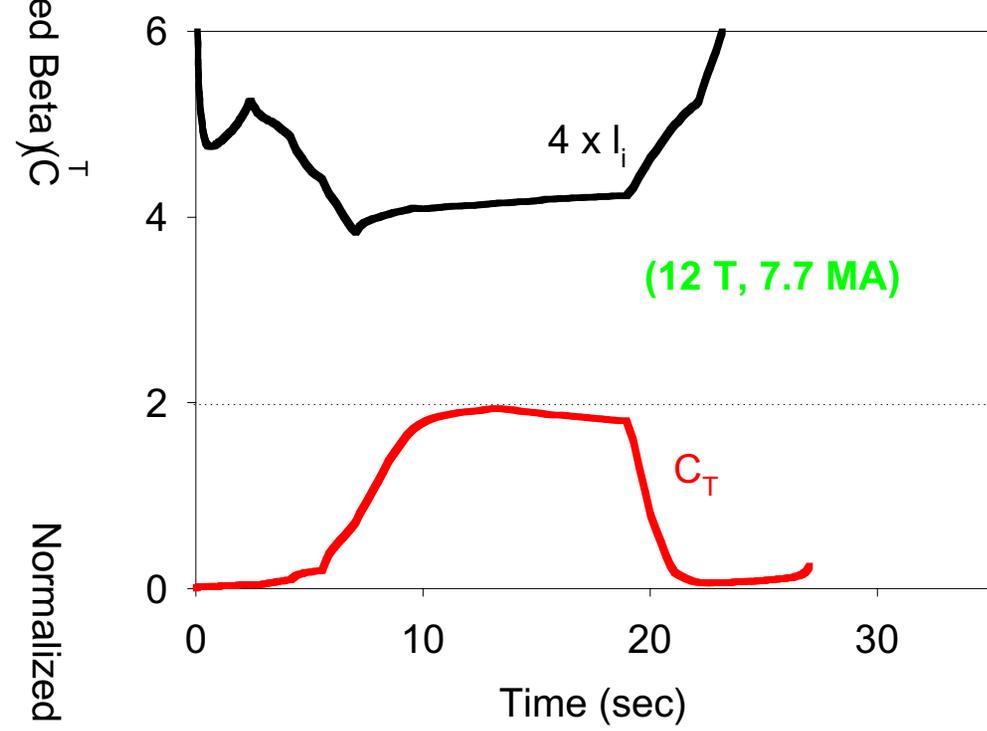
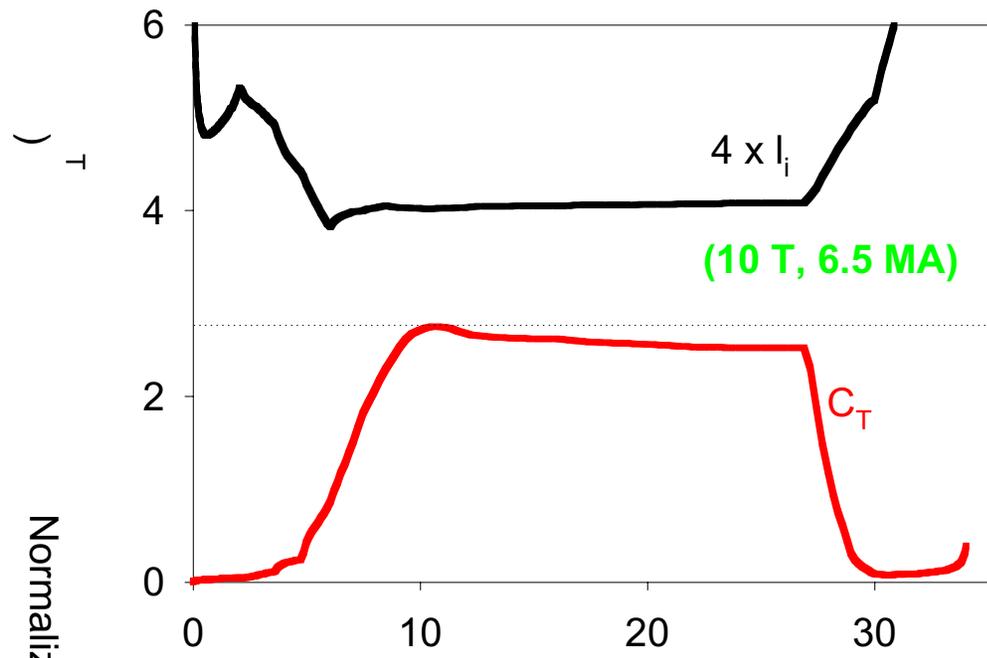
Low Field

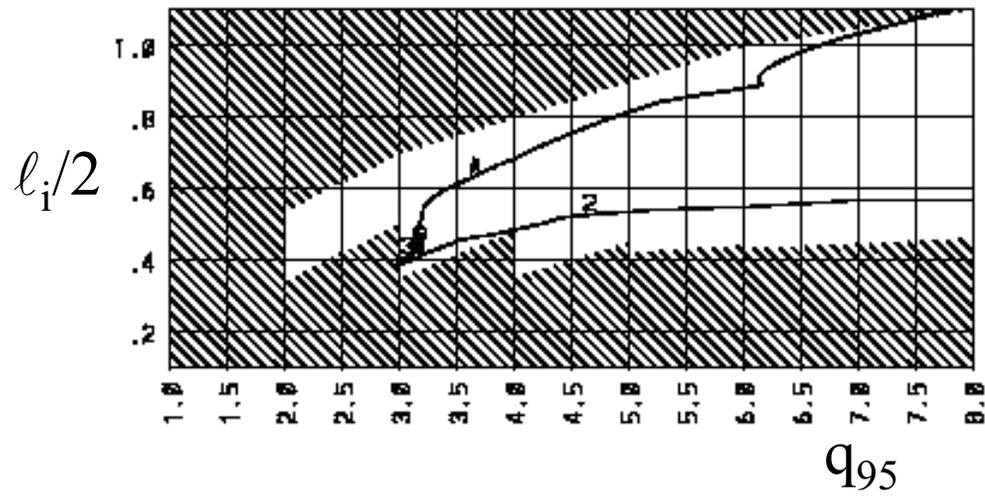
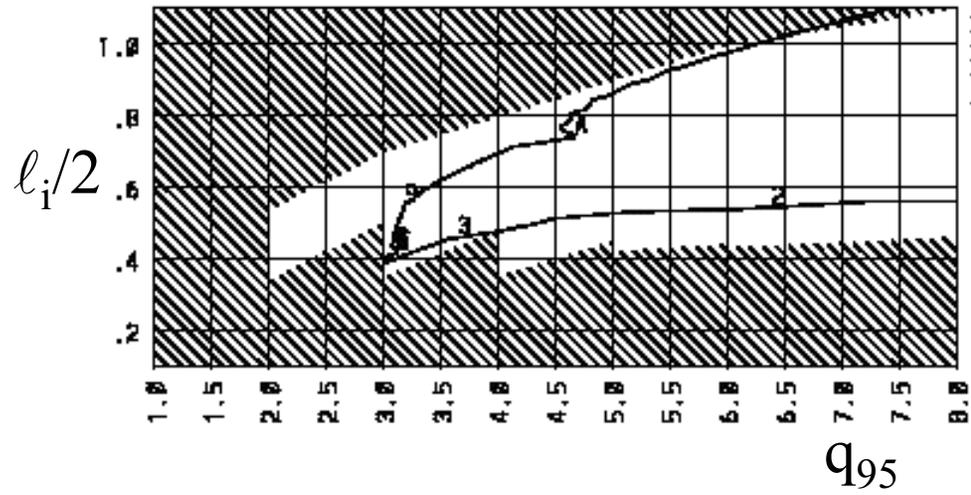
## FIRE Discharge Trajectories in Stability Space



$$S = (1 + \kappa^2) / 2$$

$$\epsilon = a/R$$



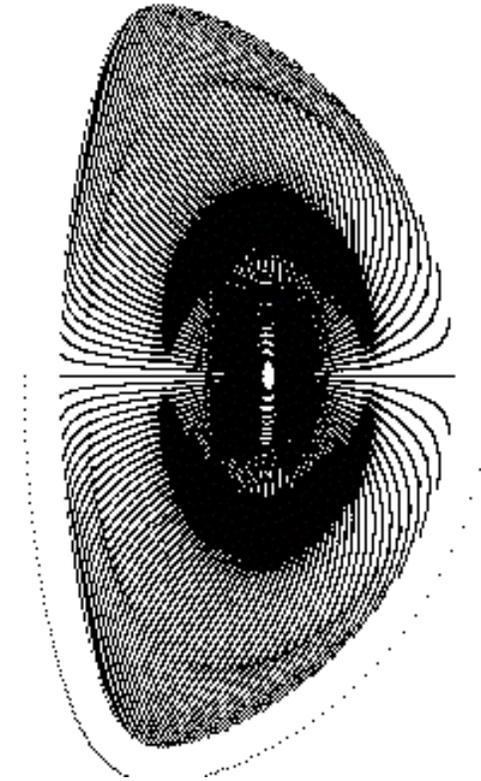
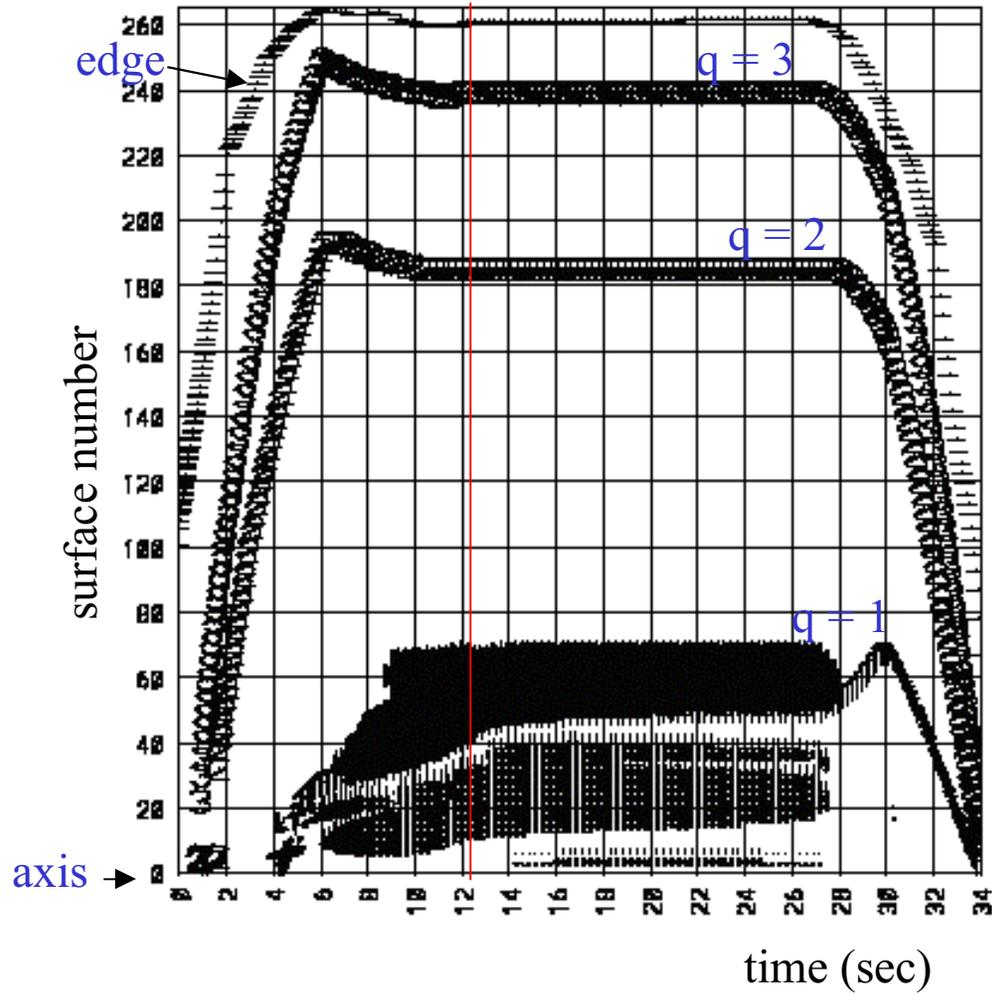


## Physics Question: Role of the $m=1$ mode

- Ideal MHD theory predicts  $m=1, n=1$  mode unstable at high  $\beta$  for  $q_0 < 1$
- High- $n$  ballooning modes also predicted to be unstable in the vicinity of and interior to the  $q=1$  surface
- Proper physics description must take into account energetic particle drive, kinetic stabilization, 2-fluid effects, and non-linear saturation mechanism
- This should be [and is] one of the major thrusts of the 3D macroscopic simulations communities
- FIRE will provide critical data point for both extrapolations and for code benchmarking

Low Field: 10 T, 6.5 MA

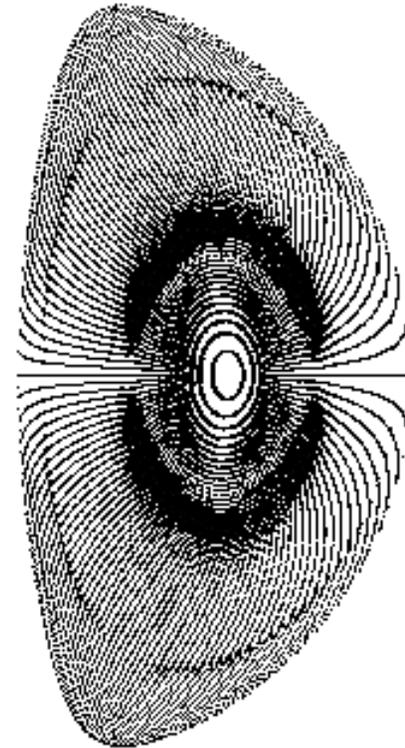
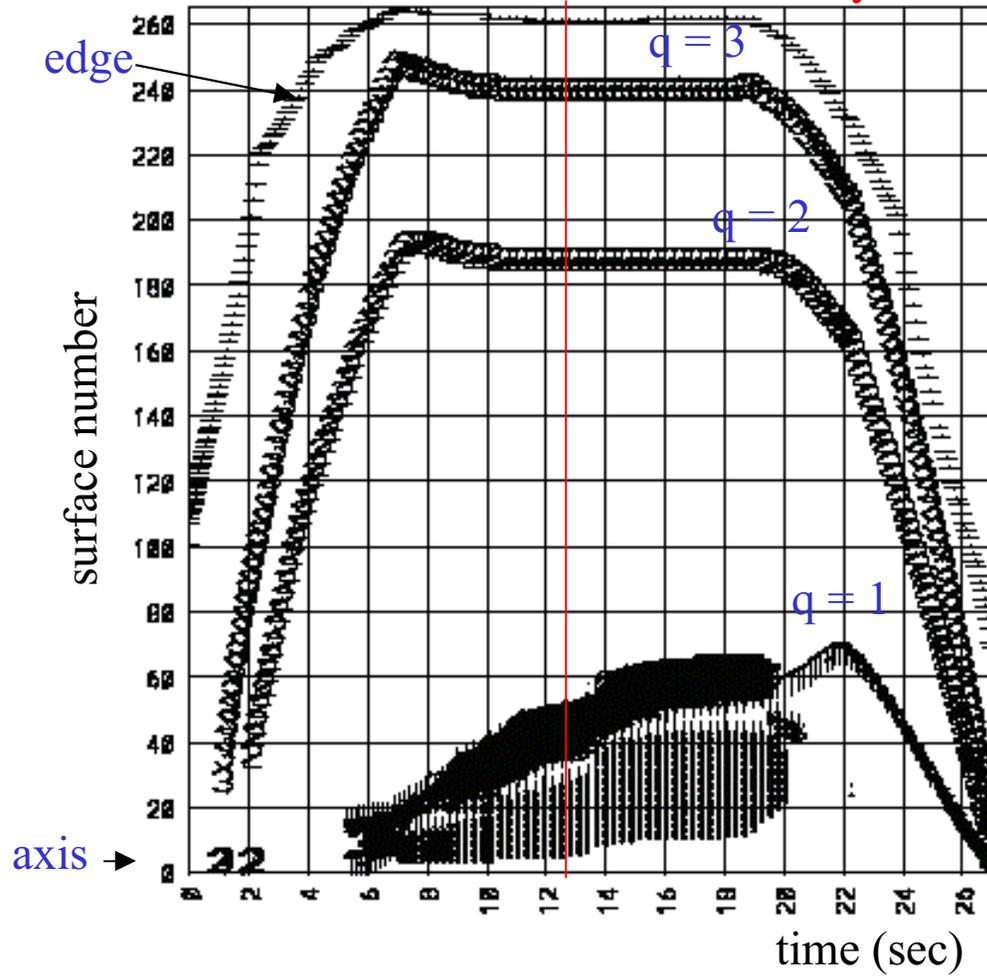
Balloon and Mercier stability



PEST unstable  
eigenfunction at  
 $t=12.5$  sec

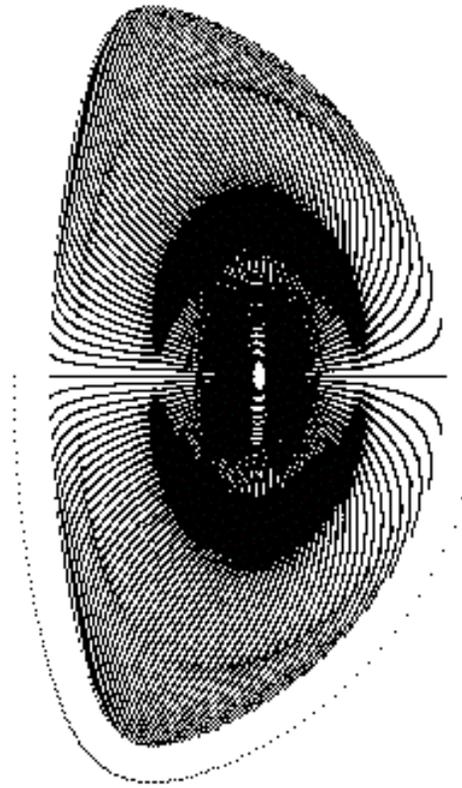
# High Field: 12 T, 7.7 MA

## Balloon and Mercier stability



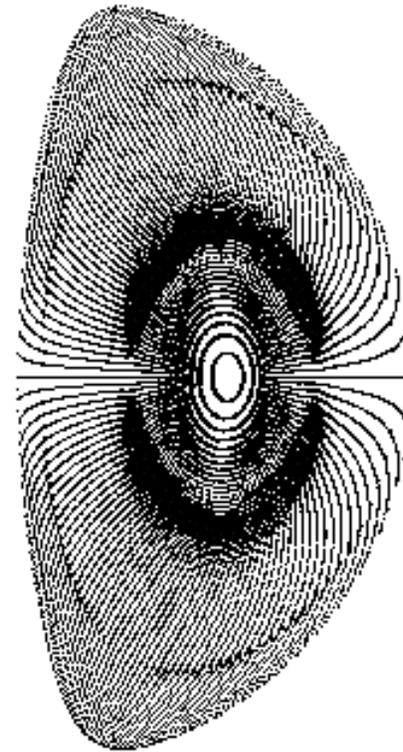
PEST unstable  
eigenfunction at  
 $t=12.5$  sec

## Comparison of unstable Eigenvalues



Low Field

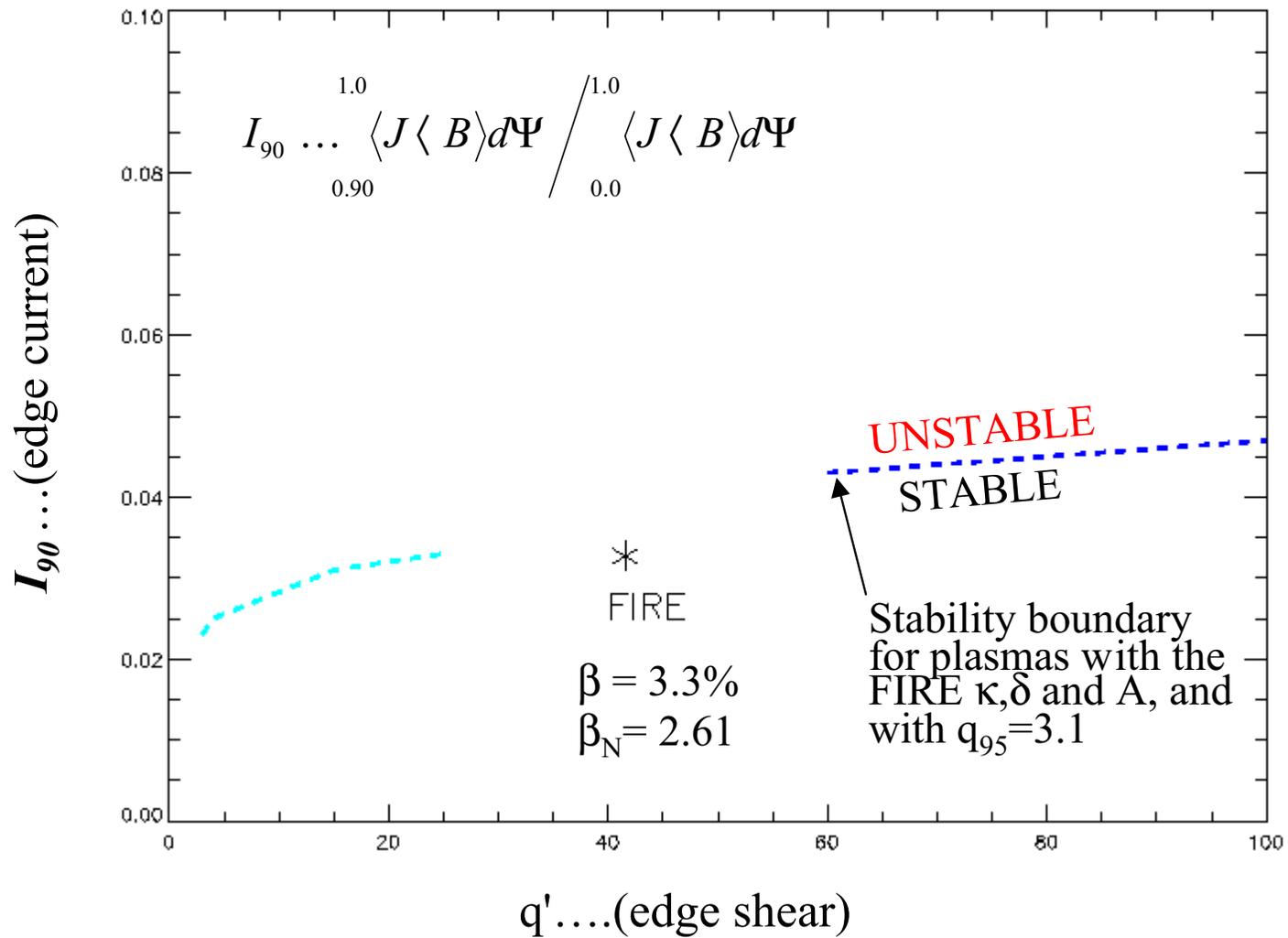
$$\gamma^2 = -.0083$$



High Field

$$\gamma^2 = -.0039$$

# FIRE nominal operating point is stable to kink modes

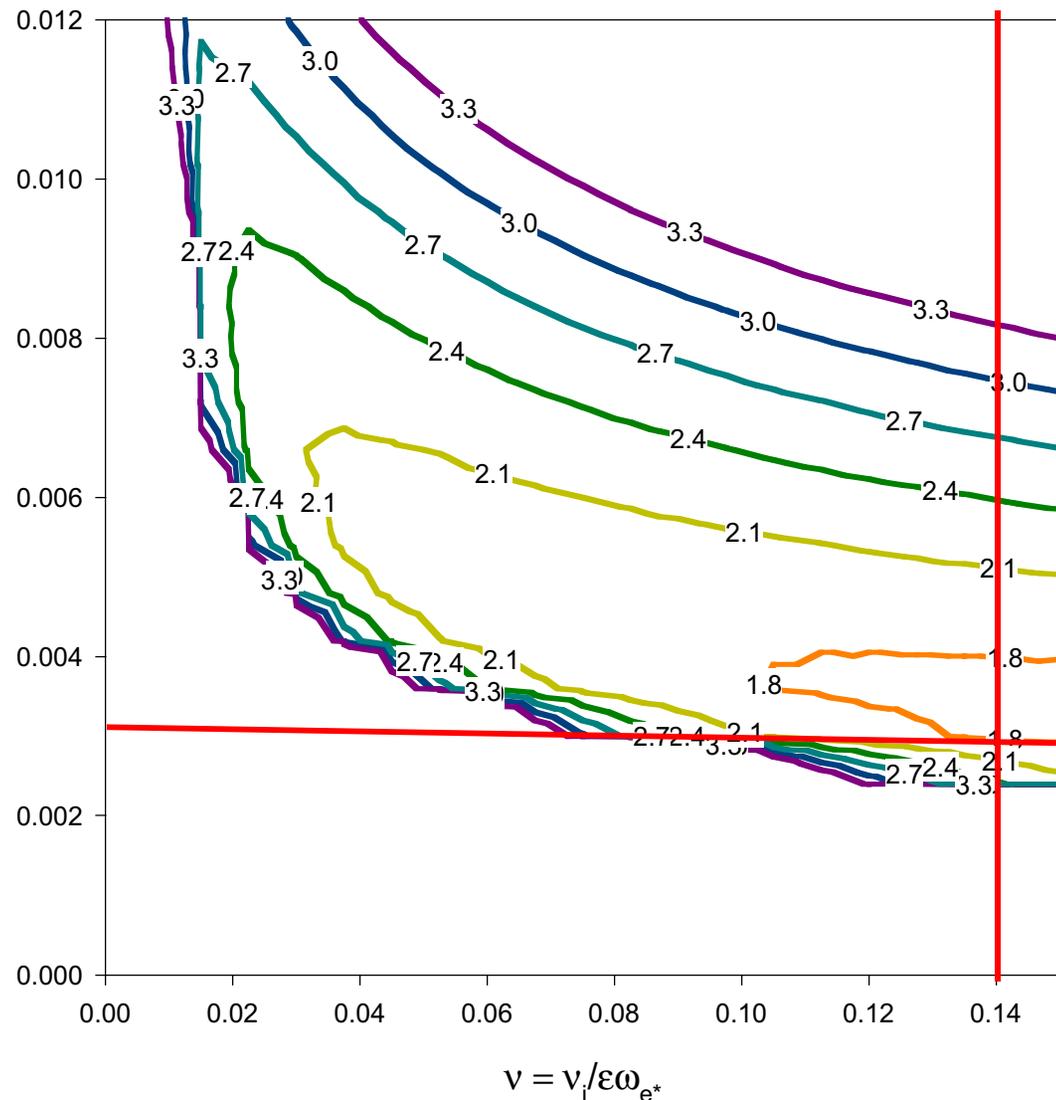


# Physics

## question: NTM

- neoclassical tearing mode sets  $\beta$  limits in many long-pulse discharges
- scaling of this to new devices largely result of empirical fitting of quasi-linear formula
- this is another major thrust of 3D macroscopic modeling effort
- FIRE will provide critical data point

Critical  $\beta_N$  fit for  $q=1$  sawtoothed induced  $m/n=3/2$  NTM



(From LaHaye, Butter, Guenter, Huysmans, Marashek, and Wilson)

# Kinetic MHD is becoming much more capable

TFTR Equilibrium

$R=2.62$  m,  $a=0.95$  m,

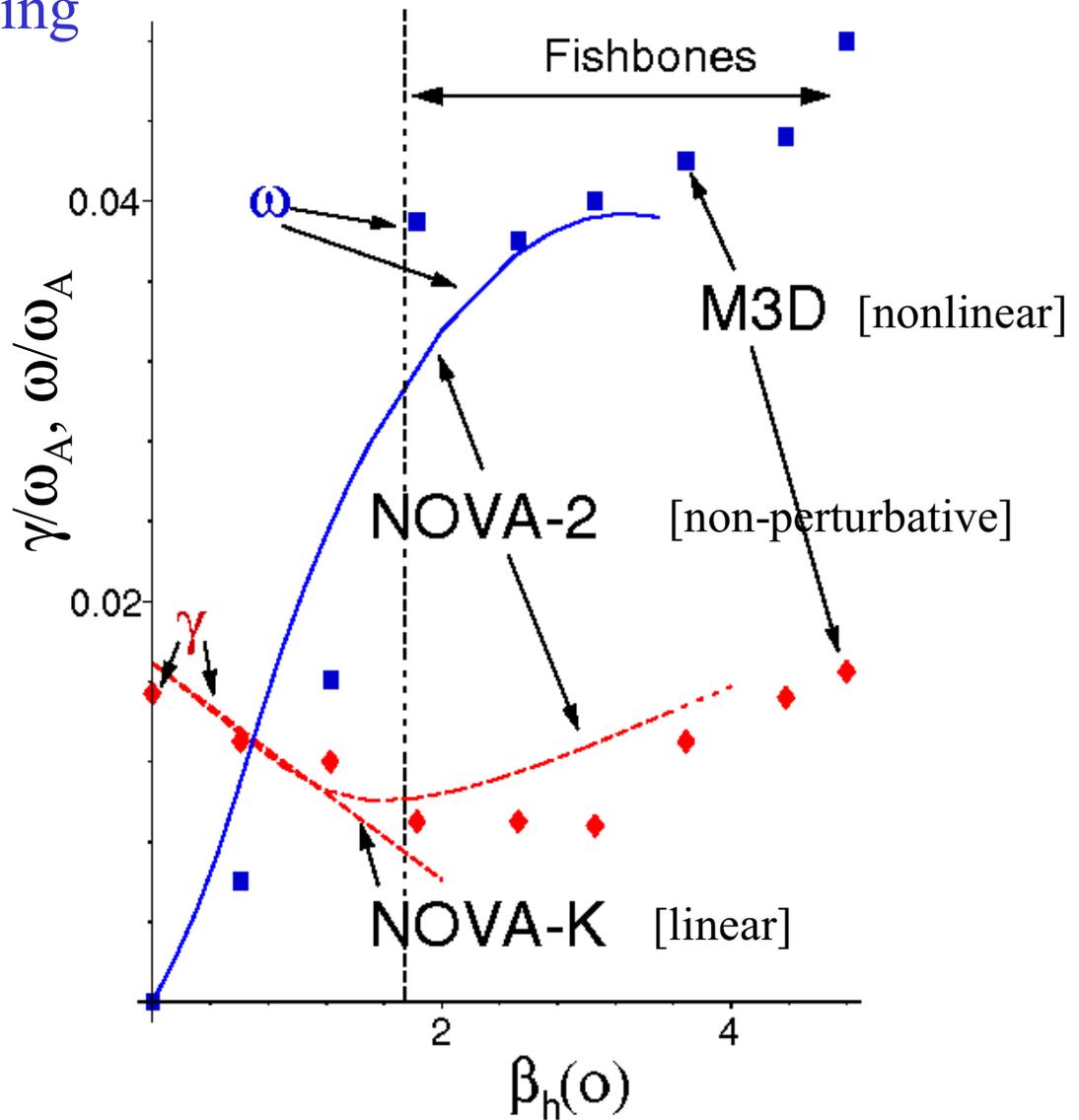
$\beta_{pl}(0) = 5\%$ ,  $\beta_{pl} + \beta_h = \text{const}$ ,

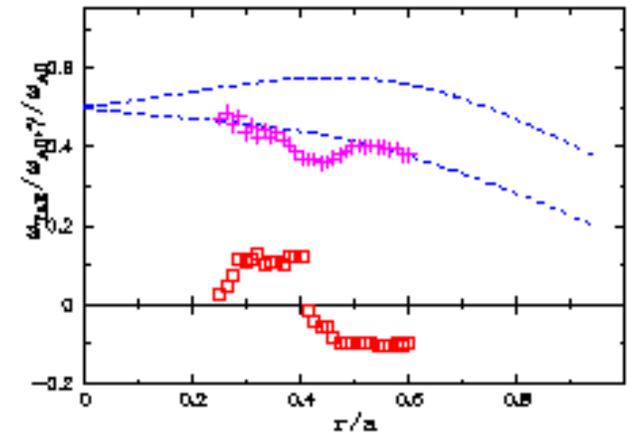
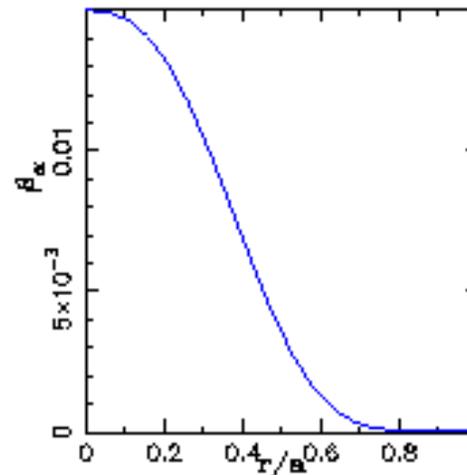
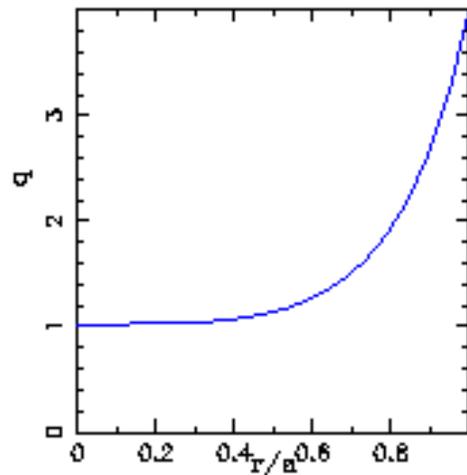
$B=4.45$  T

Deuterium hot slowing down ions  $v_h = 10^9$  cm/sec,  $v_h/v_A=1$ ,  $R/\rho_h = 55.6$

Fishbone branch reproduced by NOVA-2 and M3D

Linear stabilization phase of  $n=1$  mode agrees for 3 codes





Other parameters:

$R=2, m, a = 0.525m, B = 10T, I_p = 6.45MA;$

$n_e = 5 \times 10^{14} (1 - \Psi^{0.281})^{0.1384}, cm^{-3}, \beta_{th}(\Psi) = 9.7(1 - 0.876\Psi^{0.557})^{1.73}\%$ .

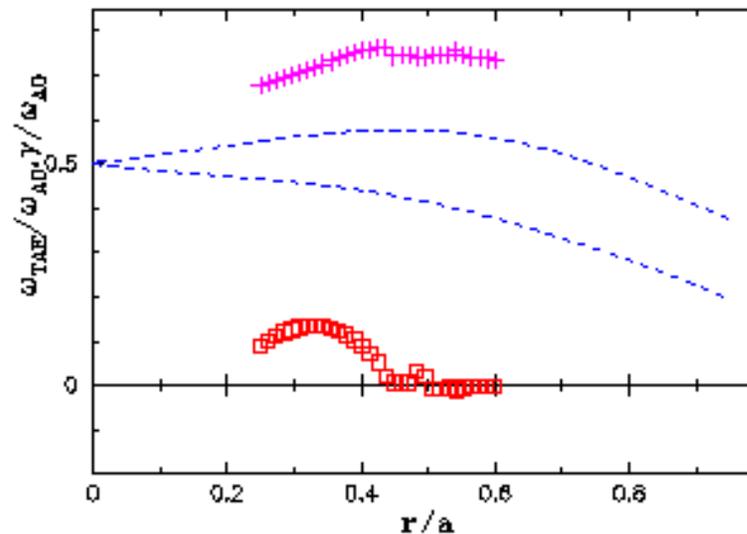
Critical for RTAE  $\beta_{0,crit} = 0.65\%$  (local  $\beta_{\alpha} = 0.4\%$ ).

## FIRE regular $q$ -profile plasma variations

*PPPL*

case	$n_e(0), 10^{14} \text{cm}^{-3}$	$n_{DT}(0), 10^{14} \text{cm}^{-3}$	$T_e(0), \text{keV}$	$n/n_{Gr}$	$P_{fus}, \text{MW}$	$\beta_{\alpha}(0), \%$
1-unst.	5.59	4.22	20	0.66	257	1.5
2-unst.	6.39	4.82	17.5	0.75	262	1.05
3-stab.	7.45	5.62	15	0.89	263	0.69
4-stab.	8.94	6.74	12.5	1.06	250	0.4

In regular  $q$ -profile there is **window** for RTAE free operation.  
 KTAEs are still unstable.

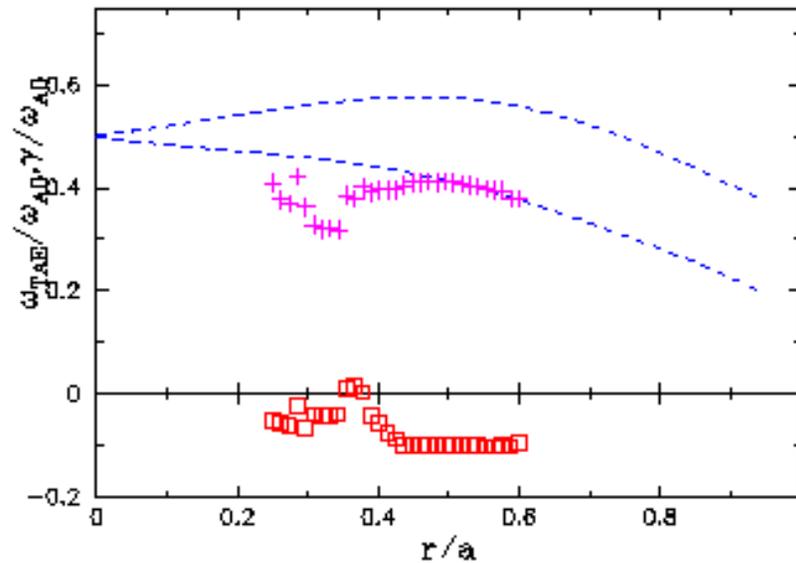
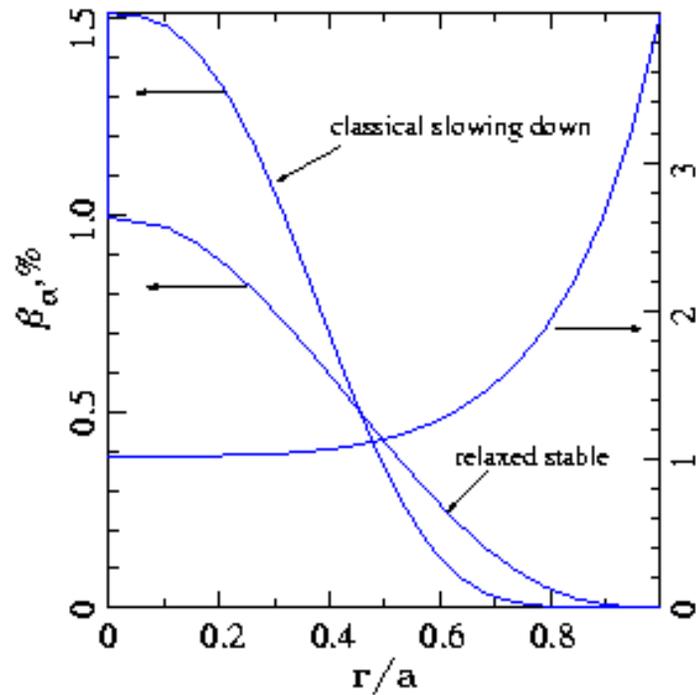


KTAE:  $\beta_{0crit} = 0.5\%$  at  $r/a = 0.35$  analysis and  $\beta_{crit} = 0.33\%$

Regular  $q$ -profile with relaxed fast particle pressure.

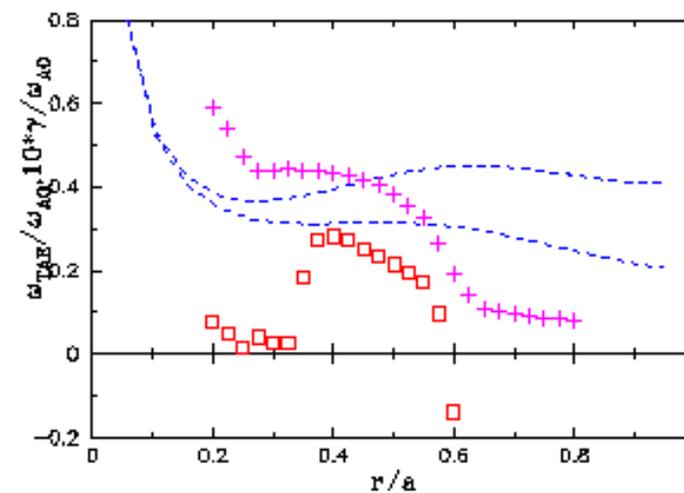
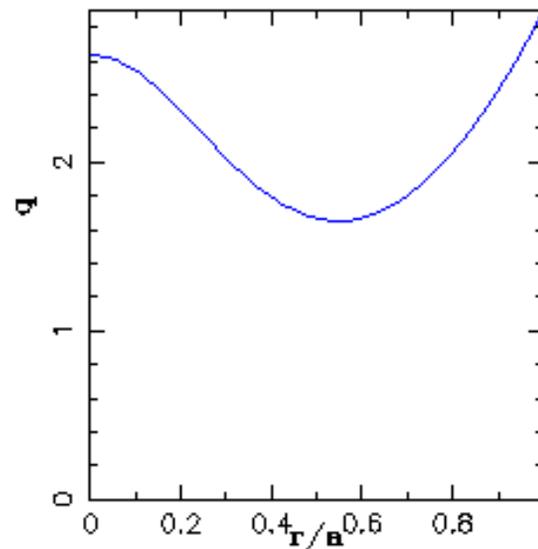
PPPL

If the profile is allowed to relax without particle loss, stability to these Alfvén waves is achieved at higher  $\beta_{0crit} - 1\%$ .



## Inversed $q$ -profile

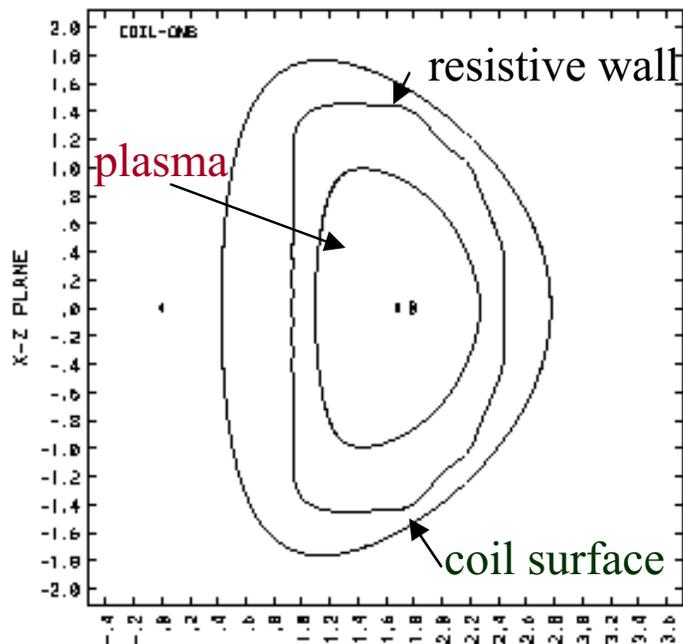
PPPL



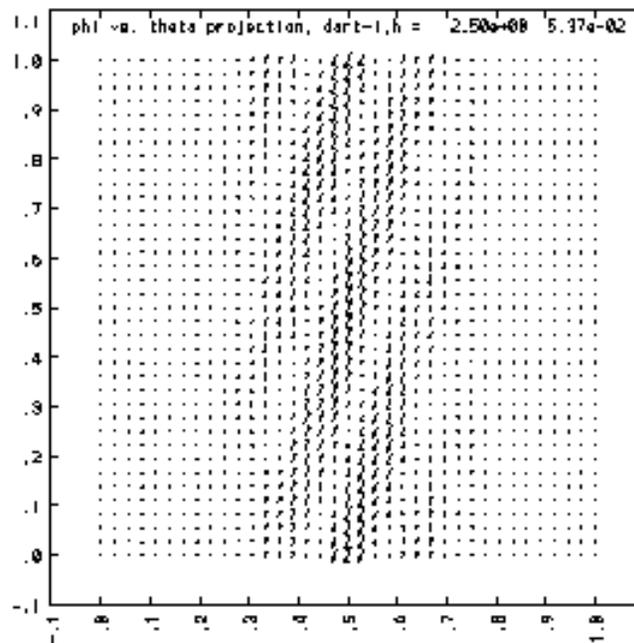
RTAE is found near  $q_{min}$  at critical  $\beta_{0crit} = 0.23\%$  at  $r/a = 0.4$ , (local  $\beta_{\alpha} = 0.047\%$ ).  
**NO relaxed RTAE stable profiles were found.** Alphas will be transported outside  $q_{min}$  surface.

# Resistive Wall Mode and Active Feedback Stabilization

We are developing a major extension of the linear stability codes to include resistive walls, coils, circuit equations, feedback systems, with self-consistent plasma response...interface with both **PEST** and **GATO**—also benchmark with Columbia **VALEN** code



**VACUUM** model includes plasma, wall, and coil surface



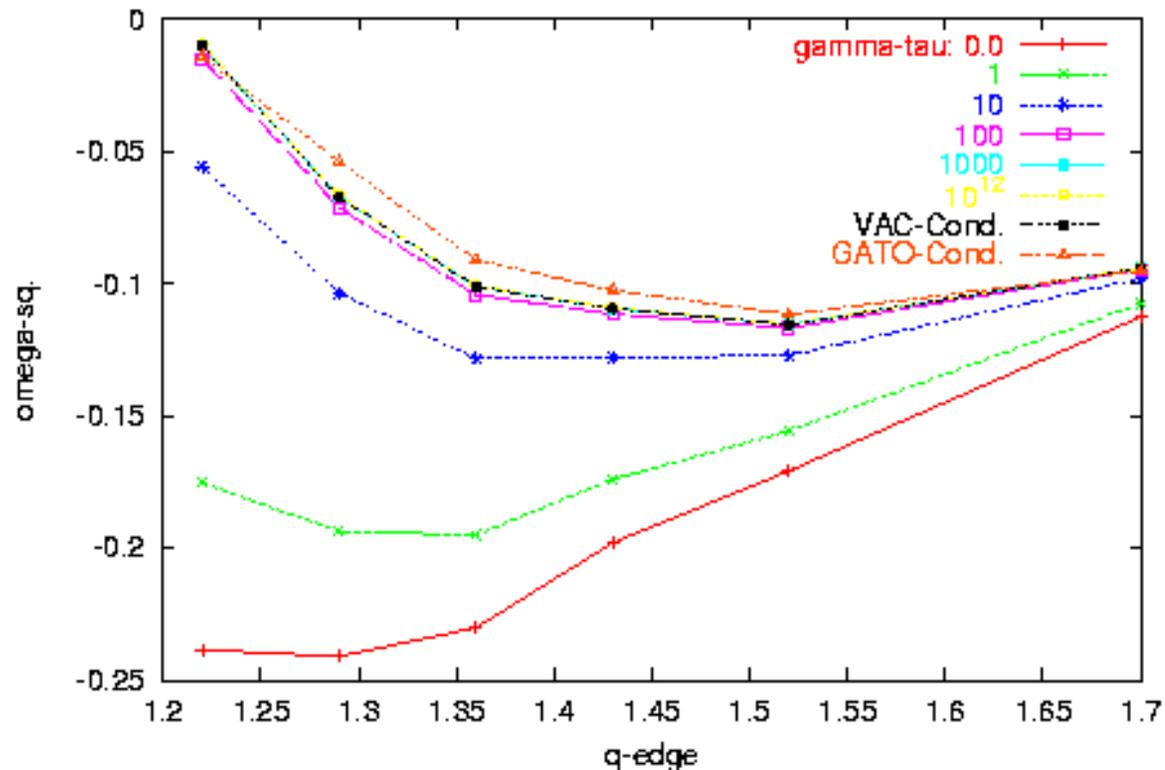
Induced currents in wall in absence of feedback

$\omega^2$  vs  $q_{\text{edge}}$  for various  $\gamma\tau_s$  using GATO + VACUUM: for a conformal resistive shell at  $b = 0.5 a$ .

- $\gamma\tau_s \rightarrow \infty$  reproduces perfectly conducting shell results
- $\gamma\tau_s \rightarrow 0$  gives no-wall limit
- $\gamma\tau_s$  in between gives intermediate result

**Future Plans:**

- include sensor and feedback coils in system while keeping the self-adjoint property



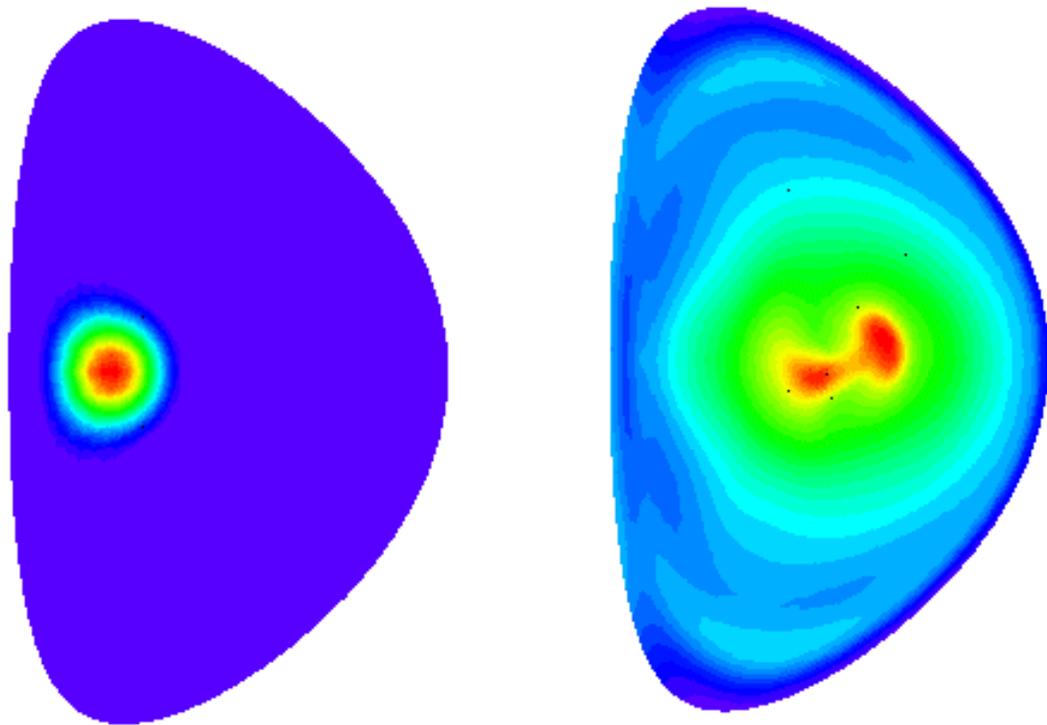
## M3D code is being applied to explain physical mechanism for deep penetration of inside pellet launch

- first 3D simulation of this experimentally discovered phenomena

[Strauss, Park, et al, Phys. Plasmas 7 (2000) 250]

- led to development of 2D model now in TSC code

[Jardin, Schmidt, et al, Nucl. Fusion 39 (2000) 923]



# Energy Confinement

- Empirical scaling laws predict FIRE will achieve  $Q=10$  at  $H_{98}=1.2$  (LF) or  $H_{98}=1.0$  (HF) using ITER98-H(y,2) fit to data
  - Need to examine scaling of narrower subsets of data: eg. With  $n/n_{GR} > 0.6$ ,  $T_i/T_e < 1.5$ ,  $q_{95} < 3.2$ ,  $\beta_\theta > 0.5$
- Good theory based model of plasma confinement would increase confidence...such as what is coming from Gyrokinetic codes
  - FIRE would provide invaluable calibration point for such codes
- Good theory based model of physics of L-H transition would increase confidence: threshold power, edge pedestal height and width
- Some uncertainties regarding impact of sawtooth, NTM, and other MHD on energy confinement

# Other Physics Issues for FIRE

## conventional operating modes

- the effect of H-mode profiles on MHD stability (Manickam)
  - relation to ELMS,  $n \sim 5-10$  peeling modes, bootstrap currents
- error fields and locked modes (LaHaye, et al)
- need to assess disruption effects

## reversed shear operating modes

- characterization of no-wall advanced mode for entire discharge (Ramos)
- wall stabilized advanced modes (GA/PPPL/Columbia experiments on DIII)

## other advanced modes

- off axis CD to raise  $q_0$  (Kessel)
- edge current drive to improve stability (?)

## Summary

- **No physics “showstoppers” have been identified, but lots of interesting physics issues will come into play**
- **Self-consistent TSC discharge simulations exist for both the high-field (12 T, 7.7 MA, H=1.0) and low-field ( 10T, 6.75 MA, H=1.2) operating modes**
- **Overall, MHD stability looks favorable. Primary uncertainty due to:**
  - MHD activity near  $q=1$  surface
  - edge currents due to H-mode pedestals
  - neoclassical tearing modes
  - error fields and locked modes
- **Experimental prototyping of the FIRE operating modes would be very beneficial**
- **“Advanced Modes” need to be further developed**