

# Optimized beta limits in DIII-D advanced tokamak discharges: global and edge

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# STEADY-STATE ADVANCED TOKAMAK OPERATION AT HIGH BETA IN DIII-D IS BEST ACHIEVED IN A STRONGLY-SHAPED DISCHARGE WITH A BROAD PRESSURE PROFILE

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- Focus is on modification of the present successful scenario with 100% noninductively driven current
- Goal of a high fraction of bootstrap current leads to exploration of methods to maximize  $q_{\min} \beta_N$
- Without modification of the pressure profile, the maximum achieved  $\beta_N$  decreases with increasing  $q_{\min}$
- With a broadened pressure profile,  $q_{\min} \beta_N$  is maximized at the highest  $q_{\min}$  tested
  - Modeling indicates that  $\beta_N = 5$  should be possible
- Increases in beta limits with elongation and triangularity motivate double-null divertor operation

# BALANCING THE REQUIREMENTS FOR STEADY-STATE OPERATION AND HIGH FUSION GAIN LEADS TO A SCENARIO WITH HIGH $q_{\min}$ $\beta_N$

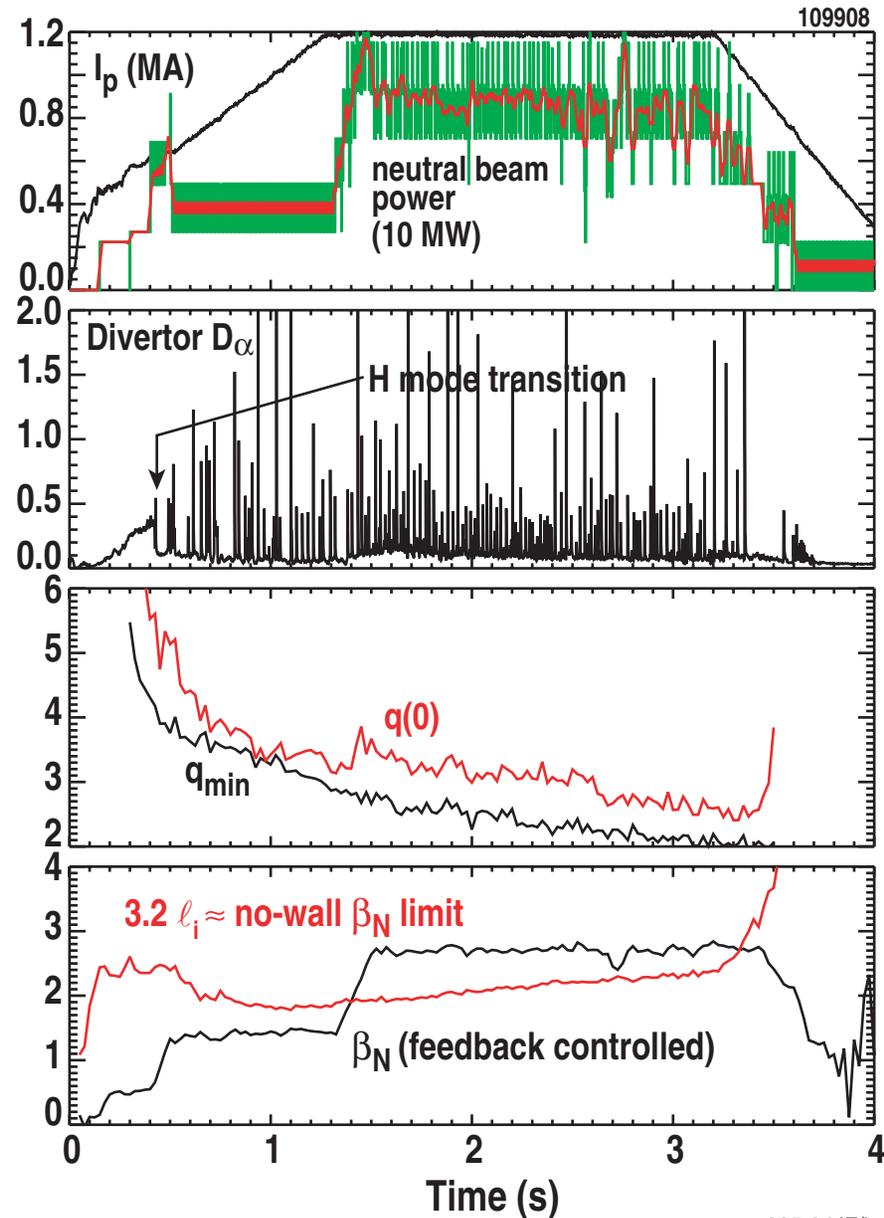
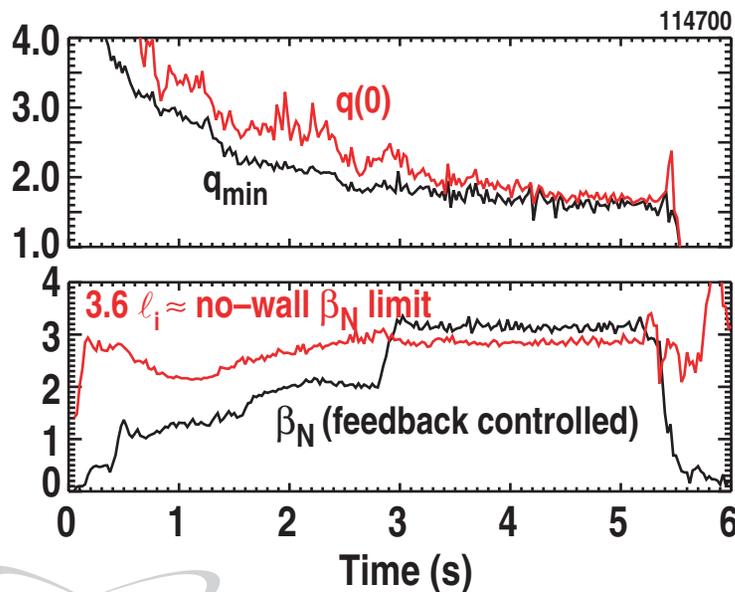
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- **Steady state:** requires a large bootstrap current fraction  
 $f_{BS} \propto \beta_p \propto q\beta_N$
- Motivates operation with elevated  $q$  across the entire profile
- For high fusion gain  $\propto \beta\tau_E \propto \beta_N H_{89}/q_{95}^2$ , increase  $q_{\min}$  rather than  $q_{95}$
- Highest possible  $\beta_N$  to maximize fusion gain and  $f_{BS}$
- Off-axis electron cyclotron current drive (ECCD) used to regulate current profile
  - Efficiency increases with  $\beta_e$
- Divertor exhaust pumping to control H-mode density
  - For relevant collisionality and efficient ECCD
  - Presently in DIII-D, this requires an **upper single-null divertor shape**

# SCALING WITH $q_{\min}$

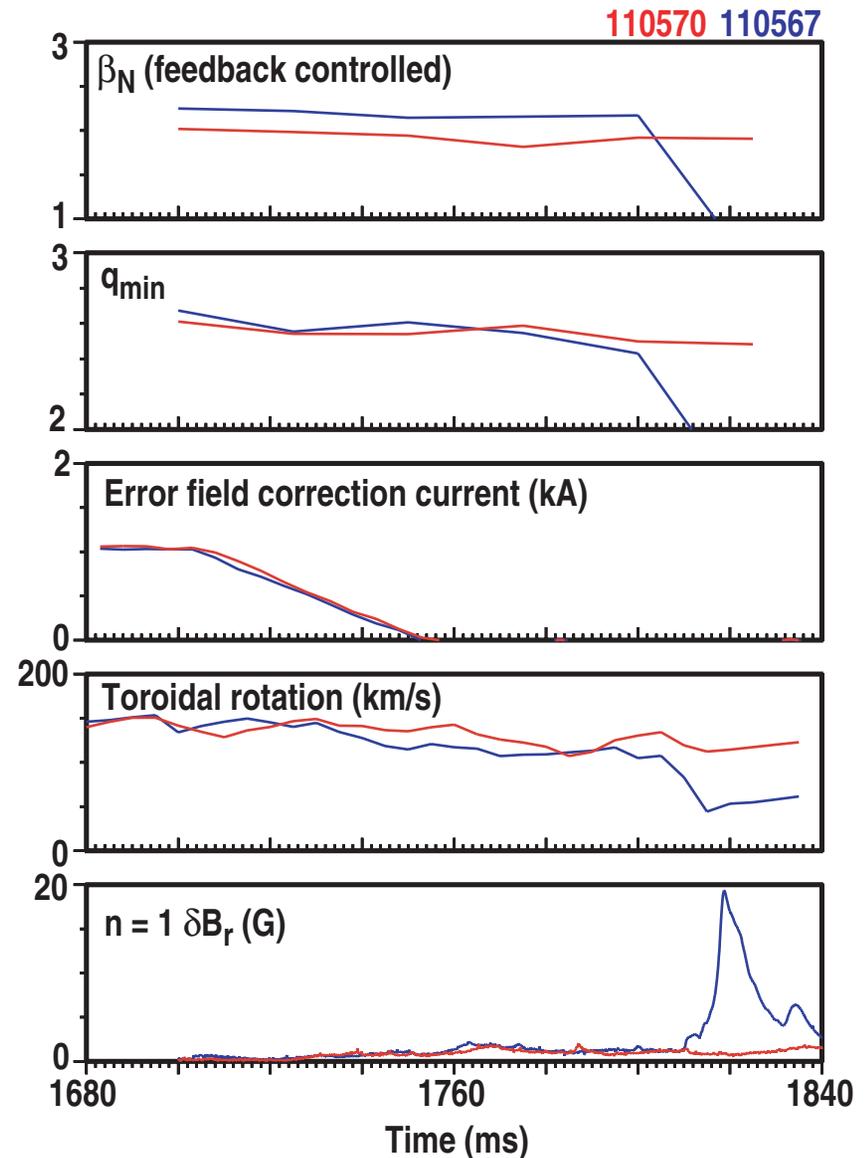
# THE $q$ PROFILE IS VARIED BY MODIFYING THE DISCHARGE FORMATION OR DELAYING THE HIGH BETA PHASE

- Increased  $T_e$  in H-mode slows rate of current penetration
- $1.5 < q_{\min} < 3$ ,  $q_{95} \approx 5$
- Two examples,  $q_{\min} \approx 2.5$ ,  $\beta_N = 2.7$  and  $q_{\min} \approx 1.7$ ,  $\beta_N = 3.2$  run without significant MHD for discharge duration



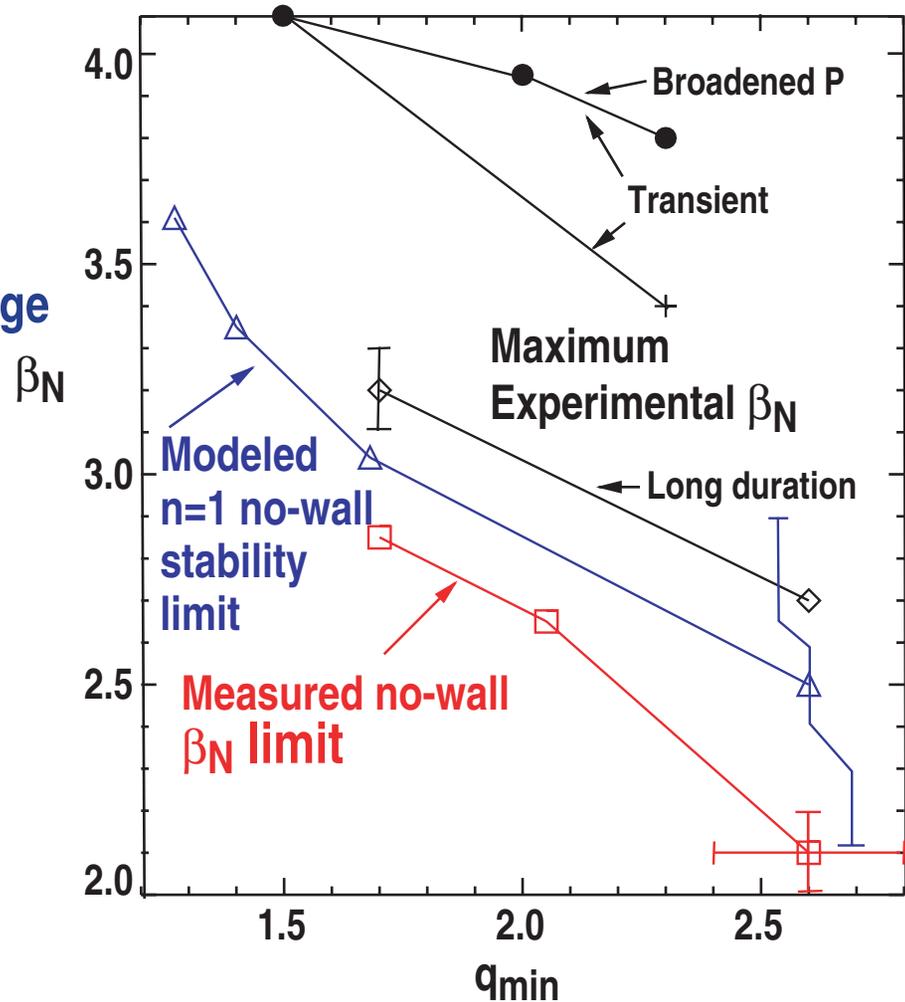
# THE NO-WALL $\beta_N$ LIMIT IS MEASURED BY MONITORING STABILITY AS THE CORRECTING CURRENT FOR NONAXISYMMETRIC FIELDS IS REMOVED

- For  $\beta_N$  above the no-wall limit, the drag on toroidal rotation is enhanced because of the plasma response to the nonaxisymmetric fields
- Rotation decreases significantly to below the critical level for  $n = 1$  resistive wall mode stabilization



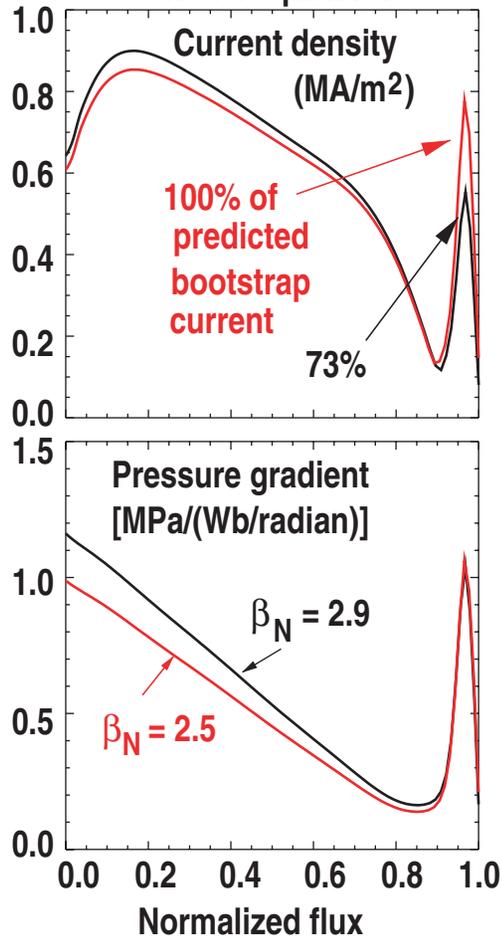
# MEASURED NO-WALL $\beta_N$ LIMIT AND MAXIMUM EXPERIMENTAL $\beta_N$ DECREASE AS $q_{min}$ INCREASES

- Trend is the same for the  $n = 1$  no-wall stability limit calculated for model equilibria
- High  $\beta_N$  for the full DIII-D discharge duration without MHD is limited to 10% – 30% above measured no-wall limit
- Dependence of maximum achievable  $\beta_N$  on  $q_{min}$  reduced by broadening pressure profile



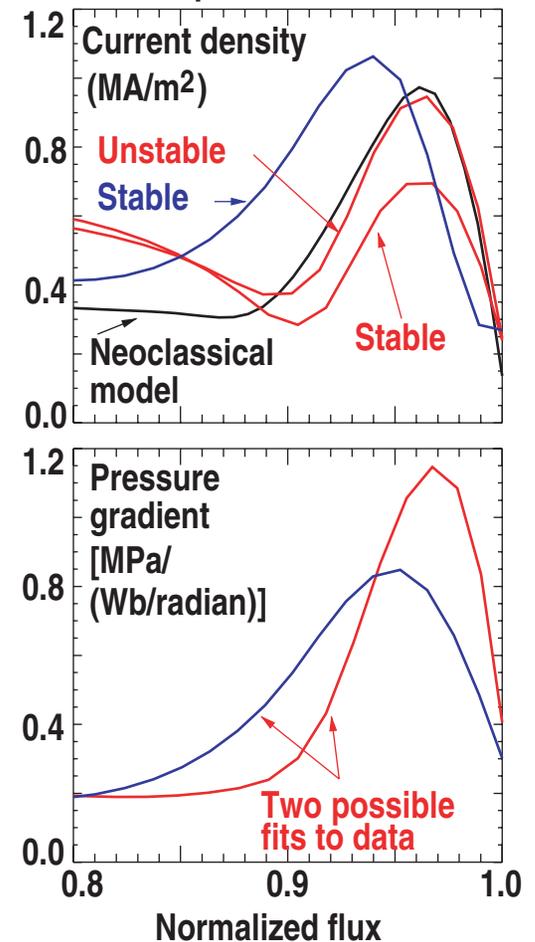
# QUANTITATIVE AGREEMENT BETWEEN THE MEASURED NO-WALL $\beta_N$ LIMIT AND THEORY DEPENDS ON VALUES OF H-MODE PEDESTAL J AND P'

Two marginally stable model equilibria



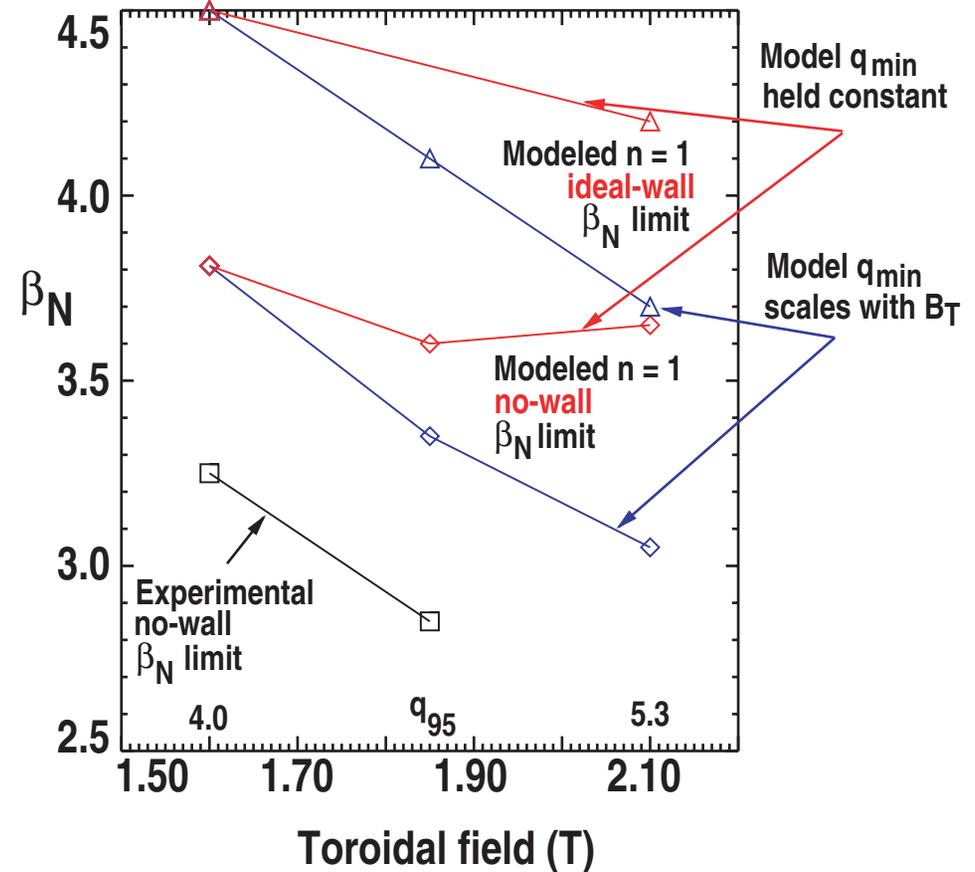
- Increased  $J_{\text{pedestal}}$  is destabilizing
- Stability is sensitive to the position of P' and J peaks
- Peak J matching neoclassical bootstrap plus ohmic best matches experimental observation of an instability

Several possible fits to experimental data



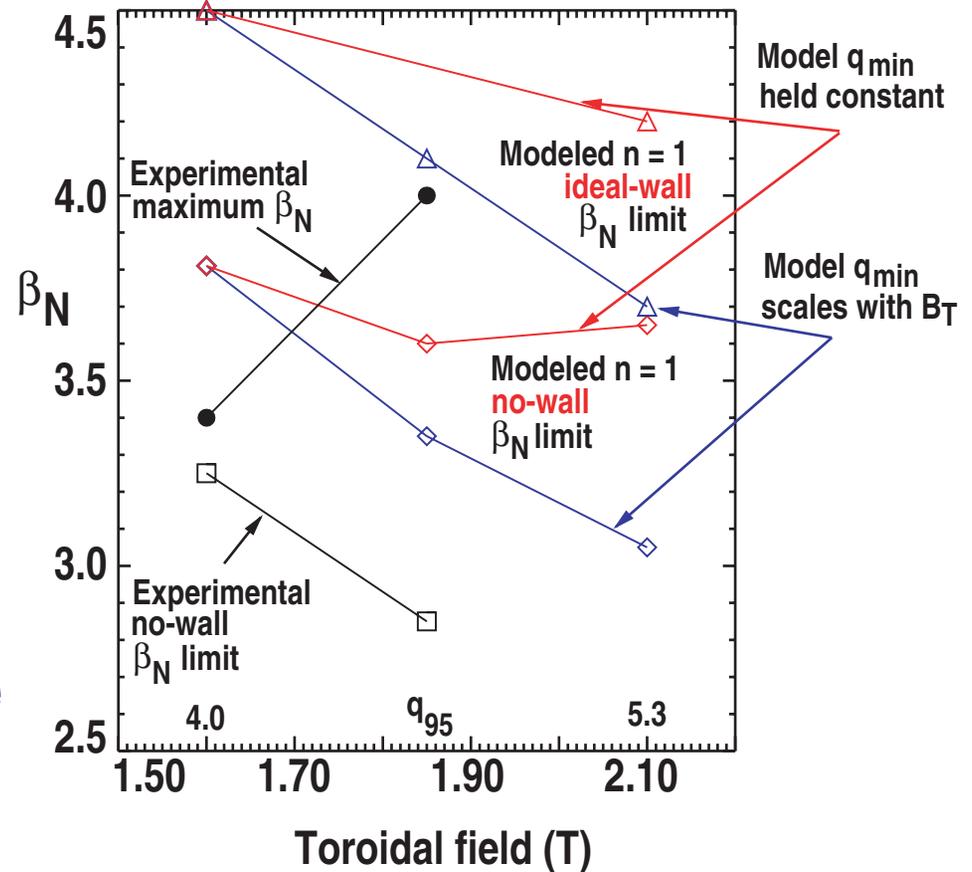
# $q_{95}$ FOR STEADY-STATE EXPERIMENTS IS CHOSEN TO MAXIMIZE THE EXPERIMENTALLY ACHIEVABLE $\beta_N$

- Modeled  $n = 1$  stability limits show a decrease with increasing  $B_T$  ( $q_{95}$ )
- Trend with  $q_{95}$  of measured no-wall limit agrees with the modeling
  - Quantitative difference results from different  $q_{min}$  values



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- Trend with  $q_{95}$  of measured no-wall limit agrees with the modeling
  - Quantitative difference results from different  $q_{min}$  values
- Operation closer to the ideal-wall limit at increased  $B_T$  is responsible for the increase in achievable  $\beta_N$

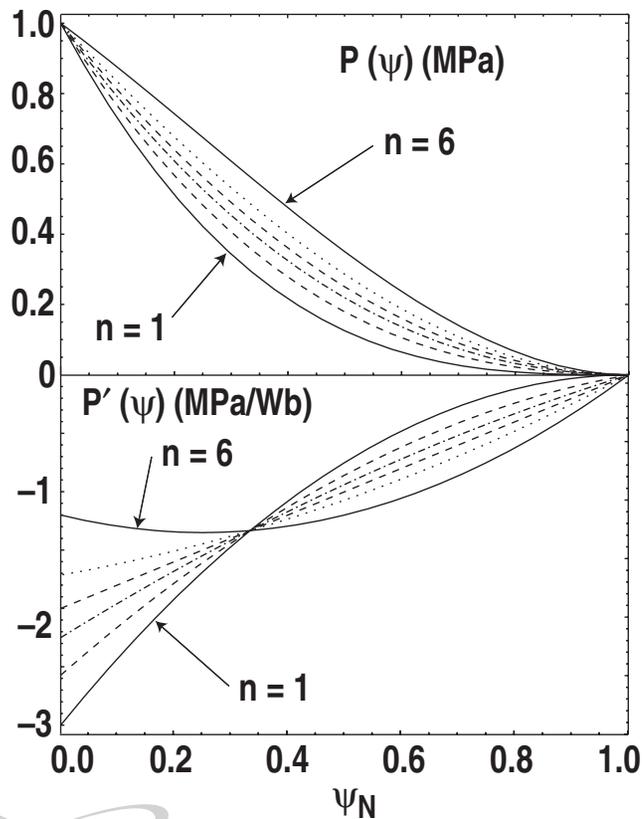


# **EFFECT OF BROADENED PRESSURE PROFILE**

# A MODELING STUDY INVESTIGATED THE DEPENDENCE OF $\beta_N$ LIMITS ON THE PRESSURE GRADIENT PROFILE SHAPE IN $f_{BS} > 70\%$ EQUILIBRIA

- Core  $P'$  specified by a family of polynomials:

—  $P'(\psi) = 1 + b_n\psi - (1 + b_n)\psi^2$



- Hyperbolic tangent form used for H-mode edge pressure pedestal:

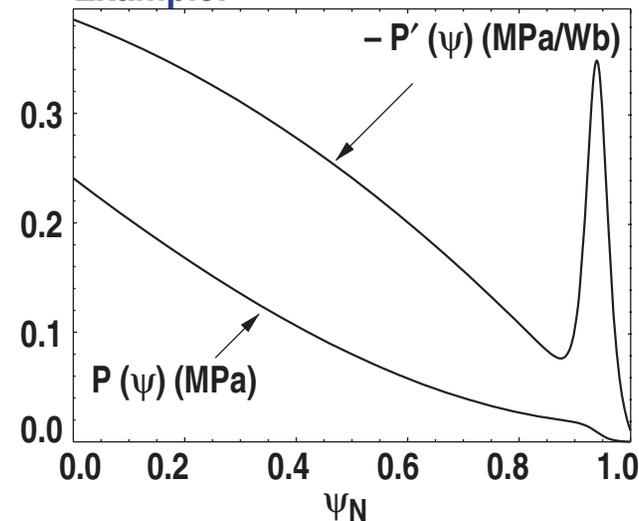
— Based on experiment scaling

—  $P_{ped} \propto I_p^2 (1 + \beta_p)^{0.9} (1 + \delta)^{2.11} (1 + \kappa^2)^{-1.15}$

- Total pressure = core + pedestal

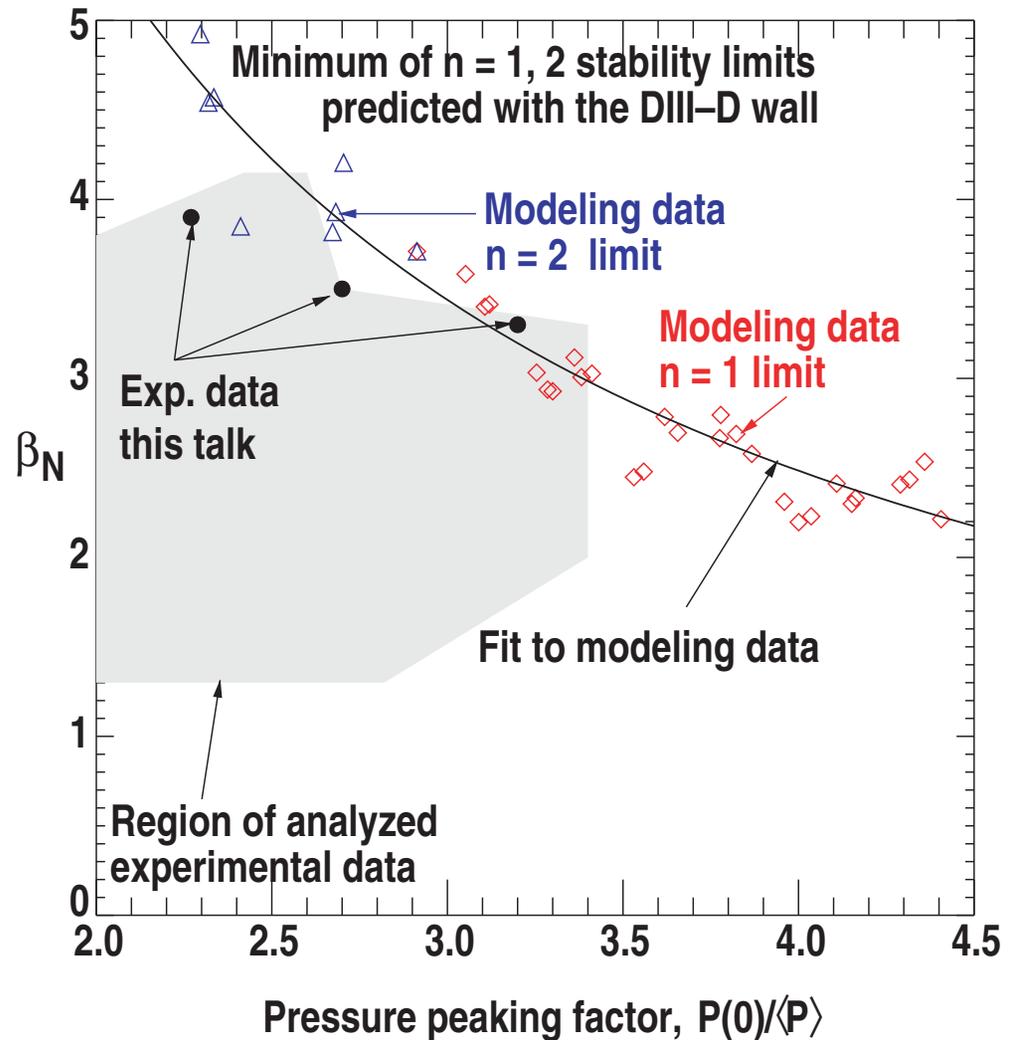
—  $P(0)/\langle P \rangle$  ranges from 2 to 4.5

Example:



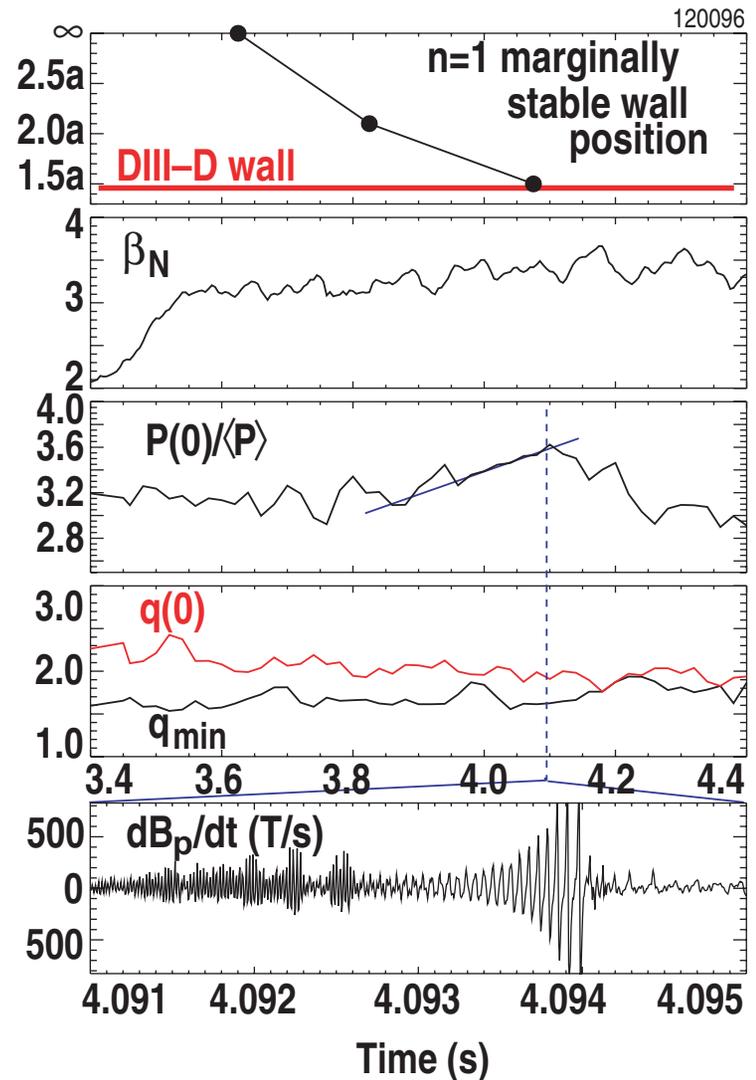
# PREDICTED $\beta_N$ LIMITS DECREASE STRONGLY AS THE PRESSURE PROFILE BECOMES MORE PEAKED

- $n = 2$  is the limit for  $P(0)/\langle P \rangle < 3$
- Scatter results from the range of discharge shapes included
- Model equilibria have  $q_{\min} \approx 2$
- Predicted values agree roughly with the experimental data
- Fit:  
$$\beta_N = 11.9[P(0)/\langle P \rangle]^{-1.13}$$

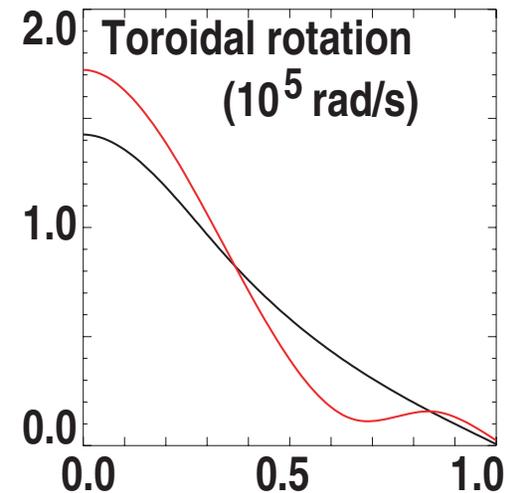
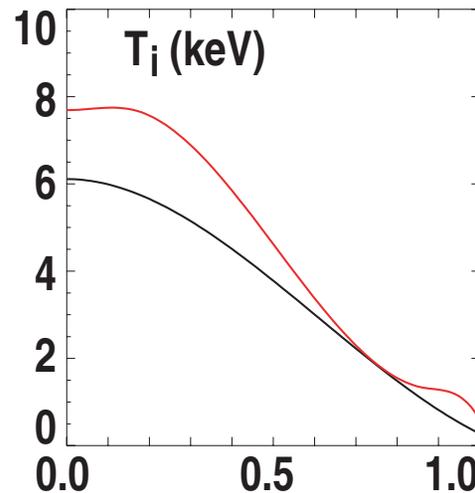
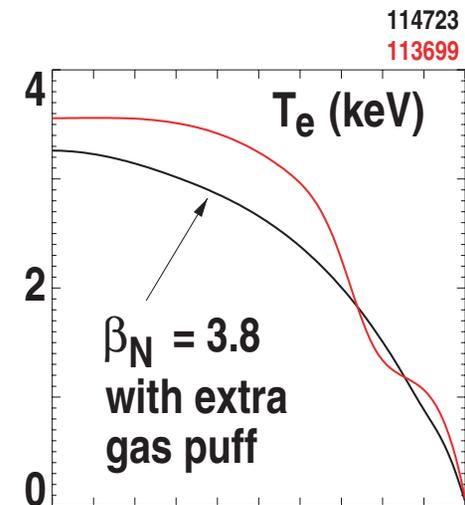
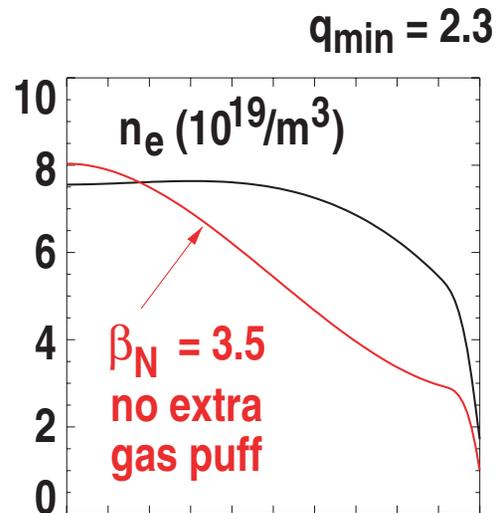
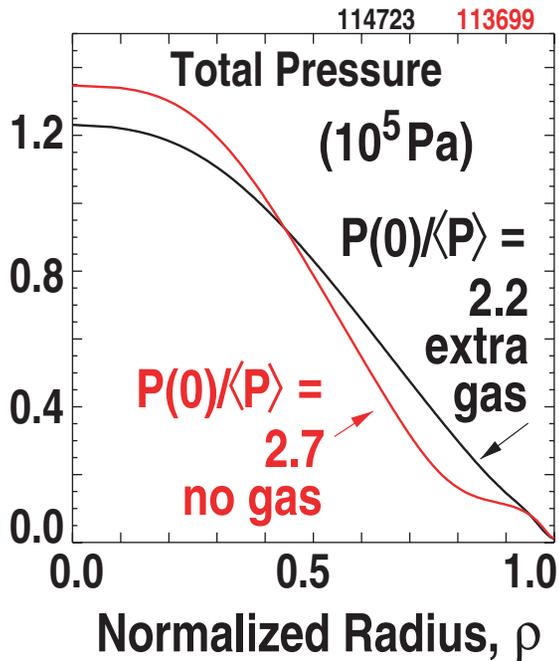


# WITH EFFICIENT PARTICLE EXHAUST PUMPING $P(0)/\langle P \rangle$ IS HIGH AND $\beta_N$ LIMIT IS REDUCED

- Pumping reduces  $n_e^{\text{pedestal}}$ , core neutral beam fueling increases  $n_e(0)$
- There is weak negative central shear that leads to a weak internal transport barrier, further peaking  $n_e, T_i$
- Internal mode grows on a rapid time scale
  - Kink mode phasing similar to pressure gradient driven resistive interchange
  - Initiates reduction in P peaking and change in bootstrap profile
  - In some discharges, a disruption immediately follows the mode



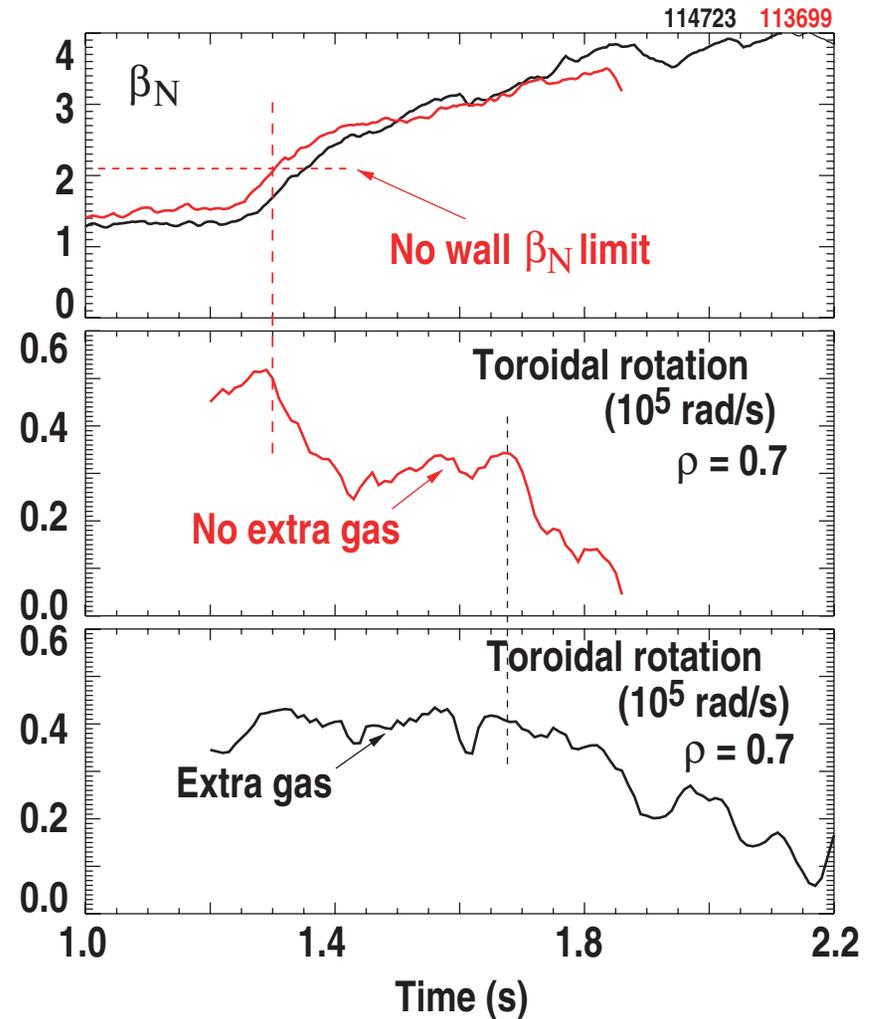
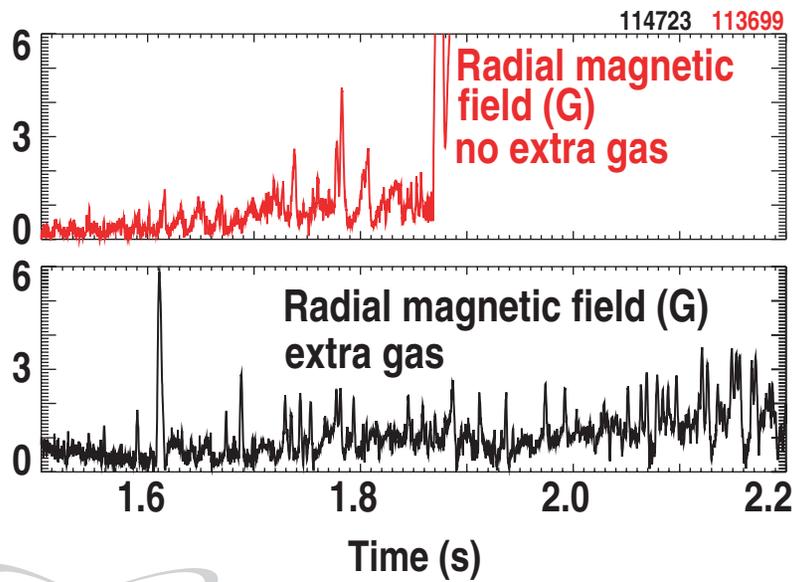
# IN THE EXPERIMENT, A BROADER PRESSURE PROFILE AND HIGHER $\beta_N$ WERE OBTAINED BY BROADENING THE DENSITY PROFILE WITH EXTRA GAS PUFFING



- $P(0)/\langle P \rangle = 2.2$  versus **2.7**
- In the case without the gas puff,  $P(0)/\langle P \rangle$  is enhanced because core rotational shear increases

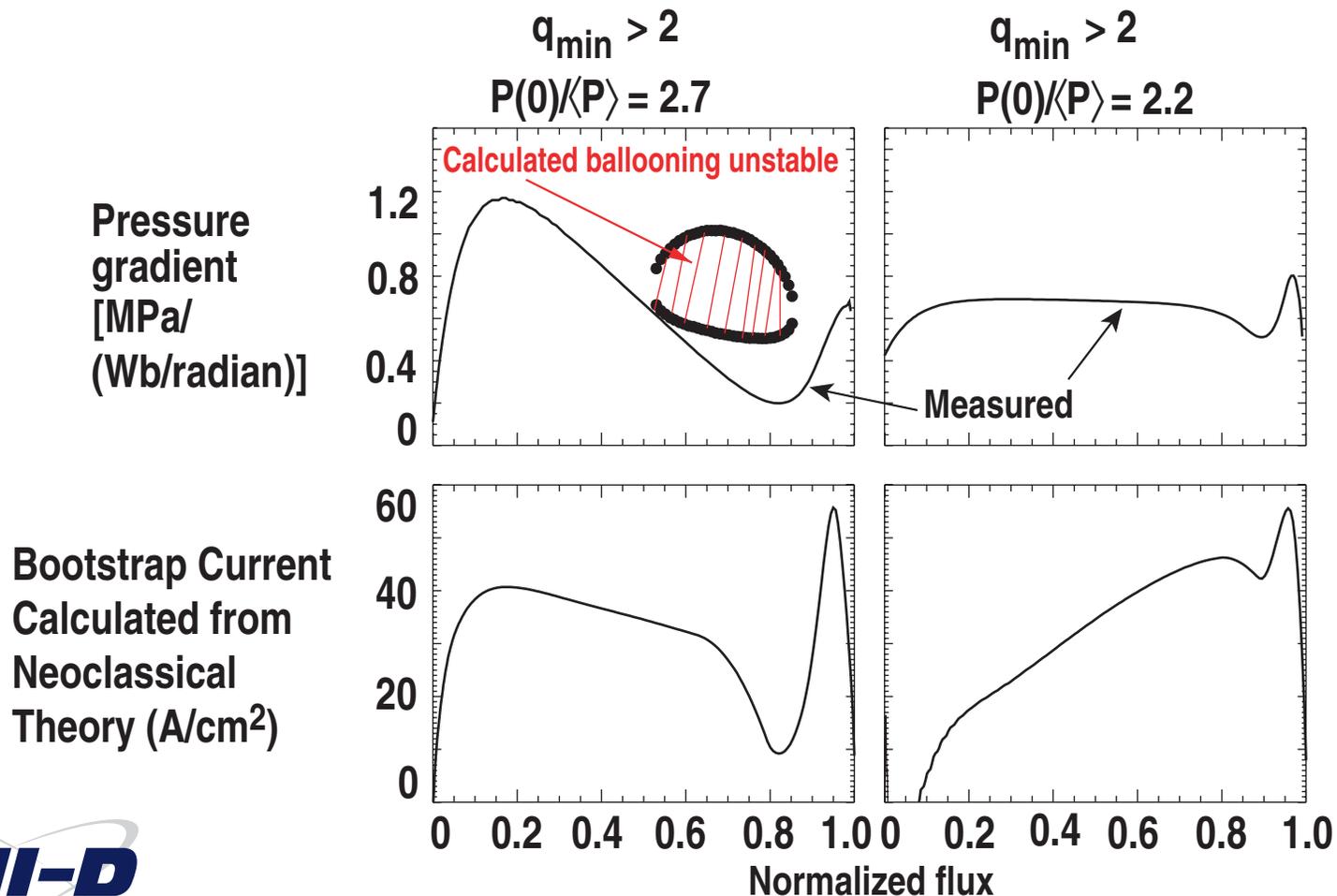
# BROADER PRESSURE PROFILE ALLOWS BETA TO CONTINUE RISING TO $\beta_N = 4$ at $q_{min} = 2$

- Rotation decreases as  $\beta_N$  passes above the ideal no-wall limit as a result of the enhanced plasma response to external, nonaxisymmetric fields
- Drop in rotation to near 0 as  $\beta_N$  approaches the maximum value results from low level  $n = 1$  resistive wall mode activity



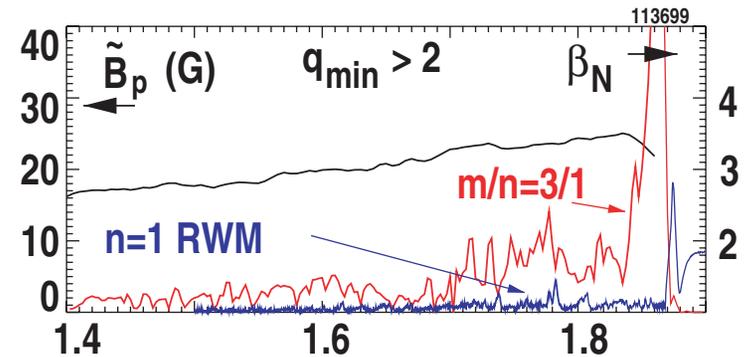
# BROAD PRESSURE IS POSSIBLE BECAUSE OF ACCESS TO THE INFINITE- $n$ BALLOONING MODE SECOND STABLE REGIME ACROSS THE FULL PROFILE

- Normally there is a region where  $dP/d\psi$  is limited by ballooning stability
- Magnetic shear profile modified by broadening bootstrap current



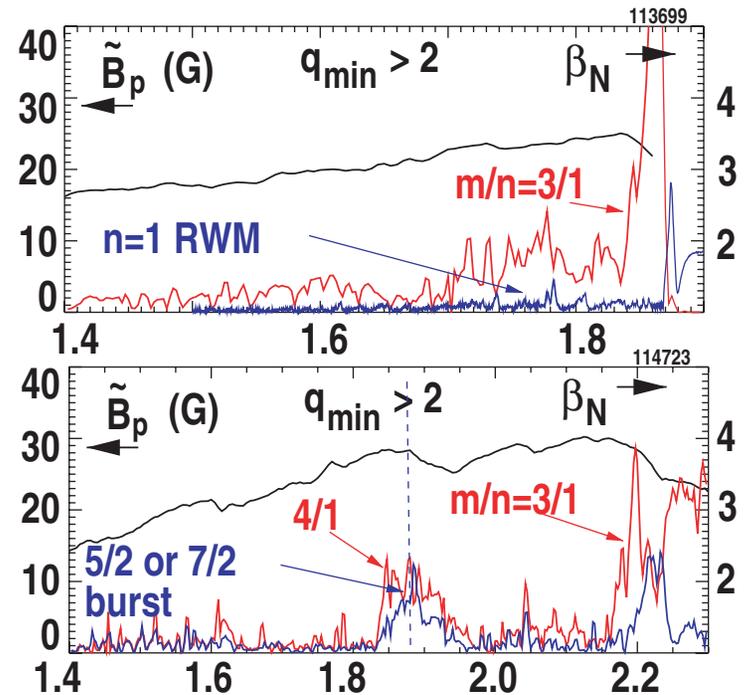
# EVEN WITH $\beta_N$ NEAR THE IDEAL-WALL LIMIT, THE HIGH BETA PHASE ALMOST ALWAYS ENDS AS A RESULT OF A TEARING MODE, NOT A KINK MODE

- $q_{\min} > 2$ , more peaked pressure:  
n = 1 tearing mode locks to low level  
n = 1 RWM



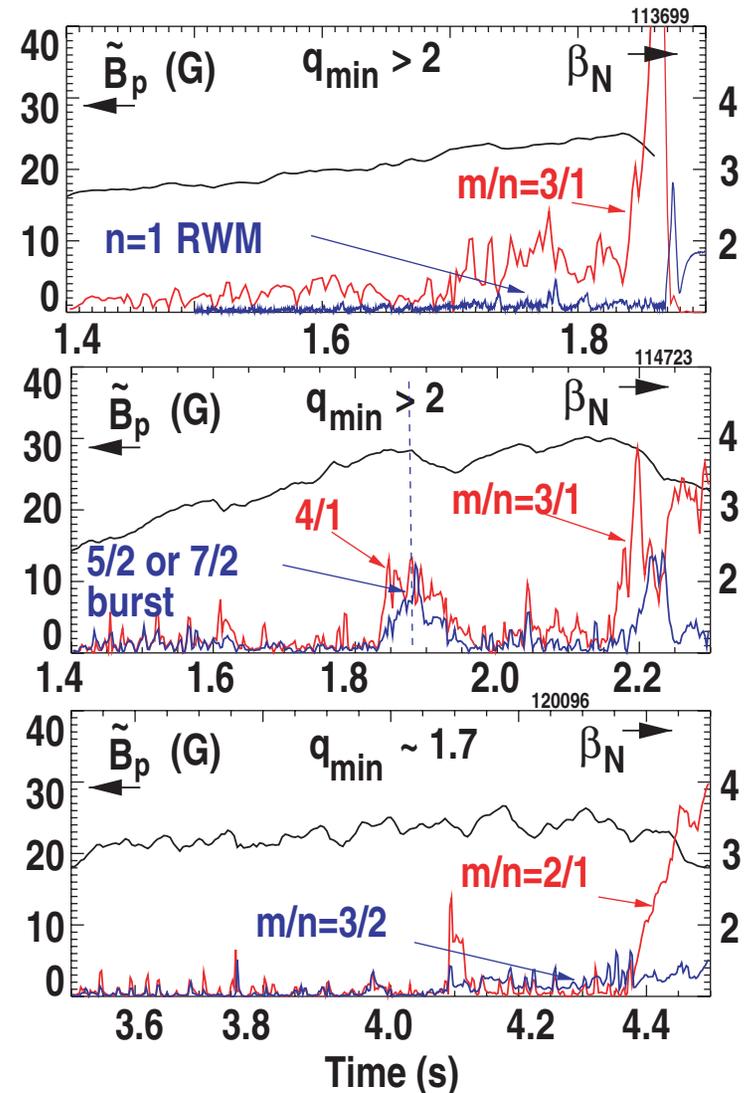
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 $n = 1$  RWM
- $q_{\min} > 2$ , broad pressure:  
 $3/1$  mode grows to large amplitude.  
 Earlier  $n = 5/2$  or  $7/2$  burst briefly reduces beta



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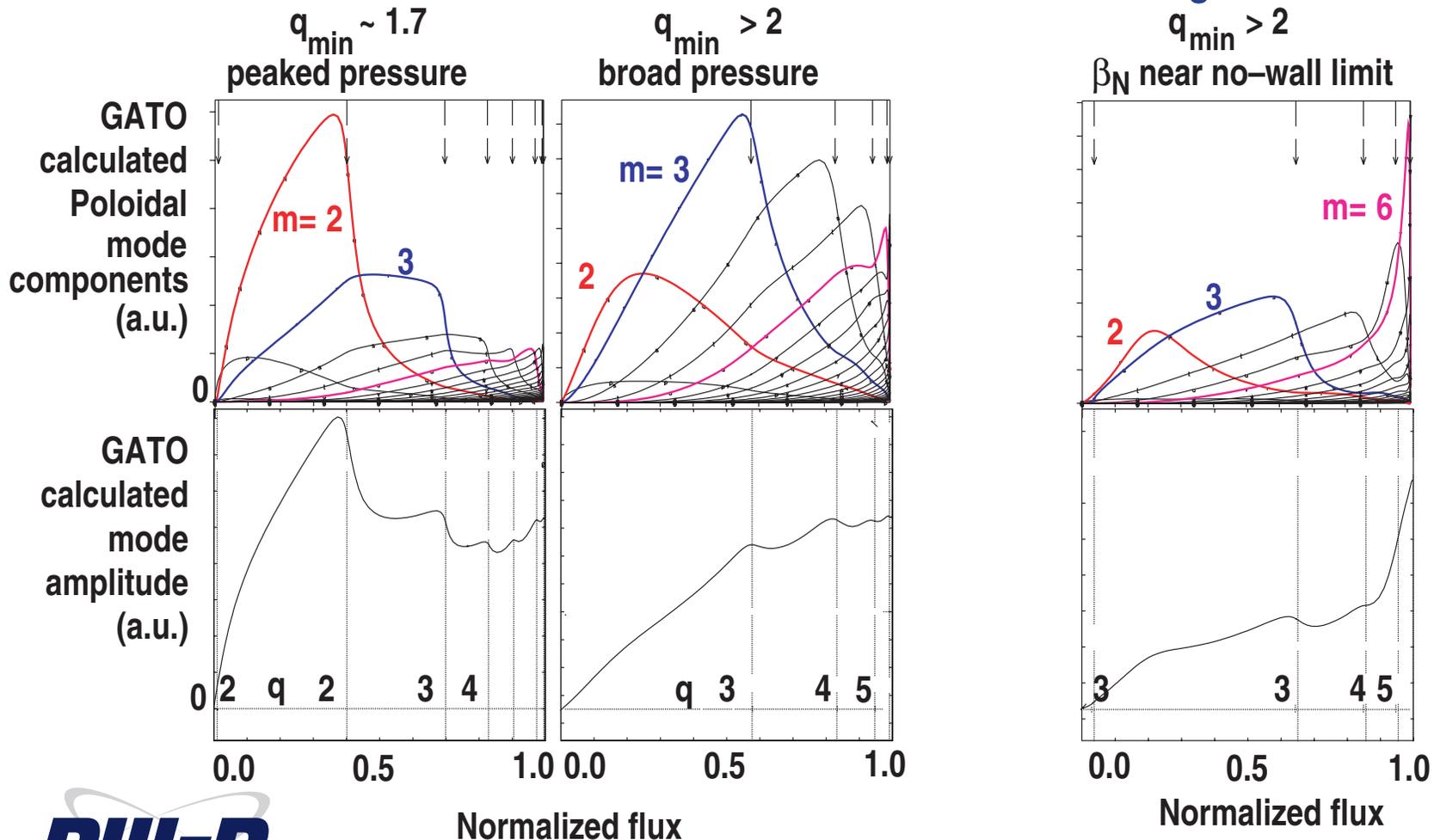
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- $q_{\min} > 2$ , broad pressure:  
 $3/1$  mode grows to large amplitude.  
 Earlier  $n = 5/2$  or  $7/2$  burst briefly reduces beta
- $q_{\min} \approx 1.7$ :  $2/1$  mode grows to large amplitude. Earlier fast growing  $n = 1$  kink-type mode triggers  $3/2$  tearing
- Even if  $q_{\min}$  is maintained above 2 to avoid the  $2/1$  tearing mode, other modes with larger  $m/n$  can still have significant effects on confinement



# THE CALCULATED STRUCTURE OF THE UNSTABLE $n=1$ MODE ILLUSTRATES THE REGIONS OF THE DISCHARGE MOST STRONGLY AFFECTING STABILITY

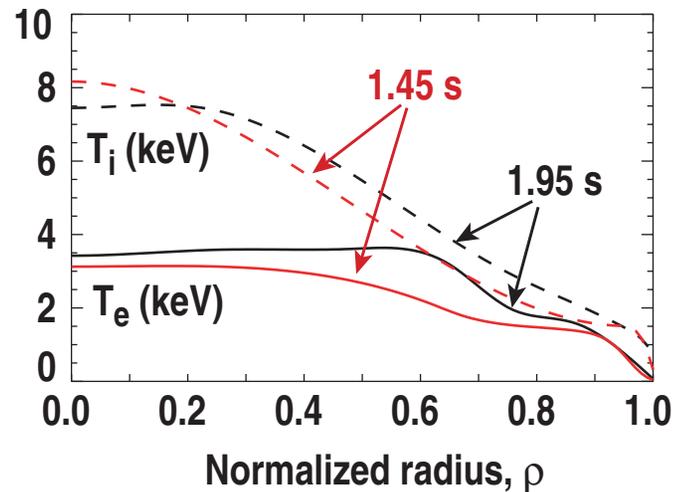
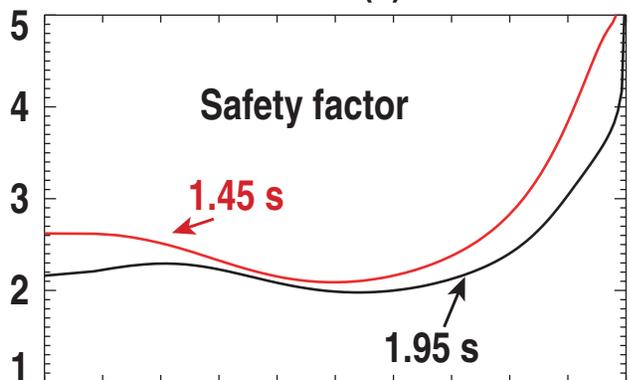
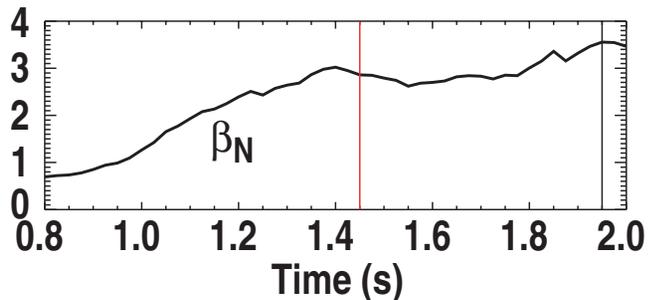
- Peaked pressure,  $q_{\min} \approx 1.7$ :  
 $m = 2$ , mode peaks in the core

- Beta near no-wall limit:  
 $m = 6,7$ , mode peaks at the edge



# A RELATIVELY FLAT $q$ PROFILE WITH LARGE $\rho(q_{\min})$ IS UNDER STUDY AS A WAY TO BROADEN THE PRESSURE PROFILE

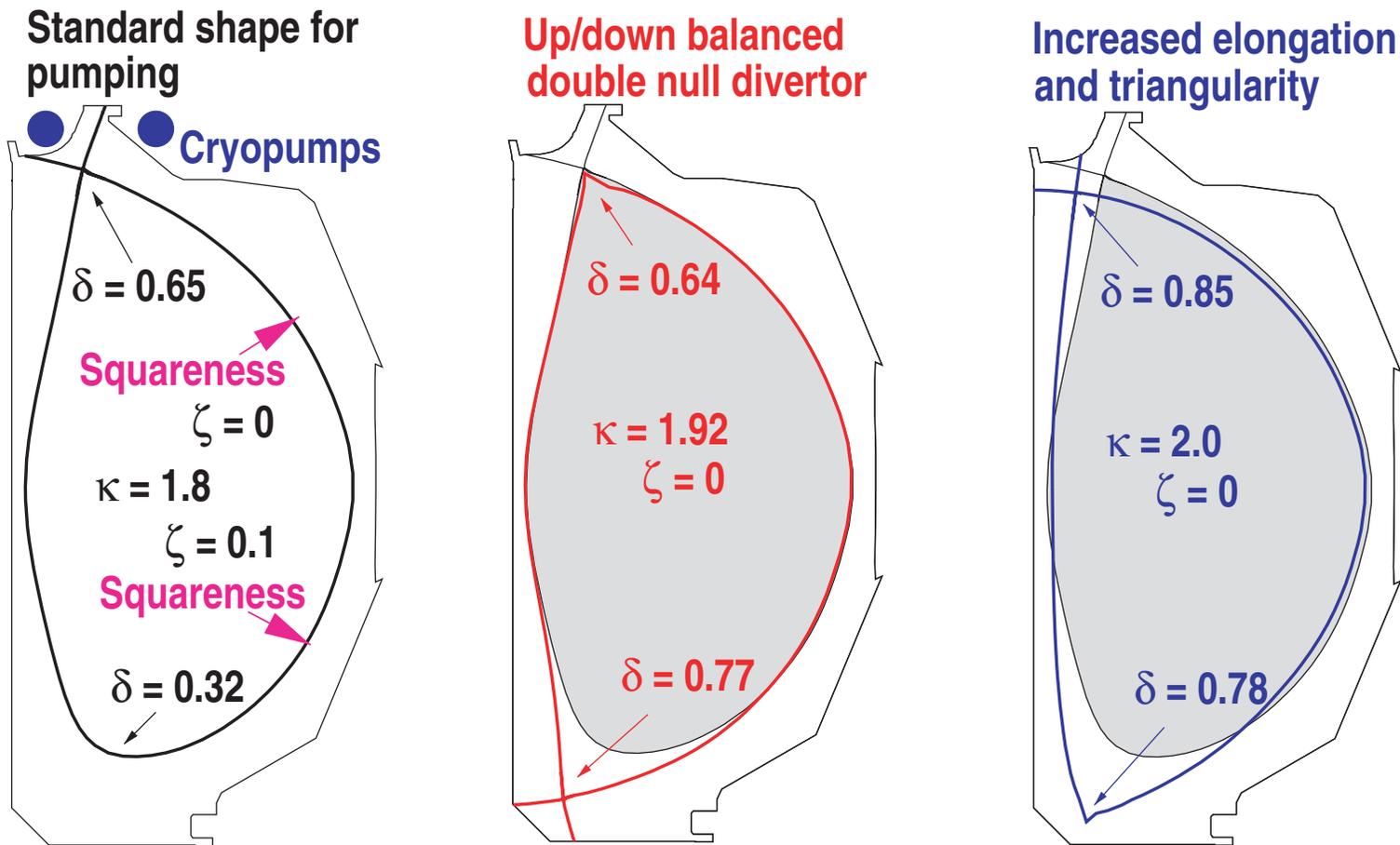
- Preliminary results show broadening of temperature profiles as  $q_{95}$  decreases and  $\rho(q_{\min})$  increases
- A safety factor profile with  $q_{\min} > n$  ( $n$  integer) and  $q_{95} < n + 1$  could be a way to avoid tearing modes



# **DISCHARGE SHAPE CHANGES**

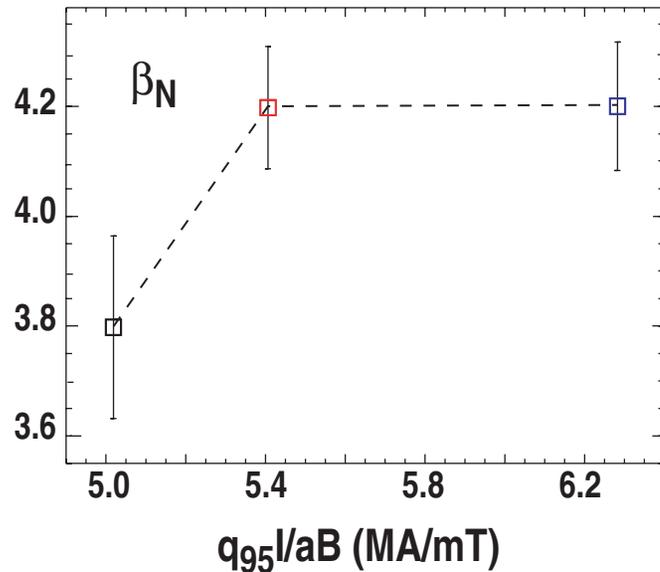
# IN THE EXPERIMENT, THE ACHIEVABLE $\beta_N$ WAS COMPARED IN THE STANDARD PUMPING SHAPE AND DISCHARGES WITH STRONGER SHAPING

- Cryopumps were not used so no change in particle pumping with shape

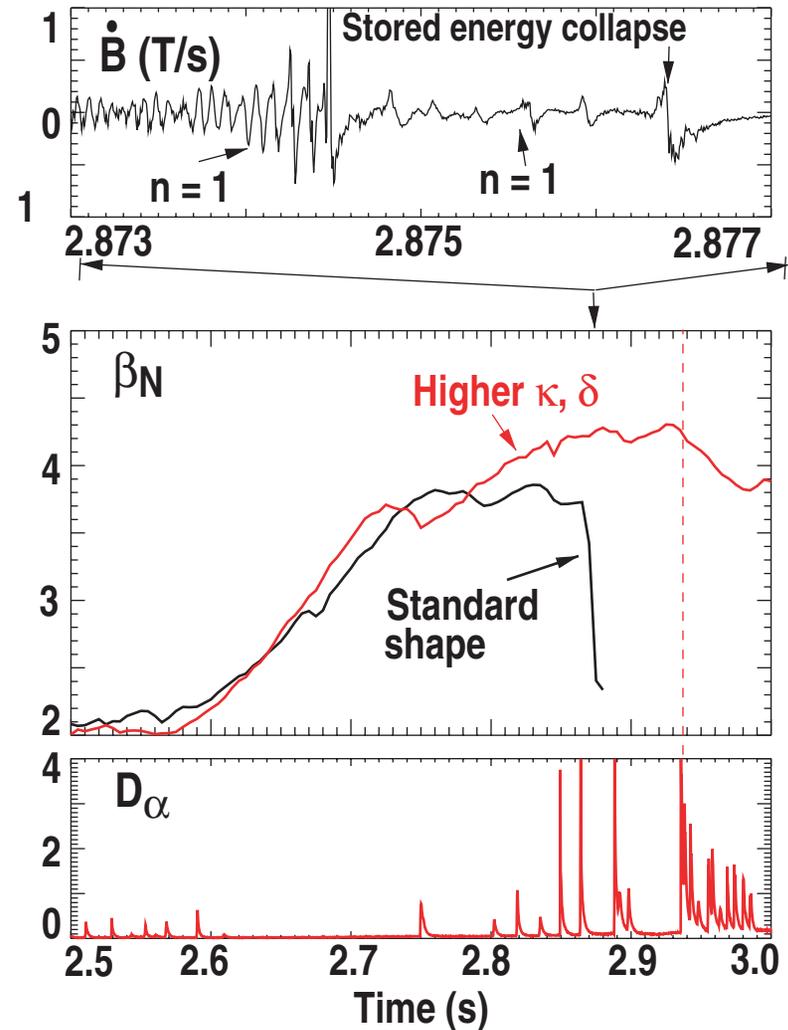


# THE MAXIMUM $\beta_N$ WAS OBTAINED IN THE UP/DOWN SYMMETRIC DOUBLE-NULL DIVERTOR SHAPES

- Changes in profiles could also be important:  $\ell_i$ ,  $P(0)/\langle P \rangle$ , H-mode pedestal

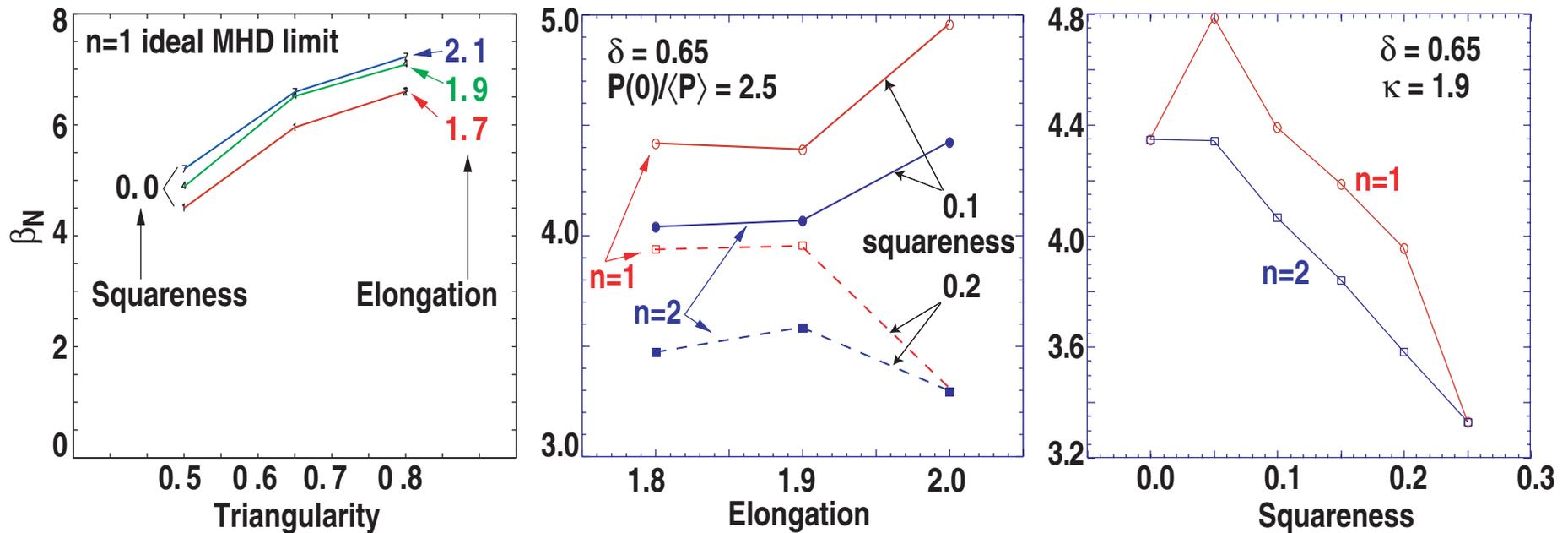


- $\beta_N$  not limited by an ideal kink
  - Standard shape: fast growing core  $n = 1$  leads to a disruption
  - Higher  $\kappa, \delta$  shapes: large ELMs lead to a soft collapse



# MODELING STUDIES PREDICT THAT INCREASES IN $\kappa$ , $\delta$ INCREASE THE IDEAL, LOW- $n$ $\beta_N$ LIMITS

Examples of results from a broad range of parameter scans with double-null



- Indicates increase in experimental  $\beta_N$  likely results from increase in  $\kappa$ ,  $\delta$  in transition from single-null to double-null shape
- $n = 2$ ,  $n = 3$  limits are lower than for  $n = 1$  (here pressure is broad)

## Increasing the H-mode edge pedestal height can help to broaden the pressure profile

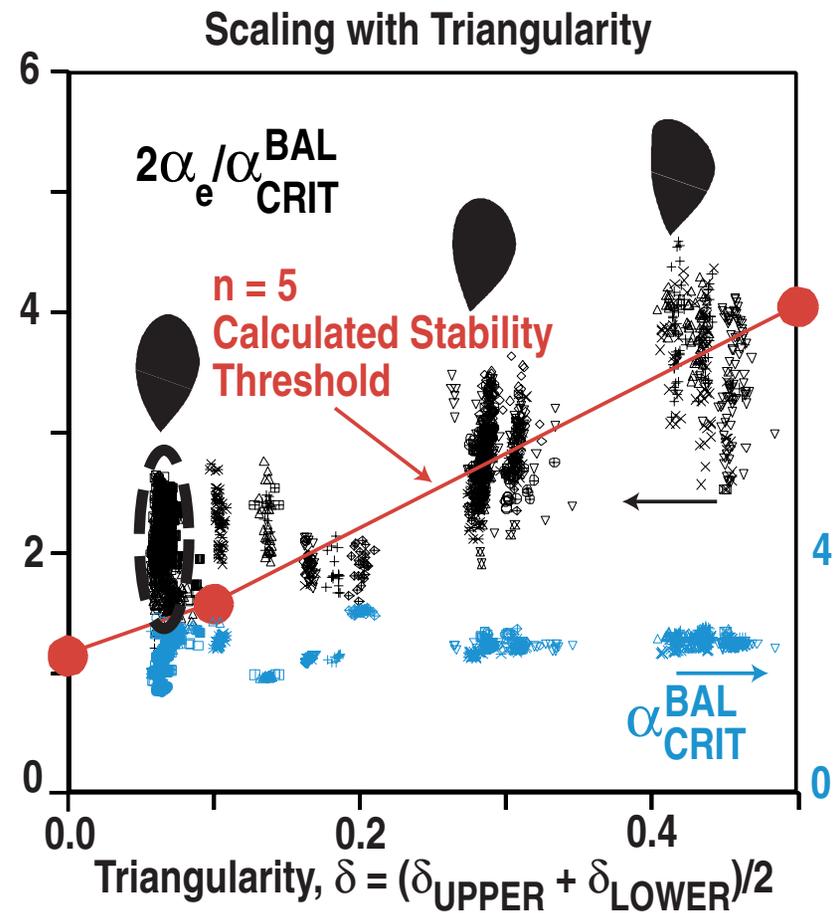
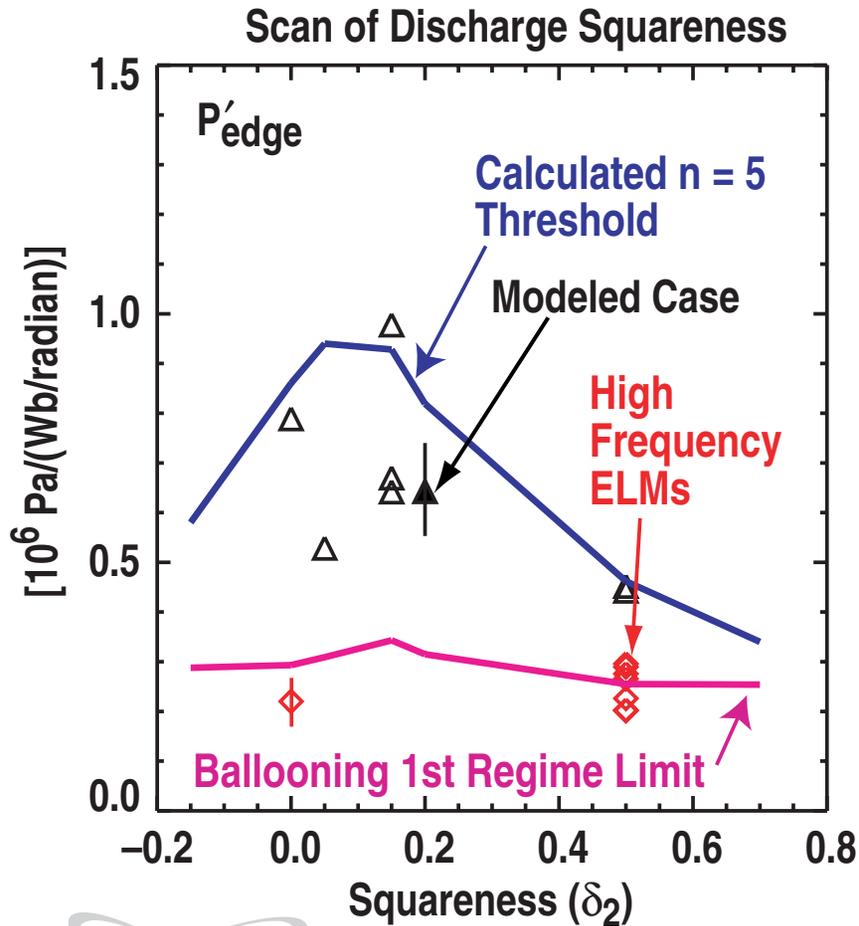
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- The pressure pedestal height is a function of the discharge shape.
- The pedestal height is limited by ELMs.
  - Type I ELM stability has been successfully compared to stability of medium-n ballooning/peeling modes.
- For fixed pedestal width, increasing the height increases the edge-region pressure gradient and bootstrap current.
  - These changes are destabilizing for low-n and medium-n edge-driven modes.
- Additional modeling is probably necessary in order to understand the net effect on global, low-n stability of changes in the pedestal height and width.

# MEASURED $P'_{edge}$ SCALES WITH DISCHARGE SHAPE LIKE THE PREDICTED THRESHOLD FOR $n = 5$ IDEAL, KINK/BALLOONING MODES

- Squareness scan shows quantitative agreement within 40% for similar pedestal width

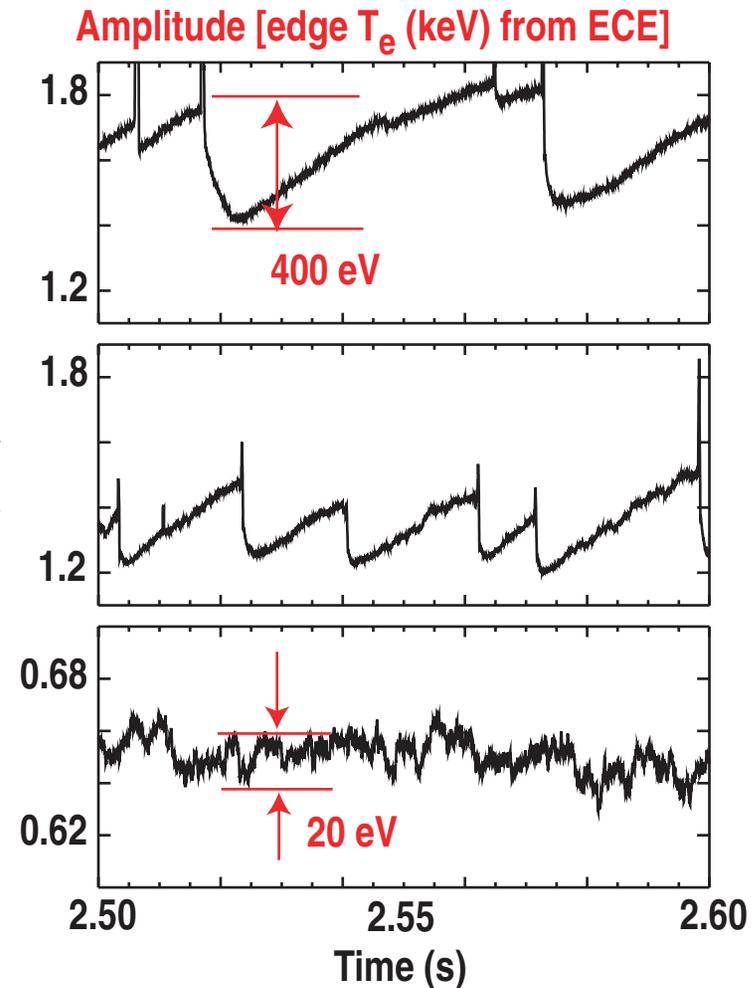
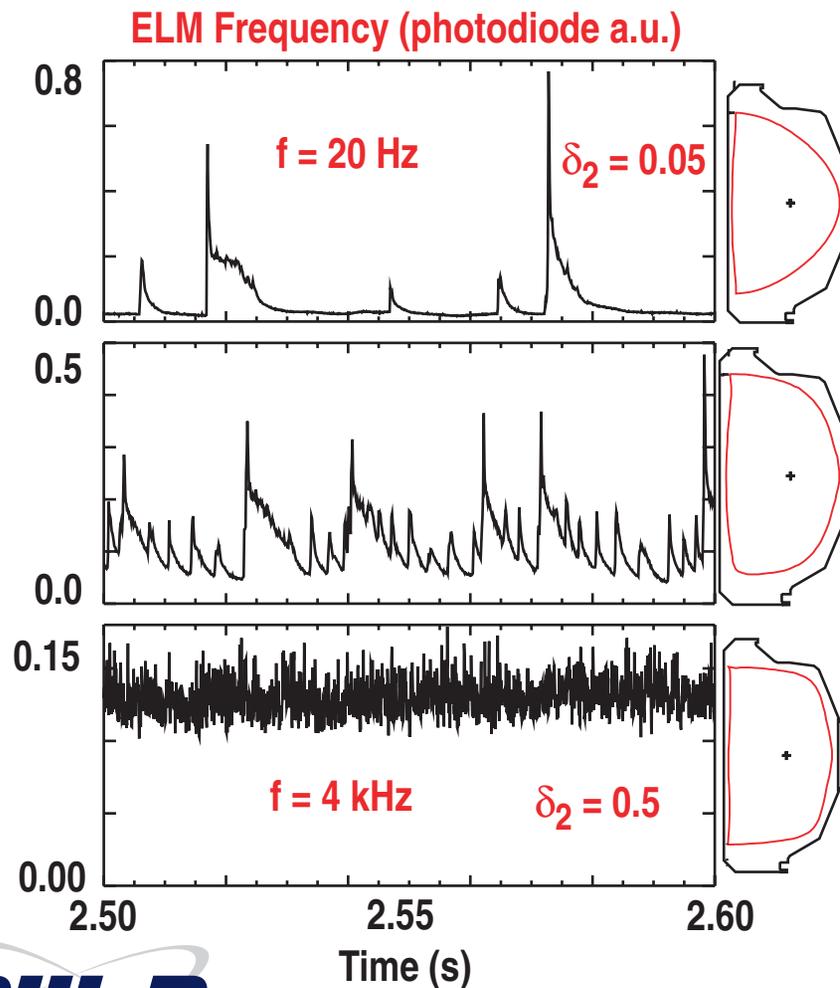
- Pedestal pressure also increases with triangularity



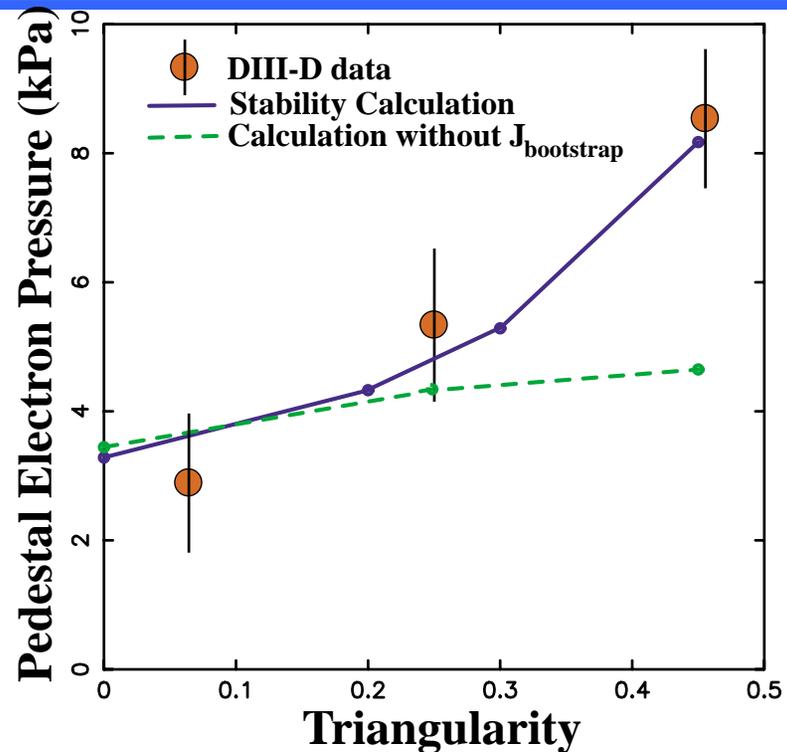
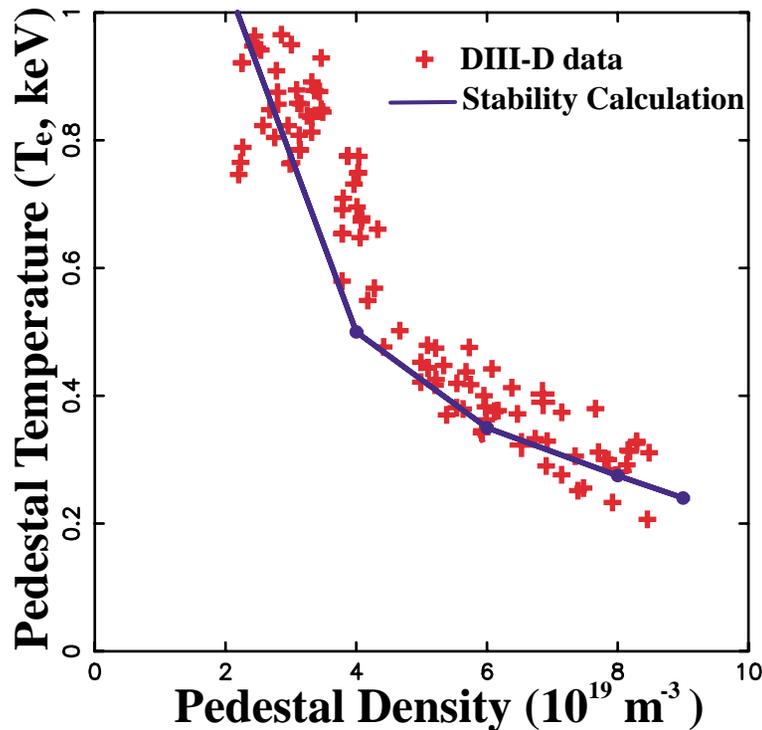
# CHANGE IN BALLOONING 2nd REGIME ACCESSIBILITY IS INDICATED BY CHANGES IN ELM FREQUENCY AND AMPLITUDE

- At sufficiently high squareness:
  - ELM frequency increases a factor of 10
  - $T_e$  perturbations are not measurable

- Abrupt: only a small shape change required



# Trends in Existing Pedestal Database Can Be Understood Using Stability of Model Equilibria



- Trends with density and triangularity calculated using series of model equilibria, and compared to database
  - Inputs are  $B_t$ ,  $I_p$ ,  $R$ ,  $a$ ,  $\kappa$ ,  $\delta$ ,  $\langle n_e \rangle$ ,  $\Delta$
- Strong increase in pedestal height with triangularity is due to opening of second stability access
  - Bootstrap current plays a key role here. Without it (dashed line) second stability is not accessed at high  $n$  and strong  $\delta$  trend not predicted
- Trends with both density and triangularity accurately reproduced: indicates both that pedestal is MHD limited and that model equilibria are sufficiently accurate
  - encourages use of this method as a predictive tool for future devices

# Peeling-ballooning modes provide a constraint on the edge temperature pedestal, as well as $\beta$

Edge current density increases with edge temperature (Ohmic+collisional bootstrap)

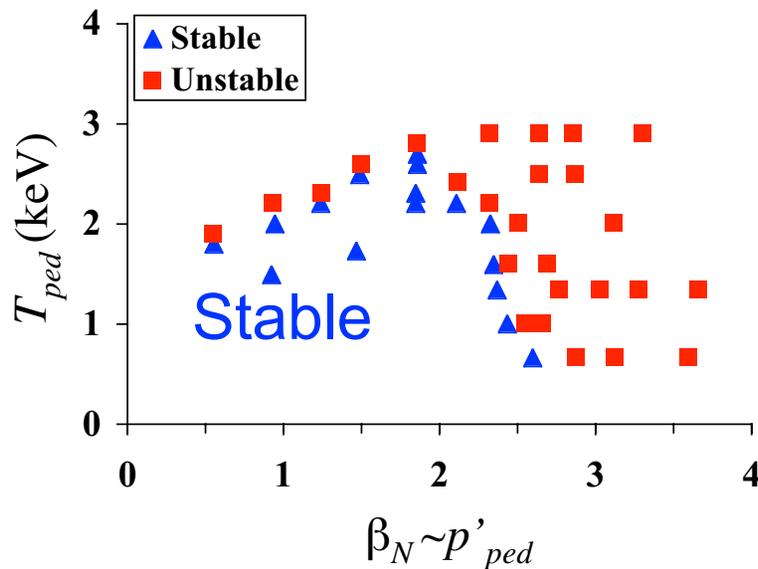
Can consider stability diagram in  $\beta_N$ - $T_{ped}$  space

MHD stability explicitly limits steady state  $T_{ped}$ , (for a given width)

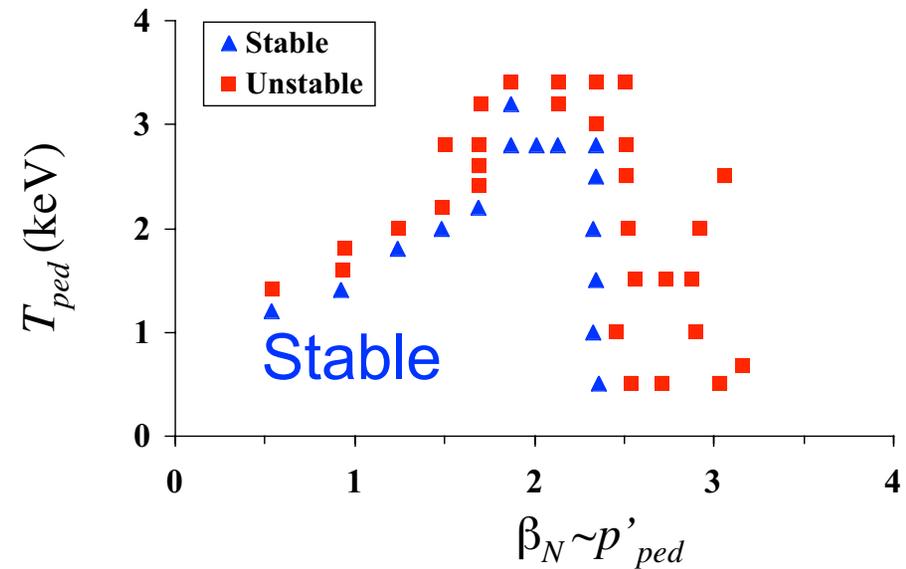
Higher triangularity decouples peeling and ballooning modes, allows higher temperature pedestal

$\kappa=1.6, A=3, R=3m$

$\delta=0.3$



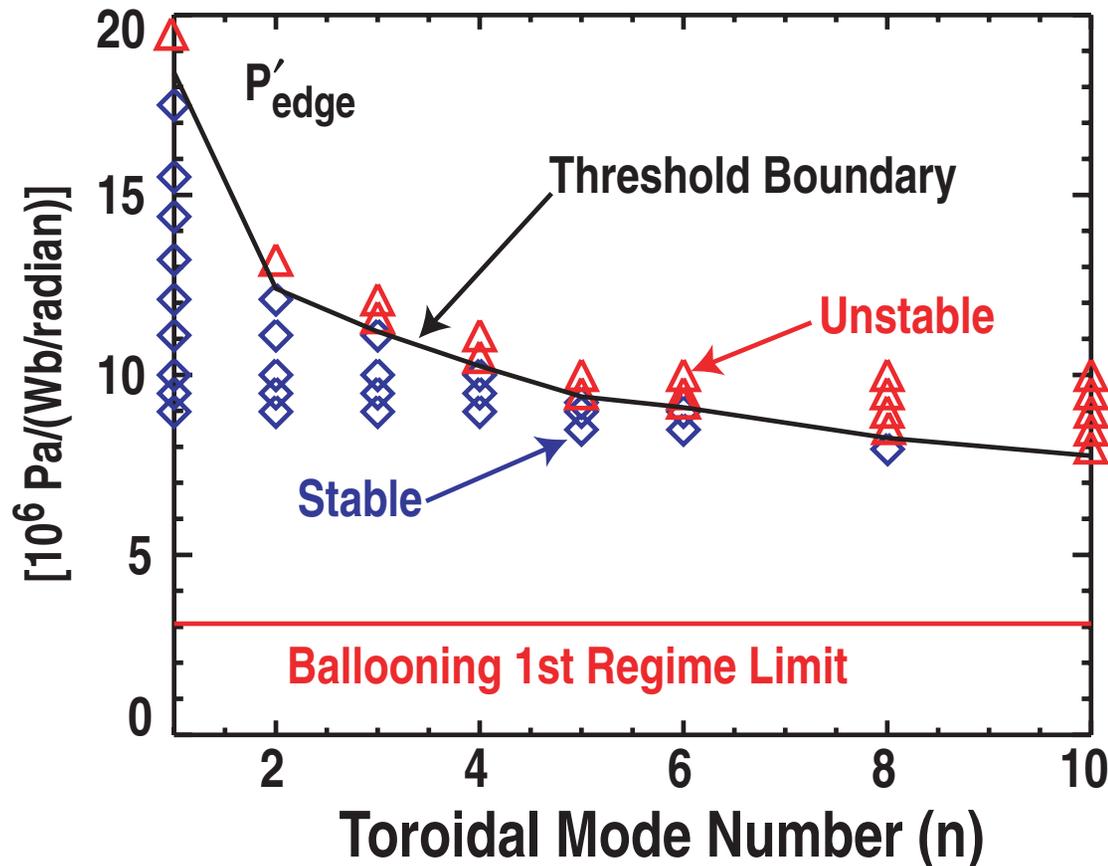
$\delta=0.5$



# MODE WITH THE LARGEST $n$ WITHOUT 2nd STABLE REGIME ACCESS WILL HAVE THE LOWEST $P'_{edge}$ STABILITY THRESHOLD

- Calculated  $P'_{edge}$  threshold decreases with toroidal mode number
- Fixed, medium squareness ( $\delta_2 = 0.05$ ) shape, wall radius =  $1.5\alpha$ , GATO code

## Calculated Stability Threshold (Full Geometry)



# OPTIMIZATION OF ADVANCED TOKAMAK DISCHARGES WITH RESPECT TO THE BETA LIMIT IS POSSIBLE THROUGH TUNING OF THE $q$ PROFILE, PRESSURE PROFILE AND DISCHARGE SHAPE

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- Goal: find the best way to operate at high  $\beta_N$  and  $q$  in order to maximize  $f_{BS}$  for steady-state and  $\beta_T$  for fusion gain
- A test of the effect of a broader pressure profile resulted in increased  $\beta_N$ 
  - From modeling, pressure profile broadening could allow large increases in achievable beta
- $q_{min} \beta_N$  increased from 6 at  $q_{min} = 1.5$  to 9 at  $q_{min} \approx 2.3$ , the highest value tested
  - Increasing  $f_{BS}$  by increasing  $q_{min}$  is feasible with broad pressure
- Operation is routinely above the no-wall stability limit
  - Optimized correction of nonaxisymmetric fields and active feedback stabilization of the RWM are essential
- Highest experimental  $\beta_N$  values were obtained in balanced double-null discharge shapes with the largest  $\kappa, \delta$

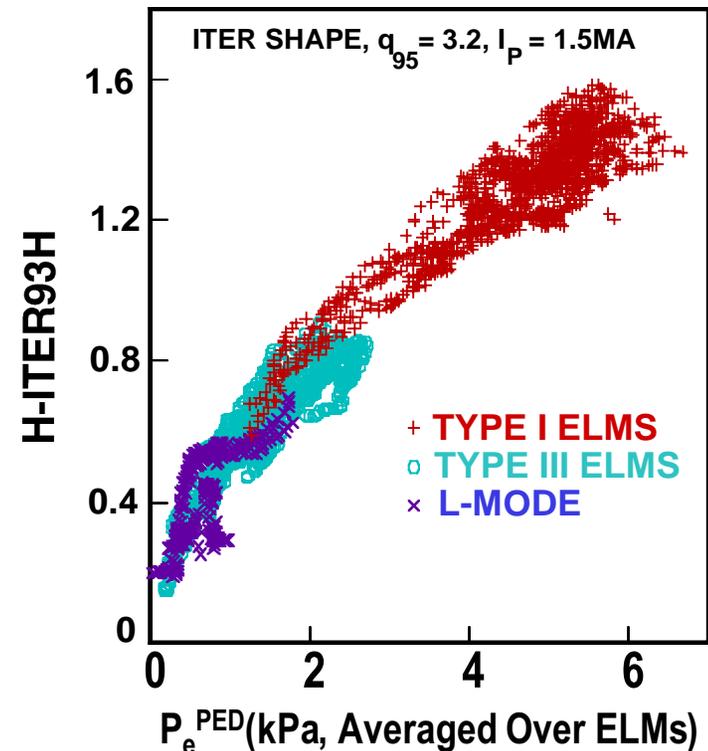
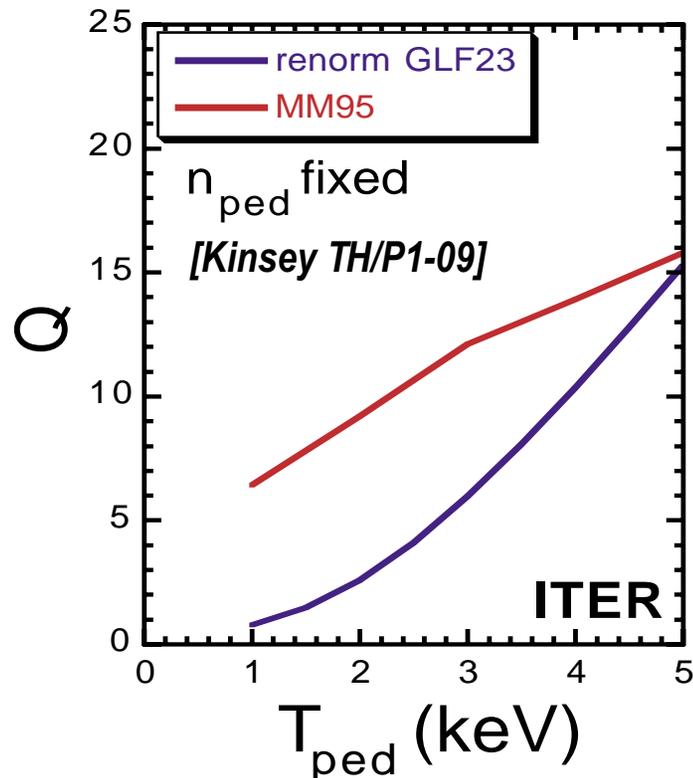
# UPCOMING WORK IN DIII-D IS WELL POSITIONED TO FOLLOW THE PATH TO HIGH $\beta_N$ AT INCREASED $q_{\min}$ INDICATED BY THESE RESULTS

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- Additional power for electron cyclotron and fast wave current drive will be available to control  $q_{\min}$  and  $q(0)$
- Conversion of 1/4 of the neutral beams to counter-injection will allow additional rotation profile control
  - Together with current profile control, provides a possible mechanism for pressure profile broadening through energy transport modification
- Lower divertor pump to be converted to pump higher triangularity double-null divertor discharges
- Recently installed internal nonaxisymmetric coils will be used for improved error field correction and improved active RWM feedback control to allow steady-state operation close to the ideal-wall beta limit

# Pedestal & ELMs Key to Plasma Performance

- Both theory and experiment indicate a strong dependence of core confinement, and therefore  $Q$  on the pedestal height ( $p_{ped}$ ,  $T_{ped}$ )

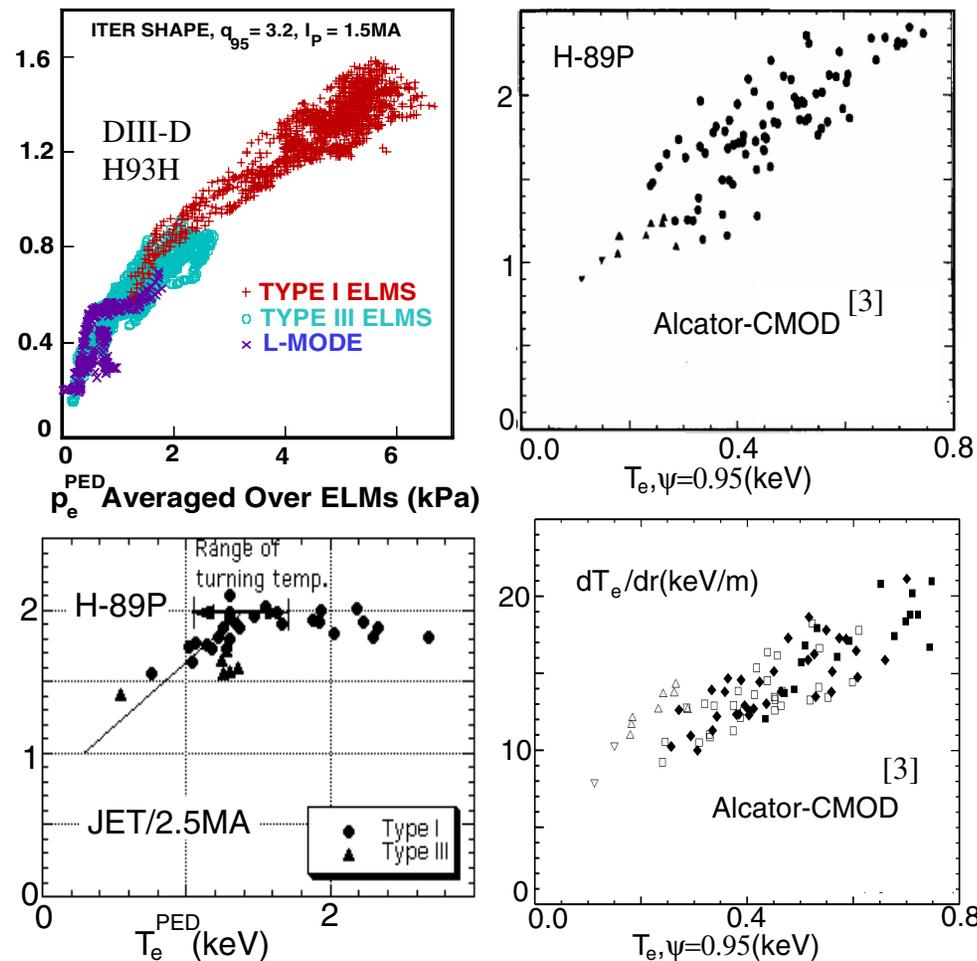


- ELM characteristics strongly impact divertor and wall heat load constraints (large Type I ELMs may not be tolerable in Burning Plasma devices)
- ➔ Goal is predictive understanding of physics controlling pedestal height and ELM characteristics  $\Rightarrow$  combination of high pedestal and tolerable ELMs

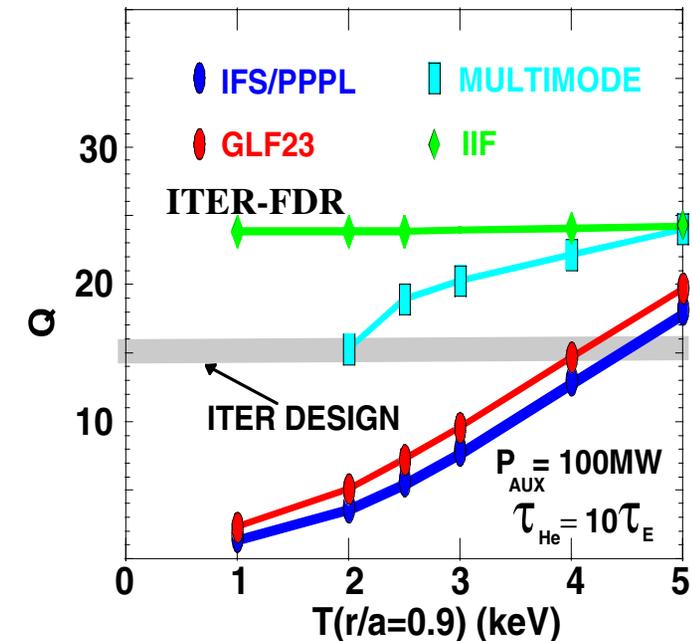
# H-mode pedestal may impact H-mode based tokamak reactor performance through temperature profile stiffness.

- ◆ Maximum  $P_F$  and  $Q$  are obtained at min  $\langle T \rangle$  for stable operation  $\Rightarrow P_F/P_{LOSS} \sim H^2$

Effect of H-mode pedestal on H factor varies with tokamak possibly due to changes in turbulent transport process<sup>[2]</sup>



Turbulent transport simulations that predict stiff temperature profiles (ITG) show strong dependence of core on edge<sup>[1]</sup>



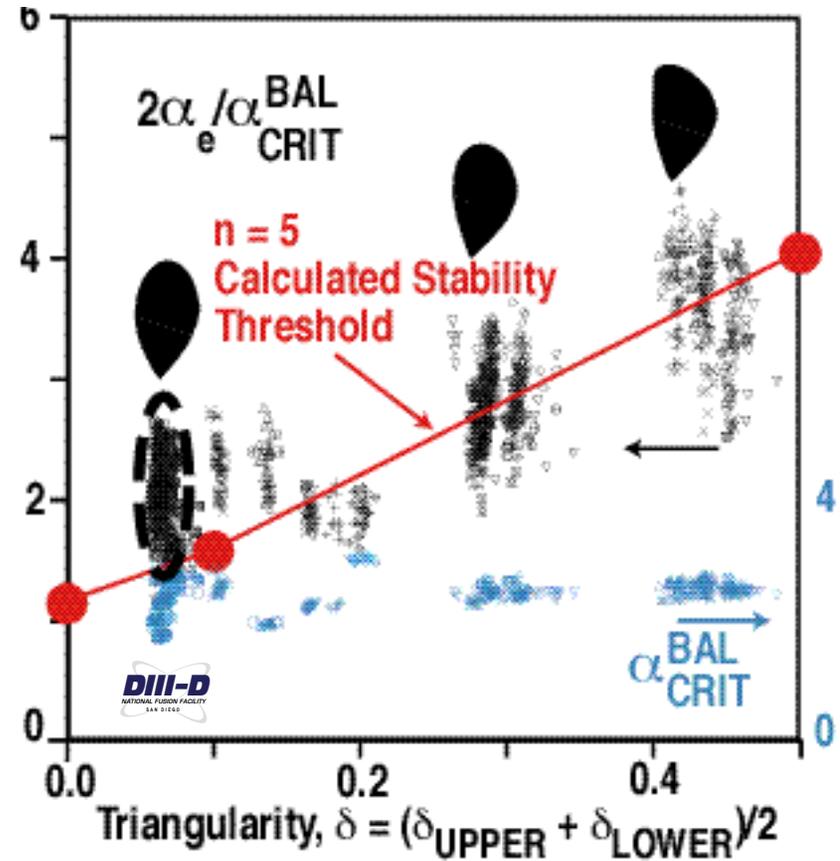
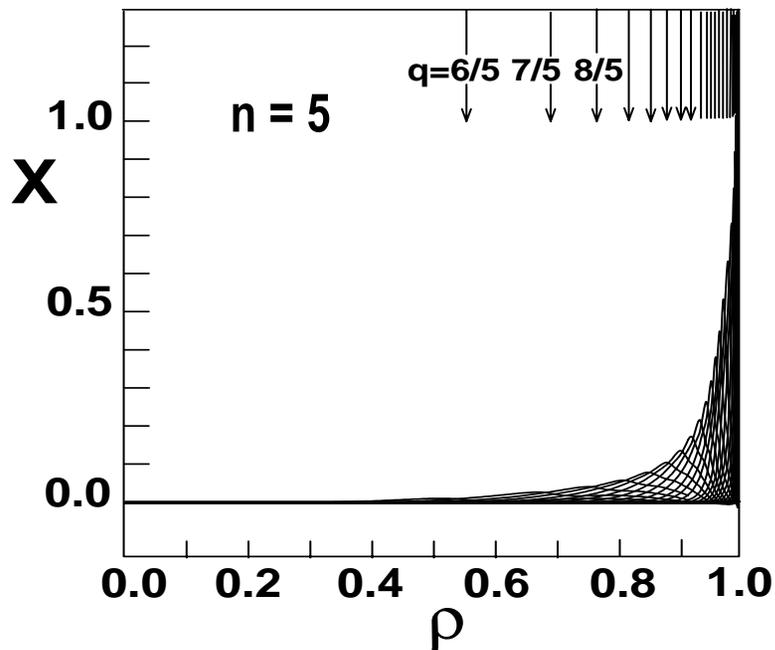
[1] J.E. Kinsey, et al., *Berchtesgarden EPS*, III 1081 (1997)

[3] M. Greenwald, et. al *Nucl. Fus.* 37 (1997) 793.

[2] G.Janeschitz, et.al *Maastricht EPS*, 23J (1999) 1445.

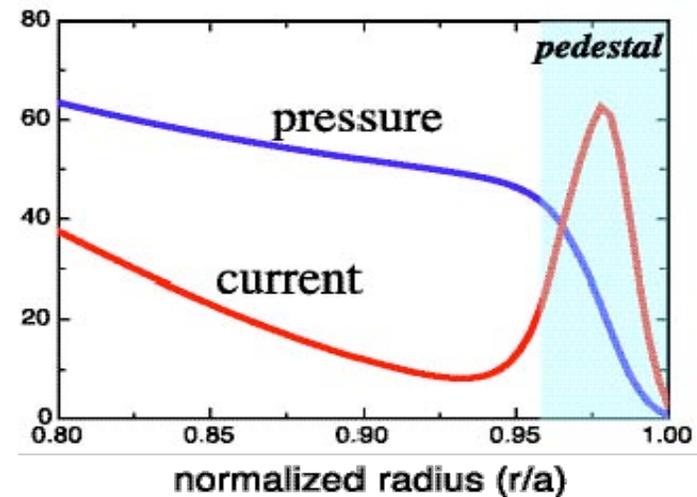
# Intermediate $n$ Peeling-Ballooning Mode Model of the Type I ELM Instability is Consistent With Observations

- $P'$  variation with shape in DIII-D, JT-60U, and AUG consistent with edge peeling-ballooning stability
- ELM onset time consistent with predicted instability onset
- Fast growing low  $1 < n < 30$  modes are observed as Type I ELM precursors

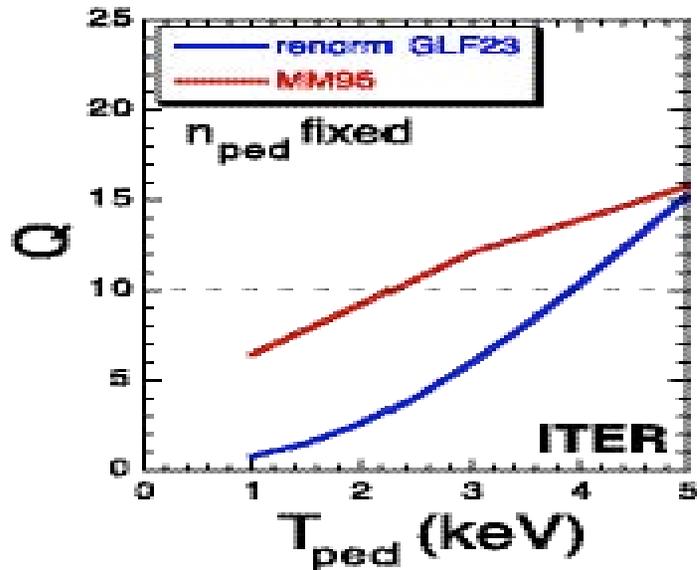


# Motivation and Background

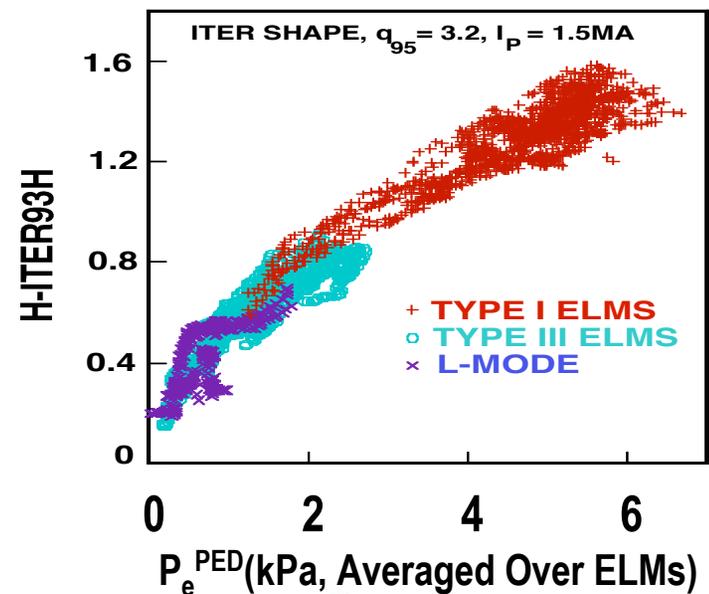
- ELMs and the edge pedestal are key fusion plasma issues
  - “Pedestal Height” controls core confinement and therefore fusion performance (Q)
  - ELM heat pulses impact plasma facing materials



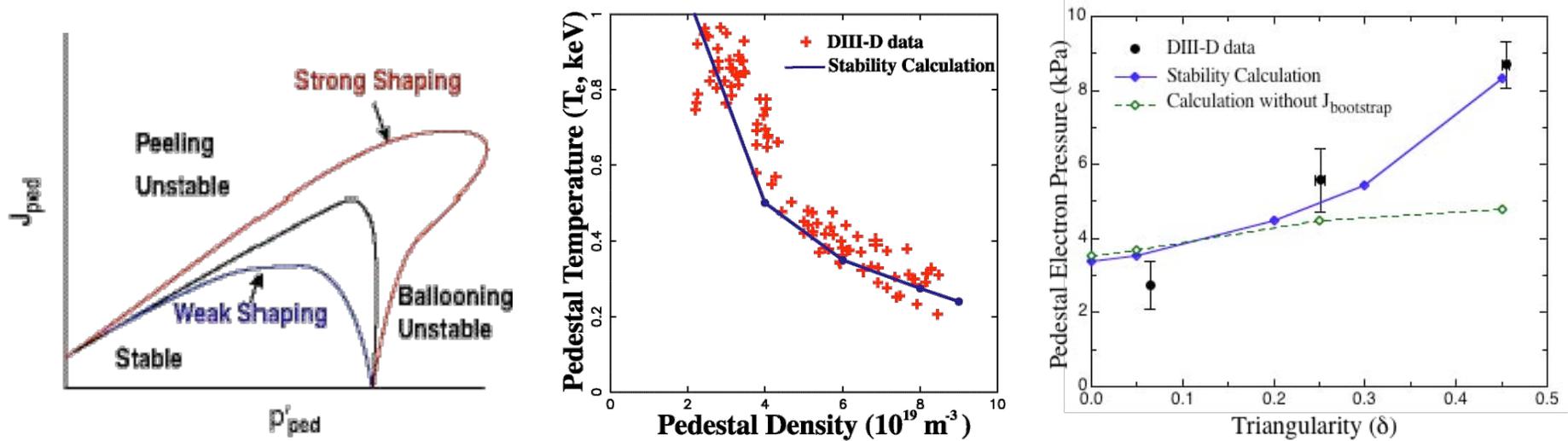
Predicted Impact of Pedestal Height



Observed Impact of Pedestal Height (DIII-D)



# Background: Extending the Peeling-Ballooning Model



- Peeling-Ballooning Model of ELMs - significant successes
  - ELMs caused by intermediate wavelength ( $n \sim 3-30$ ) MHD instabilities
    - Both current and pressure gradient driven
    - Complex dependencies on  $v_*$ , shape etc due to bootstrap current and “2nd stability”
  - Successful comparisons to experiment both directly and in database studies
- Need to understand sources and transport to get profile shapes (“pedestal width”)
- Rotation and non-ideal effects to precisely characterize P-B limits, nonlinear dynamics for ELM size